

The Symmetry Energy at very low, low, and high densities in Heavy Ion Colisions

or

All you ever wanted to know about the Symmetry Energy, but ...



Hermann Wolter
Ludwig-Maximilians-Universität München (LMU)



International Collaborations in Nuclear Theory (ICNT):
Program 2013: „Symmetry Energy in the Context of New Radioactive Beam Facilities and Astrophysics“
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Points to discuss:

- **Definition of the Nuclear Symmetry Energy (NSE)
in nuclei, nuclear matter and astrophysics**
- **NSE in microscopic calculations (also at very low densities with correlations)**
- **Investigation of the NSE in Astrophysics and Heavy ion collisions (HIC)**
- **Transport theory: approximations and implementations
fluctuations, formation of fragments**

NSE at various densities in HIC

- $\rho \ll \rho_0$: clustered matter
- $\rho \sim \rho_0$: barrier to Fermi Energy regime, isospin transport
ex.: isospin diffusion, pre-equilibrium emission
constraints
- $\rho > \rho_0$: reaction mechanism, observables
flow, particle production (pion, Kaon)

This is supposed to be an informal talk, and it can only touch on many questions!

Definitions of the Symmetry Energy

Equation-of-State and Symmetry Energy

BW mass formula

$$E(A,Z)/A = a_v - a_s A^{-1/3} - a_c Z(Z-1)A^{-4/3} - a_c (N-Z)^2 / (N+Z)^2 + \delta_{pair}$$

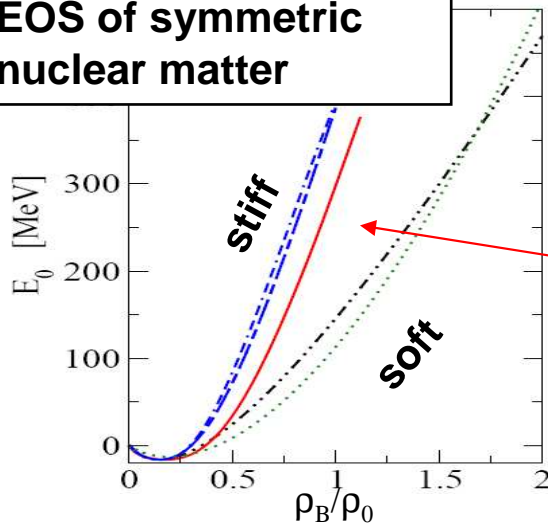
density-asymmetry dep. of nucl.matt.

$$E(\rho_B, \delta) / A = E_{nm}(\rho_B) + E_{sym}(\rho_B) \delta^2 + O(\delta^4) + \dots$$

$$\delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$

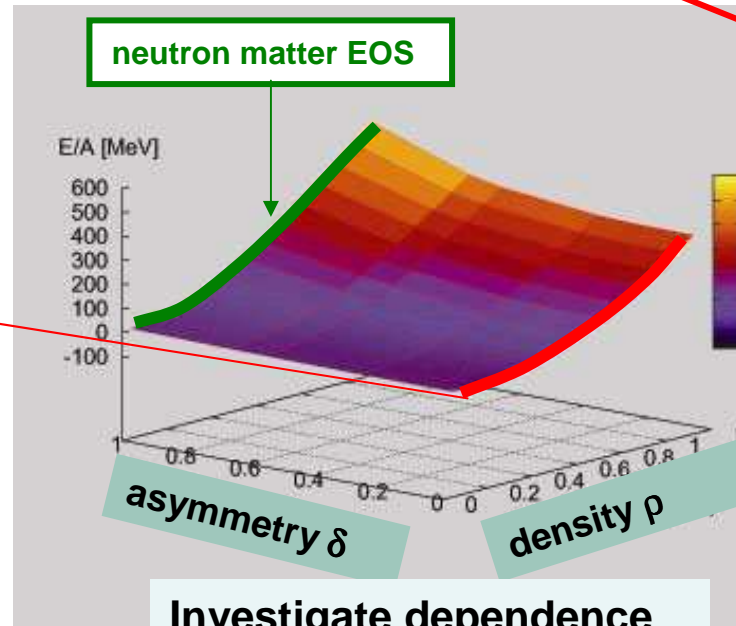
symmetry energy

EOS of symmetric nuclear matter



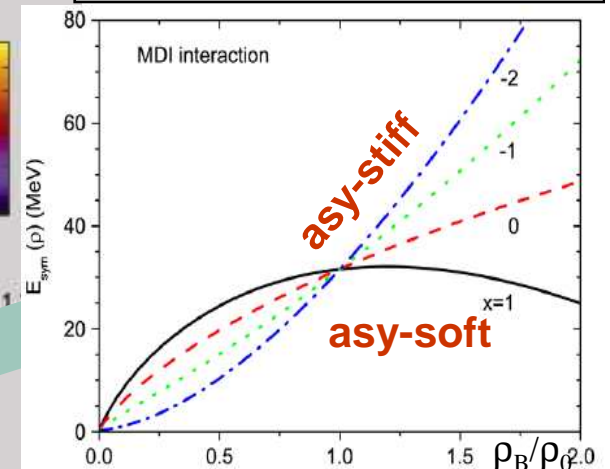
Fairly well fixed! Soft

neutron matter EOS



Investigate dependence in large part of (rho, delta)-plane

Symmetry energy: Diff. neutron and symm matter



Rather uncertain! esp. at high density Isovector tensor correlations?

Question: 2nd deriv

$$E_{sym}(\rho) = \frac{1}{2} \frac{\partial^2}{\partial \beta^2} E(\rho, \beta) \Big|_{\beta=0}$$

or finite diff

$$E_{sym}(\rho) = E(\rho, \beta = -1) - 2E(\rho, \beta = 0) + E(\rho, \beta = 1)$$

quadratic over a large interval of beta?

1.5 Representations of Symmetry Energy

$$E(\rho_B, \delta) / A = E_{nm}(\rho_B) + E_{sym}(\rho_B) \delta^2 + O(\delta^4) + \dots$$

$$\Rightarrow \frac{1}{3} \epsilon_F(\rho / \rho_0)^{2/3} + E_{sym}^{pot}(\rho)$$

$$\delta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$

Parametrizations:

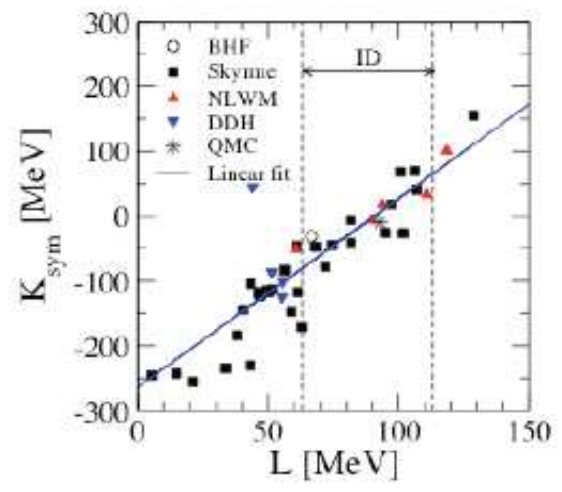
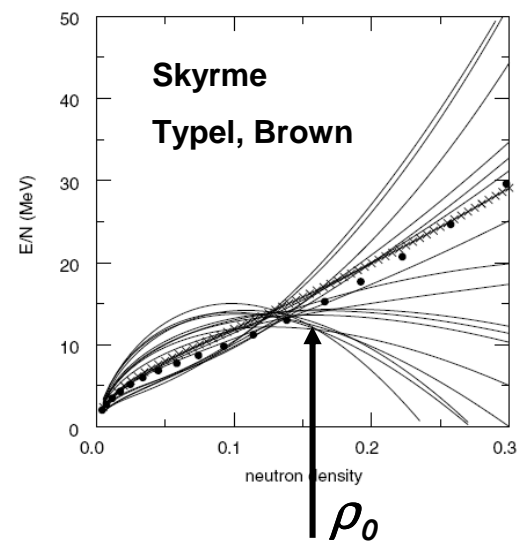
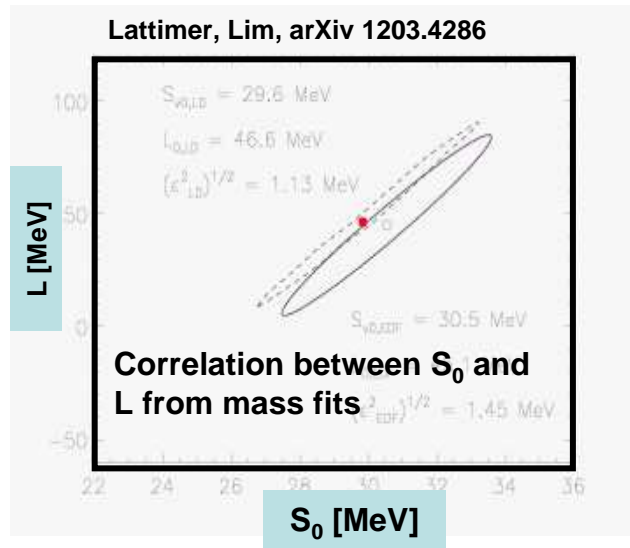
- 2. polynomial behaviour
- 3. Expansion around ρ_0

$$E_{sym}^{pot} = C (\rho / \rho_0)^\gamma$$

$$E_{sym}(\rho) = S_0 + \frac{L}{3} \left(\frac{\rho - \rho_0}{\rho_0} \right) + \frac{K_{sym}}{18} \left(\frac{\rho - \rho_0}{\rho_0} \right)^2$$

} Relation between γ and L

correlations



Correlation between L and K_{sym} ?

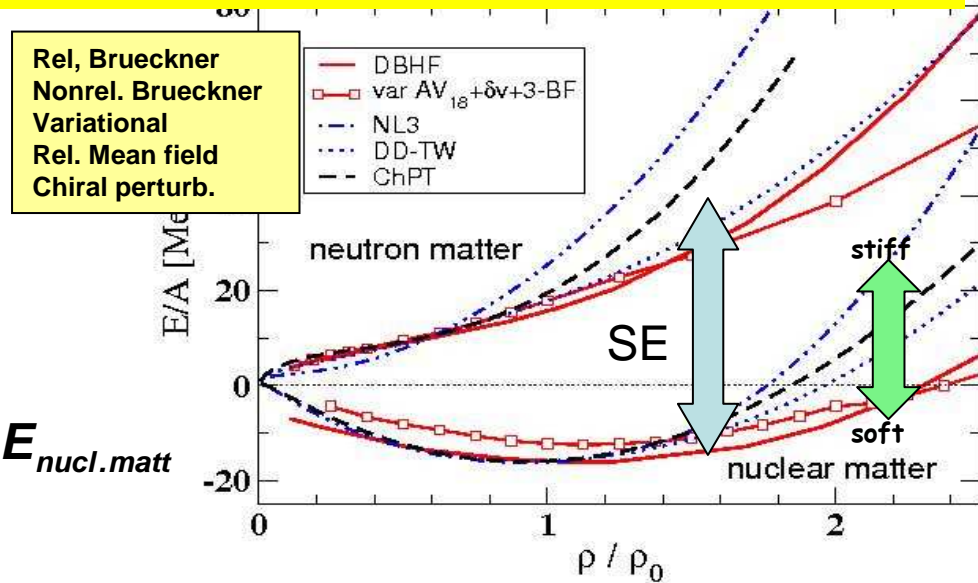
The Nuclear Symmetry Energy in different „realistic“ models

The EOS of symmetric and pure neutron matter in different many-body approaches

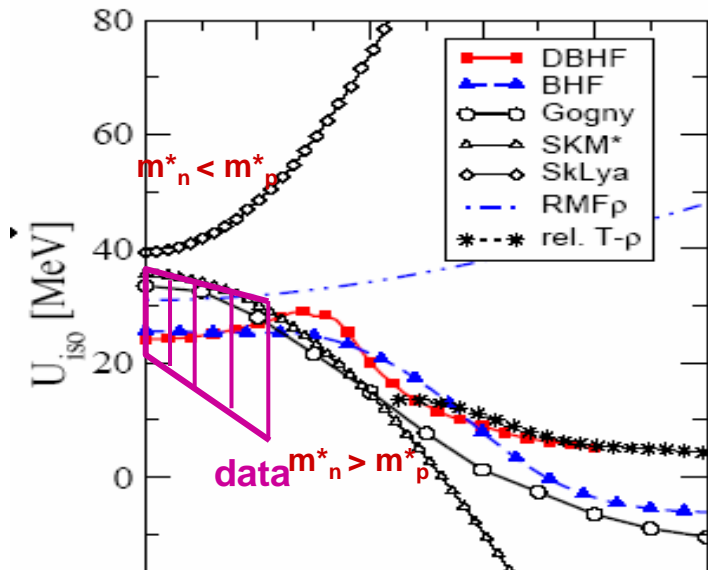
C. Fuchs, H.H. Wolter, EPJA 30(2006)5,(WCI book)

The symmetry energy as the difference between symmetric and neutron matter:

$$E_{sym} = E_{neutr.matt} - E_{nucl.matt}$$



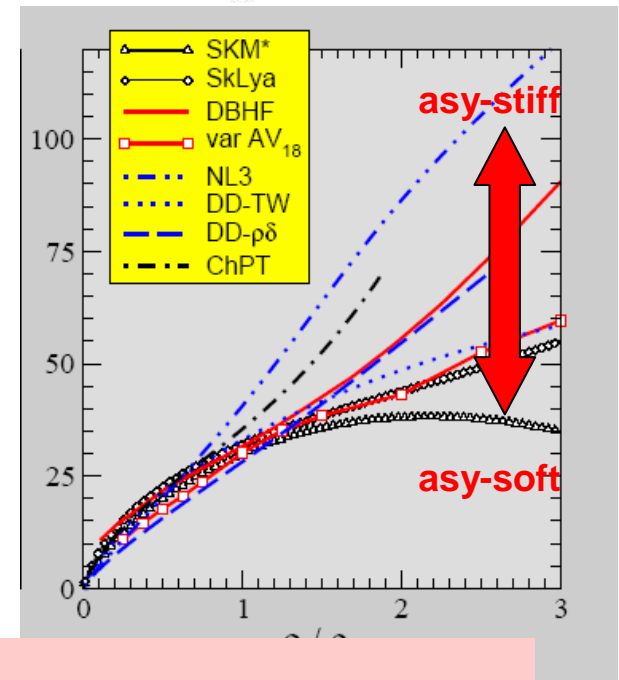
SE is also momentum dependent \rightarrow effective mass



Different proton/neutron effective masses

$$\frac{m_q^*}{m} = \left[1 + \frac{m}{\hbar^2 k} \frac{\partial U_q}{\partial k} \right]^{-1}$$

Isovector (Lane) potential: momentum dependence



Why is symmetry energy so uncertain??

\rightarrow In-medium ρ mass, and short range tensor correlations (Xu, BA. Li, PRC81 (2010) 064612);

Very low density matter in Astrophysics

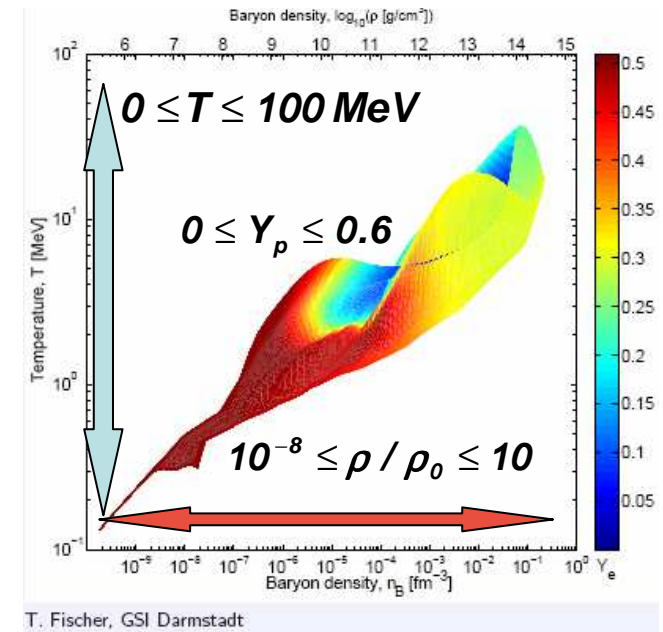


In Supernova simulations the Equation-of-State appears for a wide range of Densities, temperatures and asymmetries.

In particular also at very low densities, where correlations become important.

Various commonly used EoS's treat this in a phenomenological manner (e.g. Lattimer, Swesty; Shen, Toki; Shen, Horowitz, Teige))

There exists an exact low density limit, the Virial Theorem (Horowitz, Schwenk)



Attempted Improvements: (S.Type1, G. Röpke, T. Klähn, D. Blaschke, HHW, PRC 81, 015803 (2010))

-medium effects on light clusters, quantum statistical approach

-description of low to high density clustered matter in dens.-dep. rel. mean field model (DD-RMF)

Theoretical approach:

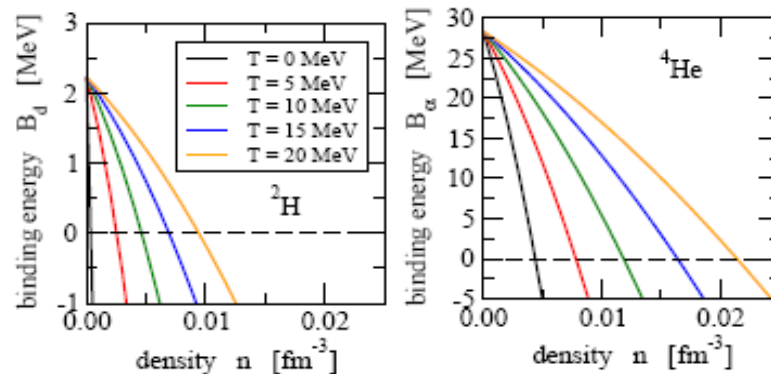
Typel, Röpke, Klähn, Blaschke,
Wolter, PRC81,015803(2010)

Quantumstatistical model (QS)

- Includes medium modification of clusters (Mott transition)
- Includes correlations in the continuum (phase shifts)
- needs good model for quasi-particle energies in the mean field

Generalized Rel. Mean Field model (RMF)

- Good description of higher density phase, i.e. quasiparticle energies
- Includes cluster degrees of freedom with parametrized density and temperature dependent binding energies
- Heavier clusters treated in Wigner-Seitz cell approximation (

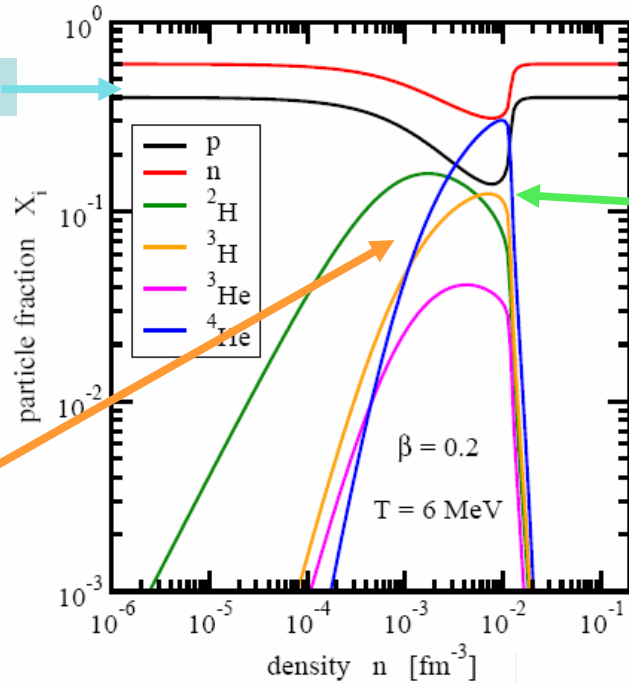


Global approach from very low to high densities

Particle Fractions

very low density: p,n

Increasing density:
clusters arise: deuteron
first, but then α
dominates



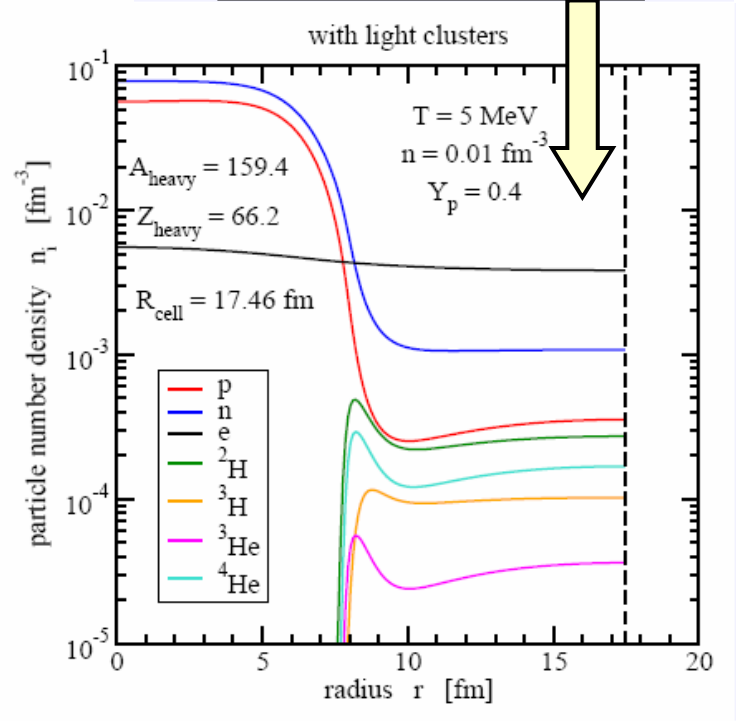
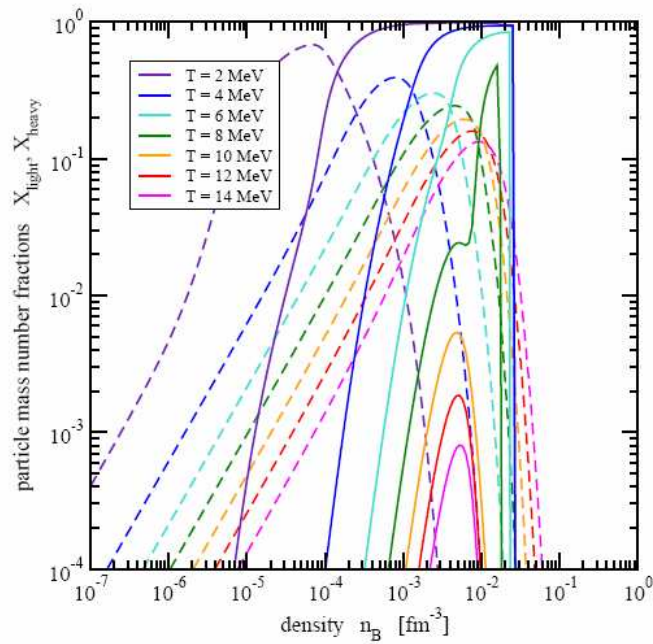
Mott density:
clusters melt,
homogeneous p,n
matter;

here heavier nuclei
(embedded into a
gas) become
important, not yet
fully implemented

Calculation in RMF of
heavy cluster in
Wigner-Seitz cell in
beta-equilibrium

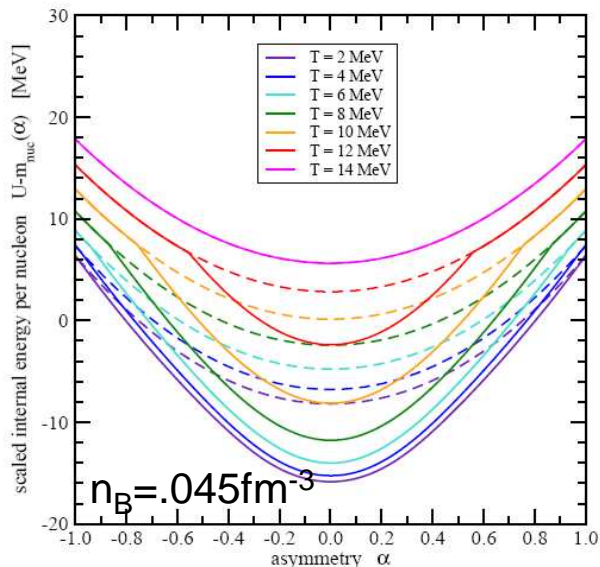
S.Typel, G. Röpke, et al., PRC 81 (2010)

Heavier clusters
(nuclei)
(- - -) light
(—) heavy
fraction



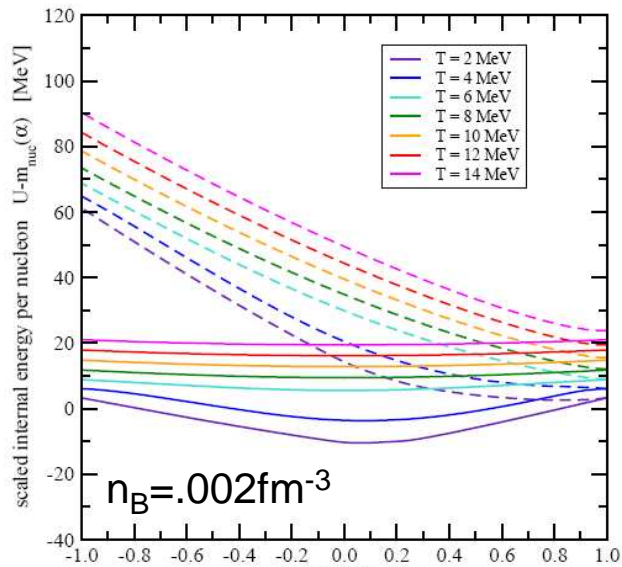
Symmetry Energy in Nuclear and Stellar Matter

Nuclear Matter (w/o clusters) without (-----) and with (——) liquid-gas phase transition

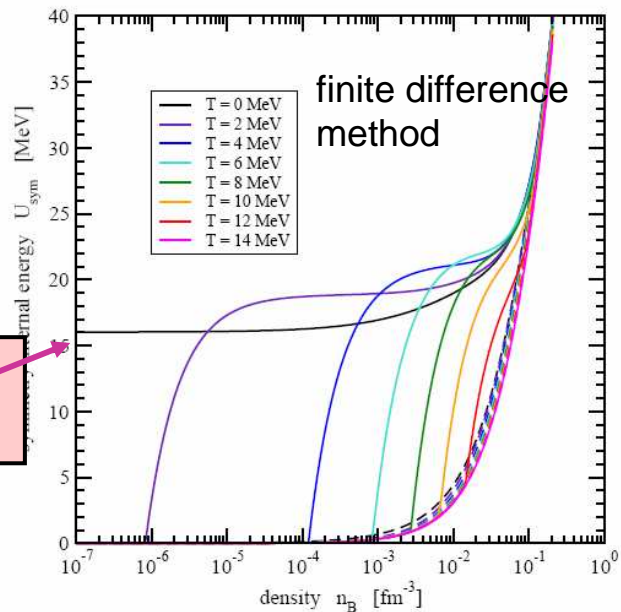


Internal Energy

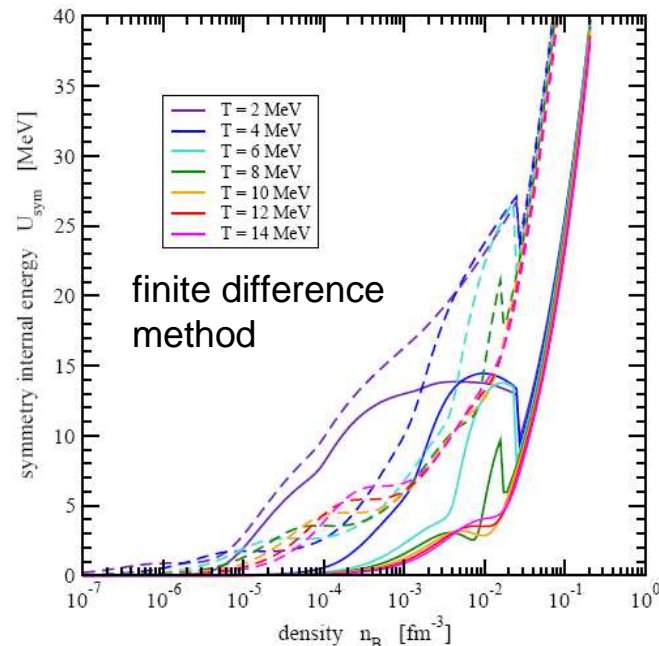
Stellar Matter (with electrons and with clusters) without (-----) and with Coulomb contrib removed (——)



Symmetry Energy

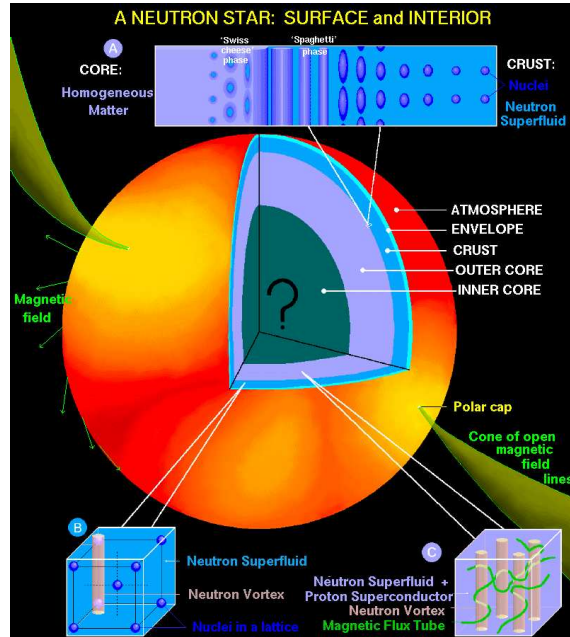


finite at $T=0$ due to PT



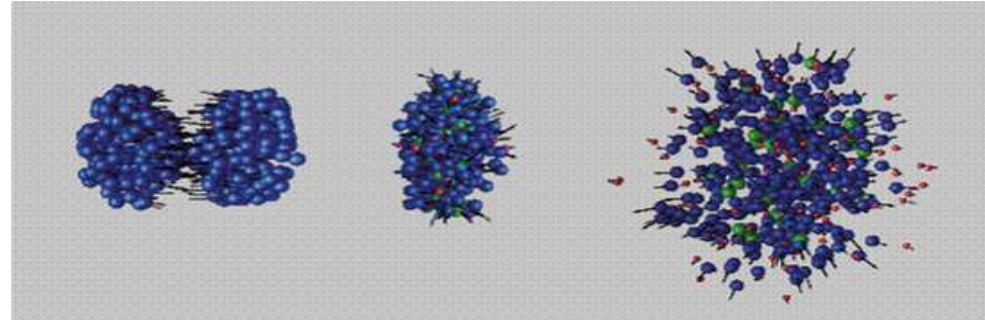
Constraints on EoS via Astrophysical Observation and Laboratory Experiments

Model for structure of NS



Simple (in some parts) and equilibrated system, but difficult to observe

Heavy ion collisions

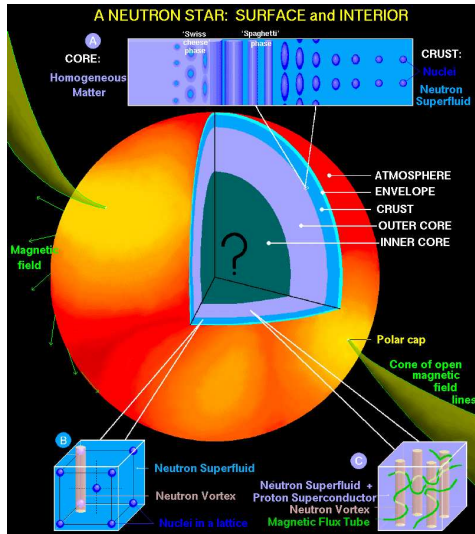


Complex system not in equilibrium, but manageable in the lab

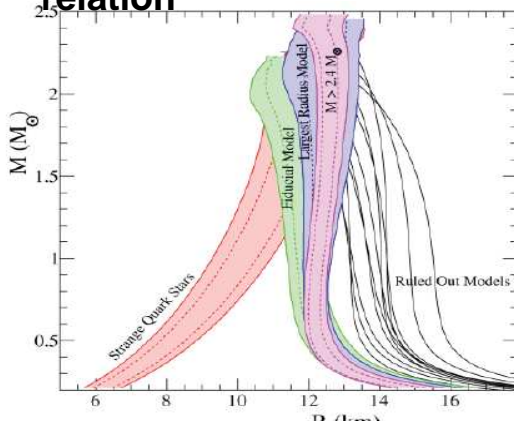
The Symmetry Energy in Astrophysics

Constraints on EoS from Astrophysical Observation

Observations of:
 masses
 radii (X-ray bursts)
 rotation periods

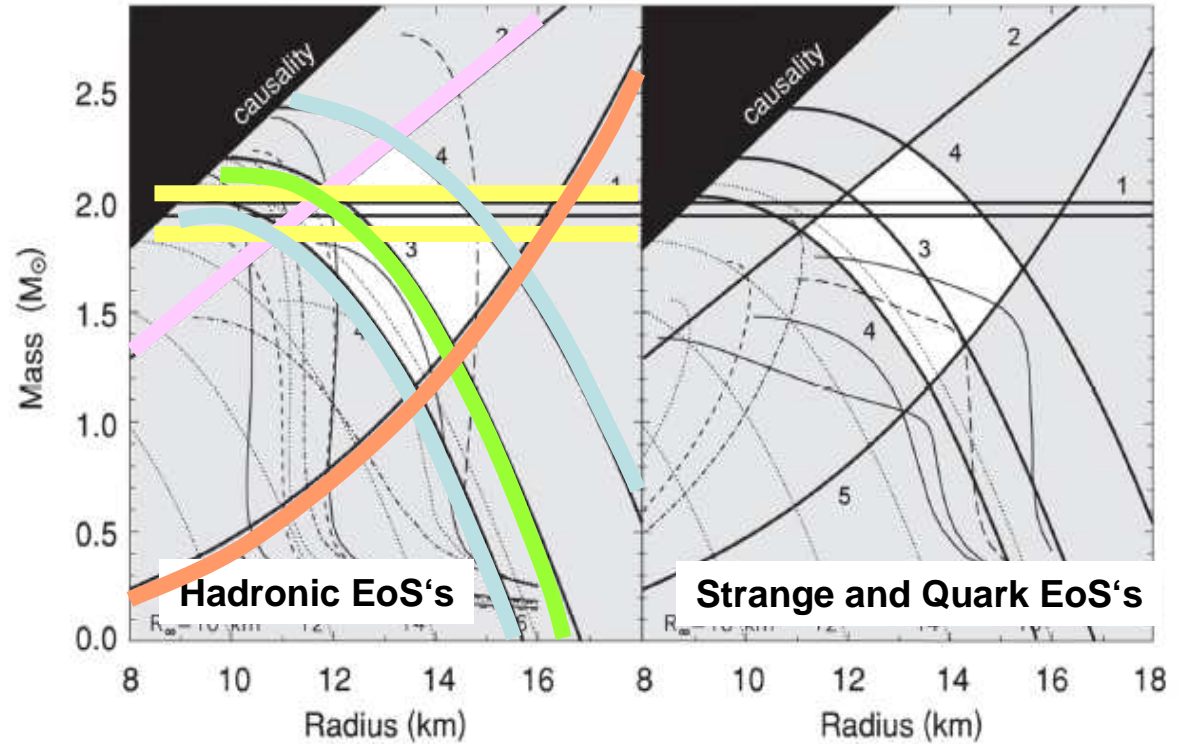


Neutron star mass-radius relation



Steiner, Lattimer, arXiv 1205.6871

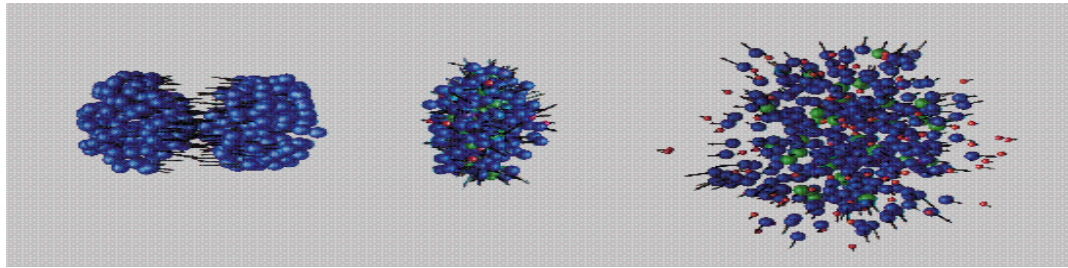
Trümper Constraints (Universe Cluster, Irsee 2012)



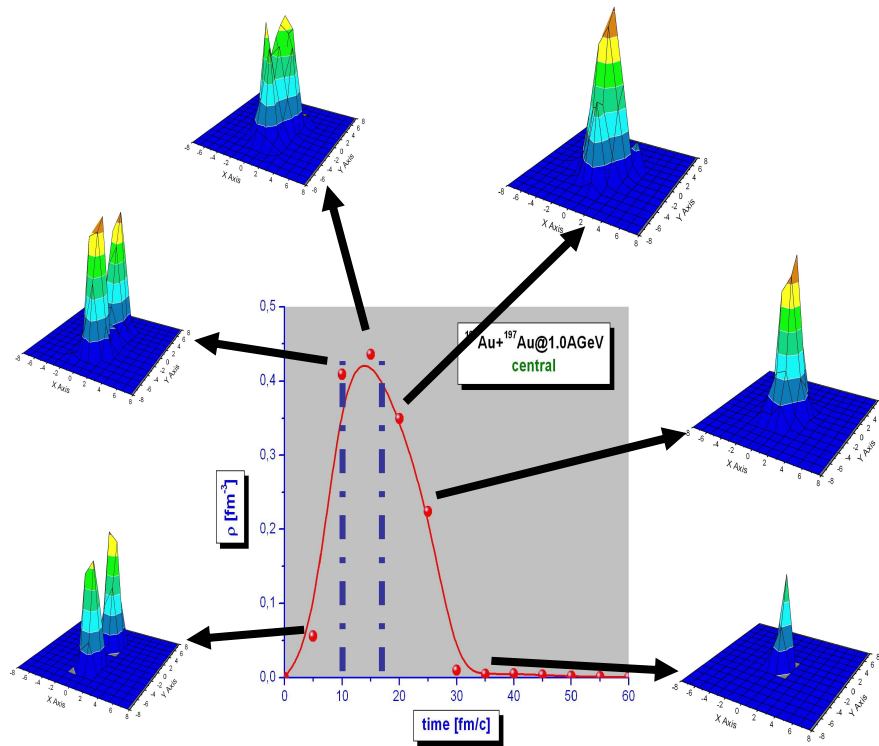
Stringent constraint on many EoS models

Transport Theory for Heavy Ion Collisions

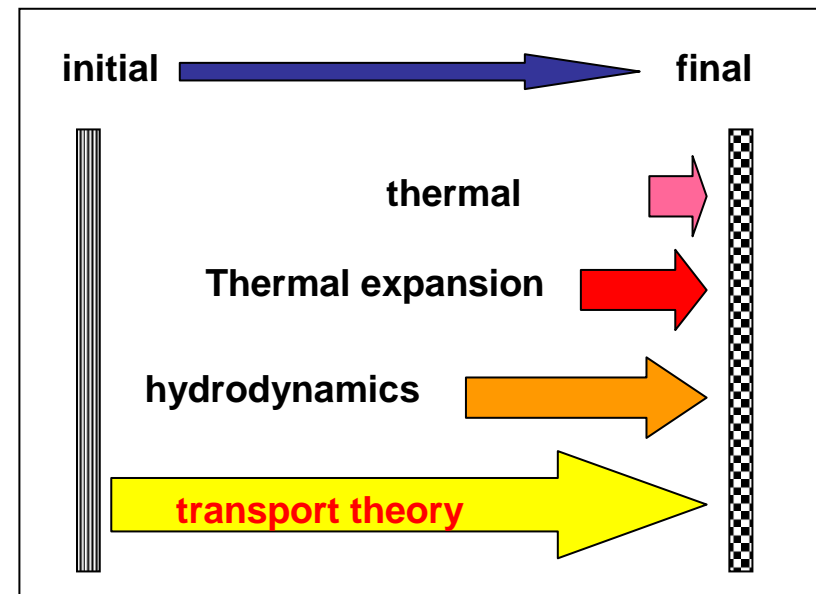
Heavy ion collisions



non-equilibrium



Levels of description of evolution
from initial to final state:



Transport equations

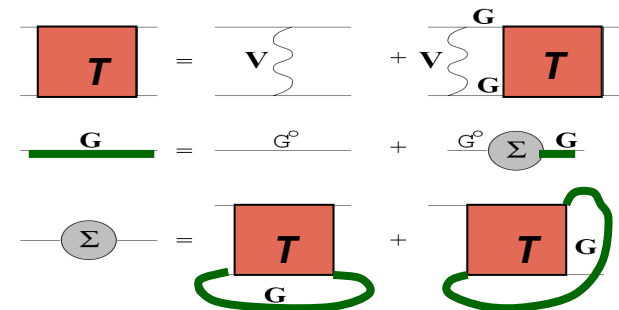
Boltzmann-Ühling-Uhlenbeck (BUU)

$$\frac{\partial f}{\partial t} + \frac{\vec{p}}{m} \vec{\nabla}^{(r)} f - \vec{\nabla} U(r) \vec{\nabla}^{(p)} f(\vec{r}, \vec{p}; t) = \int d\vec{v}_2 d\vec{v}_{1'} d\vec{v}_{2'} v_{21} \sigma_{12}(\Omega) (2\pi)^3 \delta(\vec{p}_1 + \vec{p}_2 - \vec{p}_{1'} - \vec{p}_{2'}) [f_{1'} f_{2'} (1 - f_1)(1 - f_2) - f_1 f_2 (1 - f_{1'})(1 - f_{2'})]$$

Can be derived:

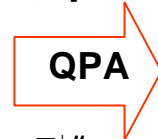
- Classically from the Liouville theorem
- Semiclassically from THDF
- From non-equilibrium theory (Kadanoff-Baym) collision term included mean field and in-medium cross sections consistent, e.g. from BHF

} collision term added (and fluctuations)



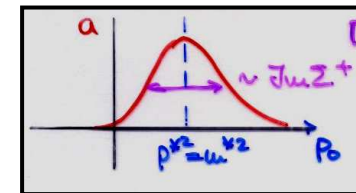
Spectral fcts, off-shell transport, quasi-particle approx.

$$A(x, p) \propto \frac{2\Gamma(x, p)}{(p^{*2} - m^{*2}) + \Gamma^2(x, p)}$$



$$\propto \delta(p^{*2} - m^{*2}) \Theta(p^{*0})$$

$$\Gamma(x, p) = m^* \text{Im} \Sigma_s^+ - p_\mu^* \text{Im} \Sigma^{+\mu}$$



Transport theory is on a well defined footing, **in principle – but in practice??**

Dirac-Brueckner (DB) self energies and in-medium cross sections

Decomposition of DB self energy

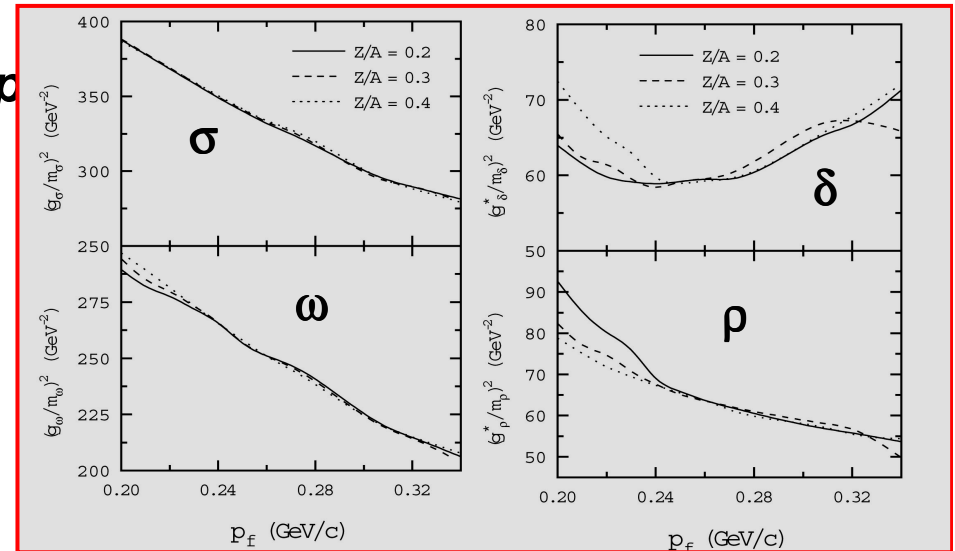
$$\Sigma_{n,p}(\mathbf{p}) = \Sigma_{n,p}^s(\mathbf{p}) - \gamma^0 \Sigma_{n,p}^0(\mathbf{p}) + \vec{\gamma} \vec{p} \Sigma_{n,p}^v(\mathbf{p})$$

Represent as density (and momentum) dependent coupling coeff.

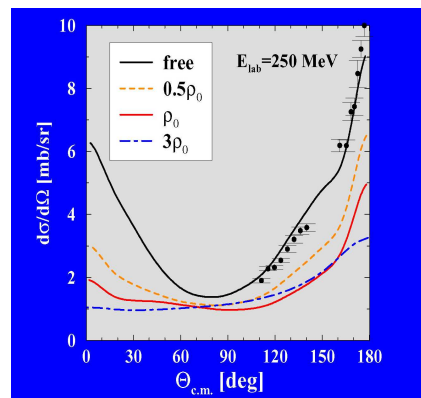
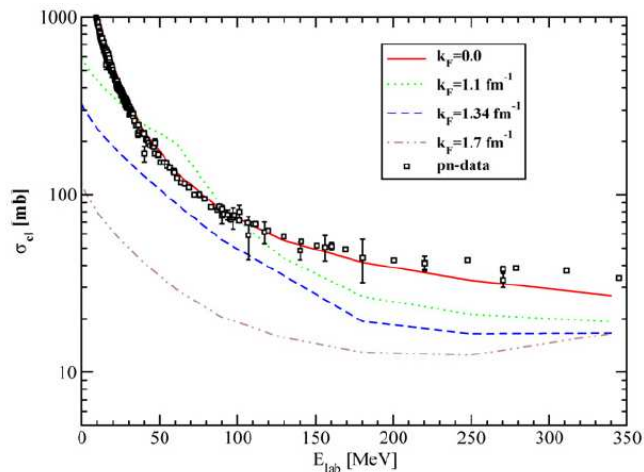
$$\Gamma_\alpha(\rho_B, \mathbf{p}) = \frac{\Sigma_\alpha(\rho_B, \mathbf{p})}{\rho_\alpha(\rho_B)}; \alpha = \{\sigma, \omega, \rho, \delta\}$$

can be used in DD-RMF approach (e.g. Typel, Wolter NPA656, 331 (1999))

deJong, Lenske, PRC 58 (98) 890

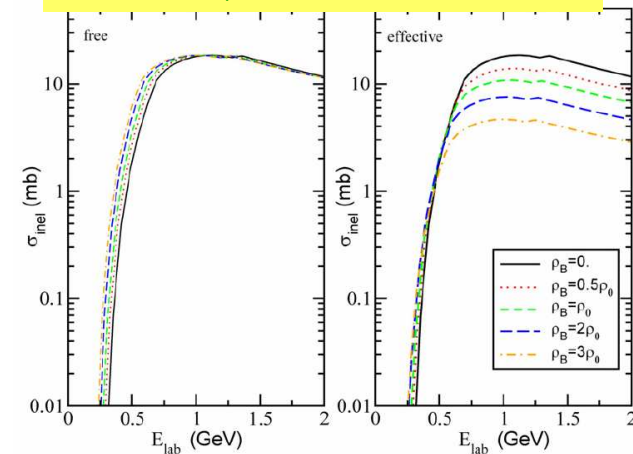


elastic np from DBHF:



[17] C. Fuchs, et al., Phys. Rev. C 64 (2001) 024003.

NN \rightarrow N Δ , from DBHF



terHaar, Malfliet, PRC 36 (87) 1611

Characterization of Codes for Transport Calculations

Realizations of transport codes:

1. Testparticle methods (BUU)

$$f(r, p; t) = \frac{1}{N_{TP}} \sum_{i=1}^{AN_{TP}} \delta(r - r_i(t)) \delta(p - p_i(t))$$

Simulate continuous phase space distribution by many test particles per nucleon ($N_{TP} = 50-200$).

- variants:
- Gaussian test particles: smoother distributions with fewer testparticles
 - include fluctuations: explicit, reduced N_{TP} , Brownian force
 - non-relativistic (Skyrme-type) or relativistic (RMF) density functionals

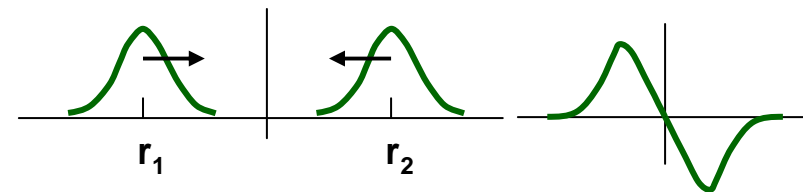
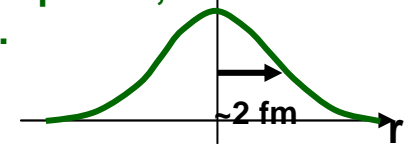
2. Quantum molecular dynamics (QMD)

Gaussian particles with large width to smooth fluctuations, but not a wave packet, since no antisymmetrization (thus similar to BUU with $N_{TP}=1$), but event generator.

variants:

- different density functionals and inclusion of isospin often denoted by different names: e.g. IQMD, ImQMD, (isospin dependence)

- antisymmetrization of wave packets included (AMD, FMD)
Particle coordinates loose meaning as WP approach each other.
reduction of wp in collision term



Fluctuations in Phase Space

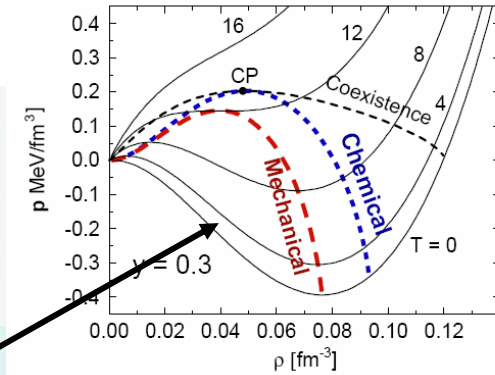
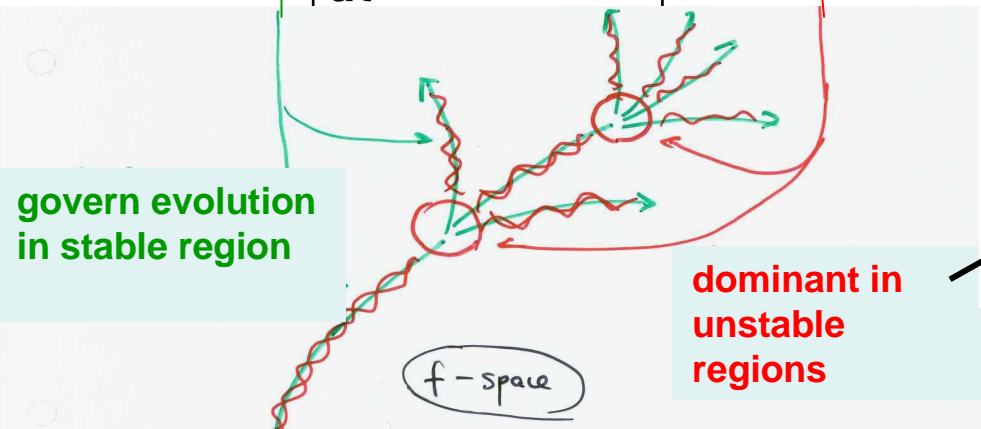
$$f(r, p, t) = \bar{f}(r, p, t) + \delta f(r, p, t)$$

Mean field evolution
(dissipative)

Fluctuations
(higher order correlations)

Boltzmann-Langevin eqn.

$$\frac{df}{dt} = I_{coll} + I_{fluc}$$



General principle: Brownian motion with friction and random force $R(t)$

$$m \frac{dv}{dt} = -\gamma v + R(t)$$

$$\Rightarrow \langle R(t)R(t') \rangle = 2\gamma T \delta(t-t')$$

Fluctuation-Dissipation theorem (Einstein relation)

→ Dissipation (collisions) and Fluctuations necessarily connected!

Origin of fluctuations: → initial state correlations (how important and realistic?)
 → higher order correlations
 → collisions (diss.-fluct. theorem)

The last two are not contained in BUU and have to be reintroduced, i.e. the Boltzmann-Langevin eq. has to be solved, at least approximatively

Fluctuations in QMD?

Classical Molecular Dynamics (CMD) has classical many body correlations:

2-body potential V_{ij} , classical eq.-of-motion, trajectories

QMD (without collisions): smeared-out classical molecular dynamics,
smearing (=width of Gaussians) much larger than size of nucleon.

mean field
$$U_i(r_i) = \sum_j \int dr_j V_{ij}(r_i - r_j) \rho_j(r_j) = \int dr_j V_{ij}(r_i - r_j) \rho(r_j)$$

same as in BUU

Thus in propagation little difference between QMD and BUU.

Difference in collision term:

QMD: collision moves **one nucleon**, large fluctuation, „event“

BUU: collision moves **one test particle** → much smaller fluctuation

(attempt to simulate this in BUU (Bertsch): move N_{TP} neighboring TPs)
→ therefore explicit fluctuation necessary (see above)

QMD: uncertainty in defining collisions.

cf. AMD, wave packet distance loses meaning, when nucleons are close
spreading of wave packet not taken into account

Expect that differences between QMD and BUU have origin in collision term

Fragment recognition algorithm in BUU:

1. „density cut“: find contours of density
 $\rho_c \sim 1/10 \rho_0$

Fragments have non-integer mass and charge numbers. Distribute to neighboring integer masses.

2. Test particle distribution sampling:

choose A out of $N_{TP} * A$ test particles with correct global properties. Treat these as nucleons and do coalescence or spanning tree algorithm (as in QMD): two particles belong to the same cluster if their distance in phase space is below a limit $r_{12} < r_0$, $p_{12} < p_0$; r_0 , p_0 parameters

Do this many times (~ 1000), and generate a distribution

→ Reconstruct many body correlations consistent with the single particle distribution

Ex.: 4 „events“ with fluctuations

458

M. Colonna et al./Nuclear Physics A 642 (1998) 449-460

$^{58}\text{Ni} + ^{58}\text{Ni}$, $E/A = 30 \text{ MeV}$, $b = 5 \text{ fm}$

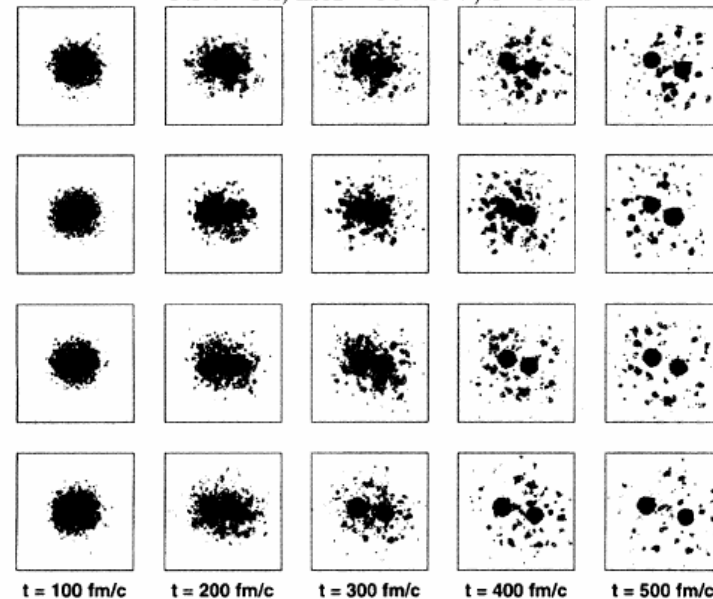
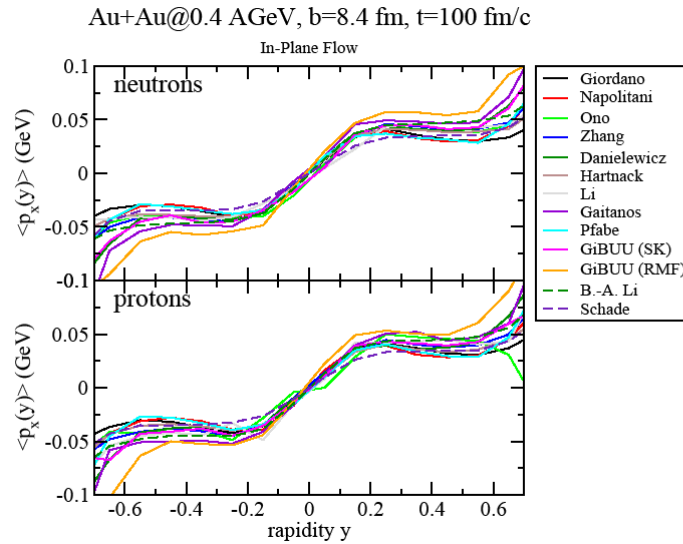


Fig. 3. Same as Fig. 1, but in the case of the binary events obtained in the collision Ni + Ni at 30 MeV/A, $b = 5 \text{ fm}$.

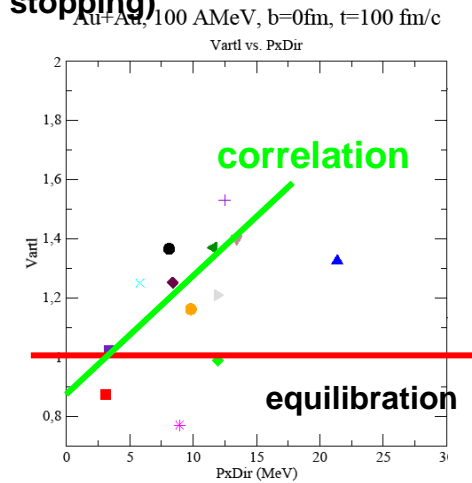
Code Comparison Project: Workshop on Simulations of Heavy Ion Collisions at Low and Intermediate Energies, ECT*, Trento, May 11-15, 2009

- using same reaction and physical input (not necessarily very realistic, no symm energy))
- include major transport codes
- obtain estimate of „systematic errors“

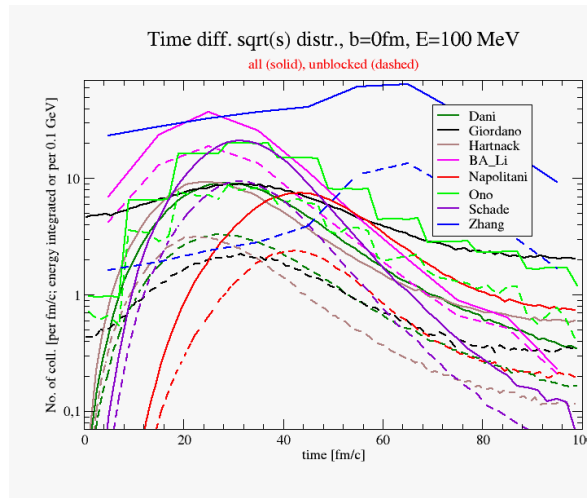
transverse
flow



Correlation between transv flow
and Vartl (ratio of long and transv
stopping)



time
distribution of
collisions
(energy
integrated)



→ agreement for flow and other one-body observables reasonable, but perhaps not really good enough to make detailed conclusions

→ symmetry effects are order of magnitude smaller: hope that differences are less sensitive (?)

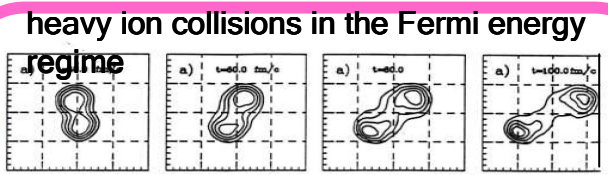
→ **origin of differences: collisions ?**

The Symmetry Energy in Various Density Regimes

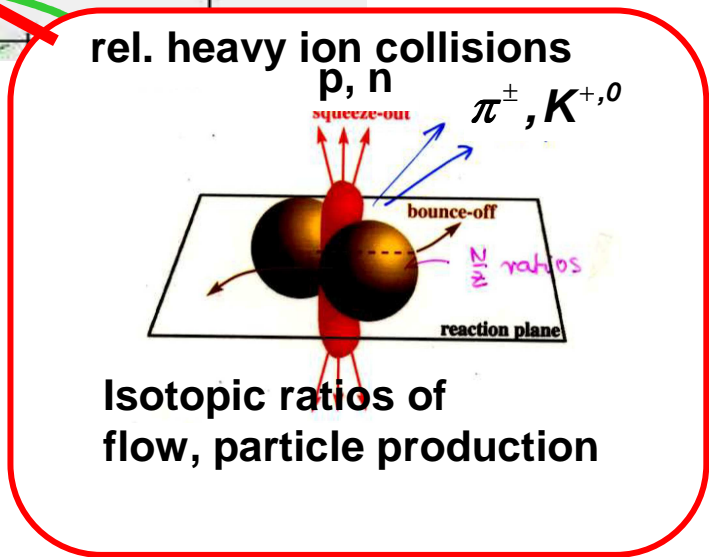
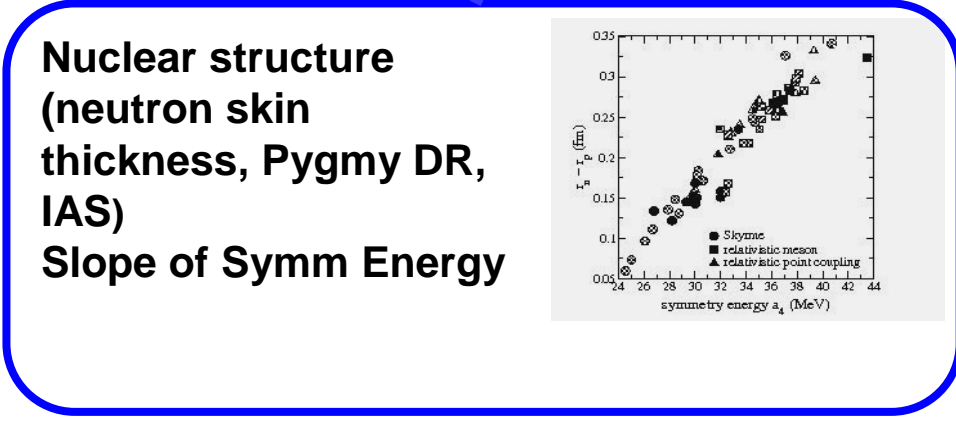
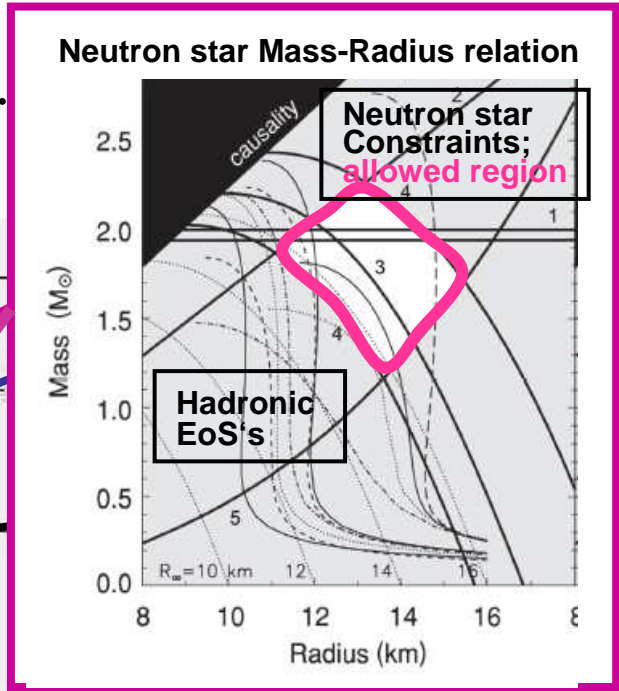
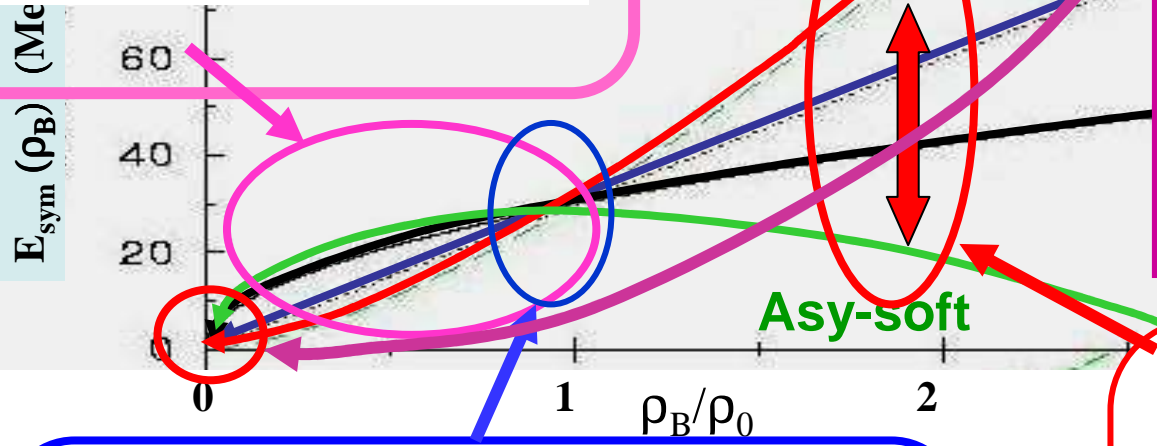
Investigations on the Nuclear Symmetry Energy

$$E(\rho_B, I) / A = E(\rho_B) + E_{sym}(\rho_B) I^2 + O(I^4) + \dots$$

$$I = \frac{N - Z}{N + Z}$$



Isospin Transport properties, (Multi-)Fragmentation

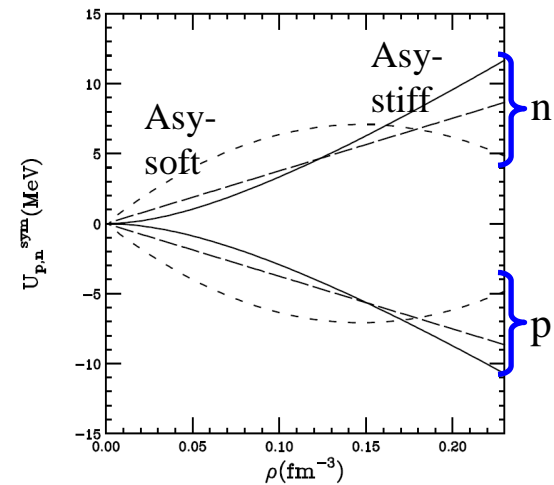


Strategies for the determination of the SE in HIC

Potential energy in nuclear matter:

$$E/A \sim -16 \text{ MeV} = T(3/5 \varepsilon_F \sim 21 \text{ MeV}) + U \rightarrow U \sim -37 \text{ MeV}$$

$U_{\text{sym}} \sim 8 \text{ MeV} \rightarrow$ small effect



Thus use **differences or ratios** of isospin dependent observables, to eliminate As much as possible uncertainties in the isoscalar sector.
Of course, no guarantee. Establish that global description of reaction is correct.

I arrived at this point during the lecture.

**The remaining slides will perhaps be discussed
in an afternoon session**

The Symmetry Energy at very low densities

A statistical analysis to determine Symmetry Energy at very low densities

S. Kowalski, J. Natowitz, et al., PRC75 014601 (2007)

$^{64}\text{Zn} + (^{92}\text{Mo}, ^{197}\text{Au})$ at 35 A MeV

Central collisions, reconstruction of fireball

Determination of thermodyn. conditions as fct of $v_{\text{surf}} = v_{\text{emission}} - v_{\text{coul}}$

~time of emission with specified conditions of density and temperature:

→ temperature: isotope temperatures, double ratios H-He

$$T_{\text{HHe}} = \frac{14.3}{\ln[\sqrt{(9/8)}(1.59 R_{V_{\text{surf}}})]},$$

→ densities ρ_p, ρ_n , from yield ratios and bound clusters

$$\rho_p = 0.62 \times 10^{36} T^{3/2} e^{-19.8/T} Y(^4\text{He}) / Y(^3\text{H}).$$

→ Isoscaling analysis

(B. Tsang, et al.,)

$$R_{12} = \frac{Y_2(N, Z)}{Y_1(N, Z)} \cong \left(e^{\frac{\Delta\mu_n}{T}} \right)^N \left(e^{\frac{\Delta\mu_n}{T}} \right)^Z \cong e^{\alpha N + \beta Z}$$

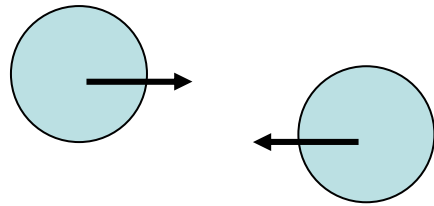
Isoscaling coefficients α and β

→ Symmetry free energy

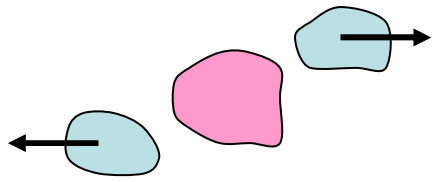
$$\alpha = \frac{4F_{\text{sym}}}{T} \left(\left(\frac{Z_1}{A_1} \right)^2 - \left(\frac{Z_2}{A_2} \right)^2 \right)$$

$$E_{\text{sym}} = F_{\text{sym}} + T S^{(\text{NSE})}$$

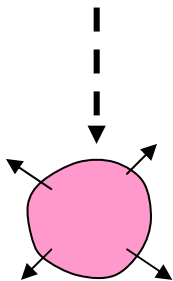
Scheme of Kowalski Interpretation



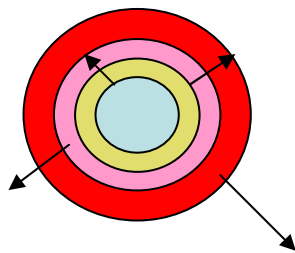
**$64\text{Zn}+(92\text{Mo},197\text{Au})$ at 35 AMeV,
i.e. two systems for isoscaling analysis**



3-source fit and complete reconstruction of participant, i.e. N,Z of source

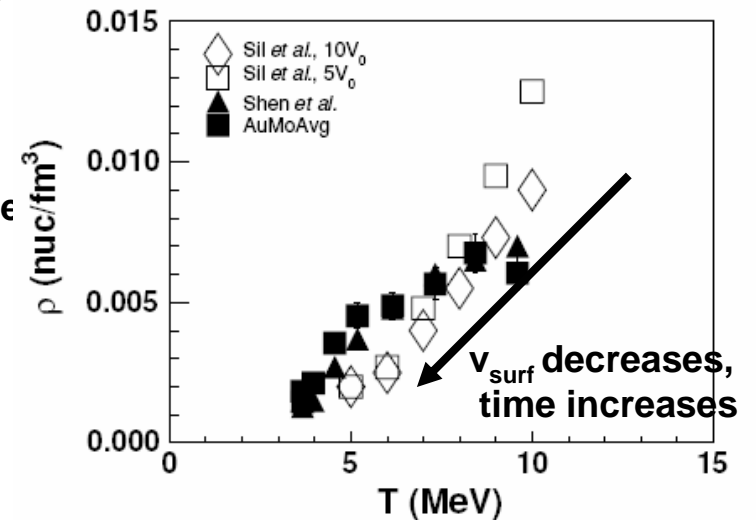


**Participant emits light clusters (p,n,d,t, 3He , α) and cools
Earlier emitted particles have higher temperature and higher initial velocity $=v_{\text{surf}}$, which is measured**

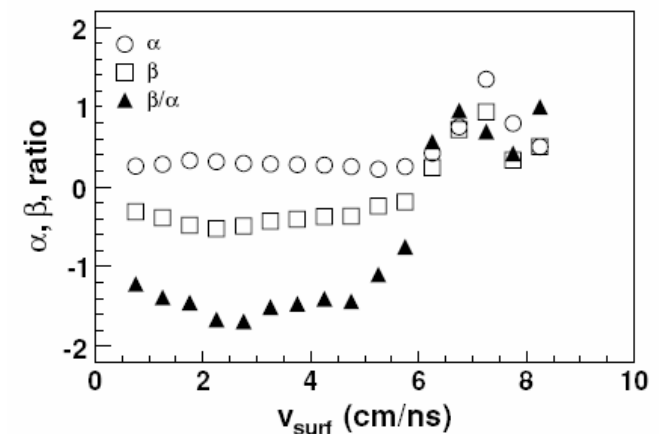


**Interpret results by thermodynamics as a function of v_{surf} ,
i.e. each shell is a piece of equilibrated dilute matter, of which T, ρ are determined**

Extracted ρ -T relation for emitting source

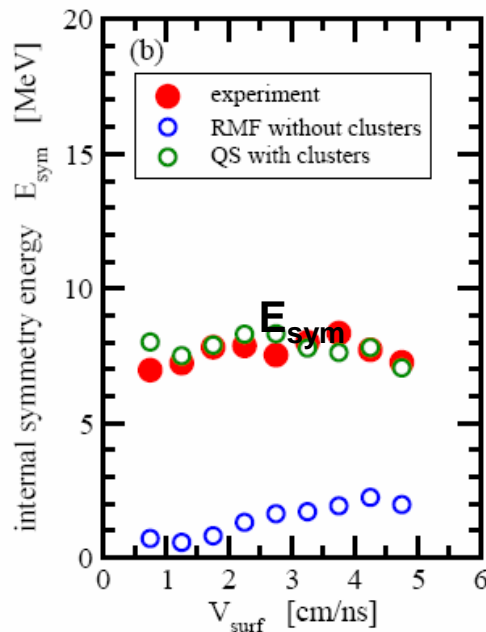


Isoscaling coefficients

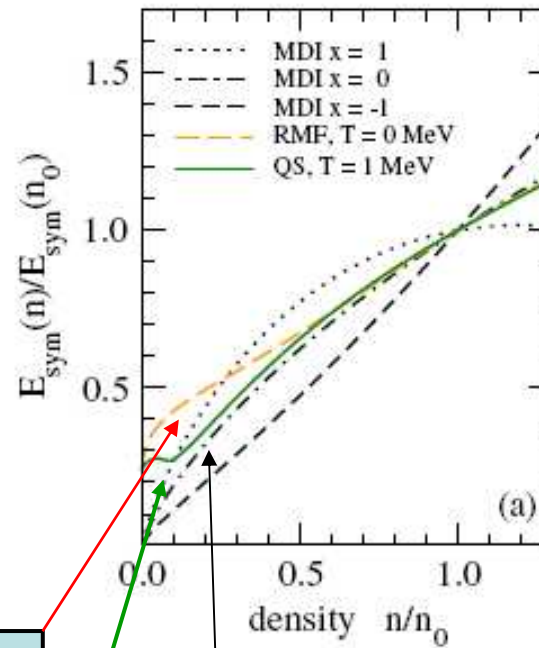


Comparison of low-density symmetry energy to experiment:

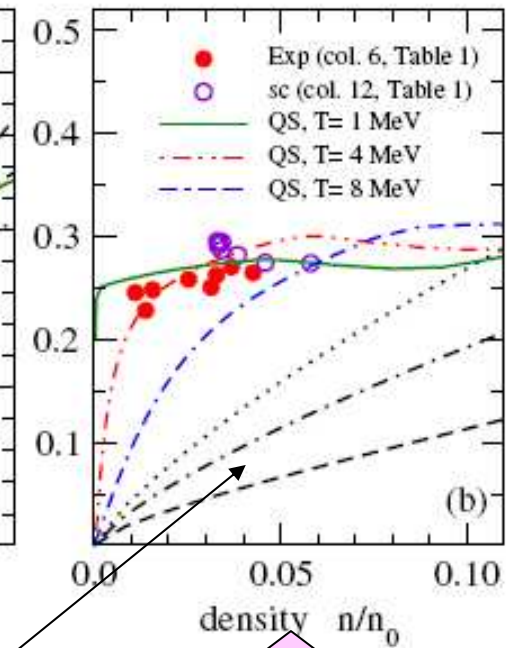
J. Natowitz, G. Röpke, S. Typel, ... HHW, PRL 104, 202501 (2010)



complete density range



low densities



Single nucleus approx.
(Wigner-Seitz), RMF

Quantum Statistical
model, $T=1$ MeV)

Parametrization of nuclear symmetry
energy of different stiffness (B.A. Li)

Successfully reproduce
the experimentally
deduced symmetry
energy at low density.

Symmetry energy is
finite at very low
density!

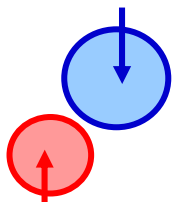
The Symmetry Energy at Low Densities

Dynamical Interpretations of Low Energy Heavy Ion Collisions

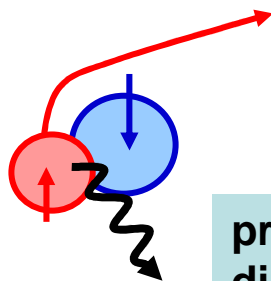
Coulomb barrier to Fermi energies

peripheral

Isospin migration

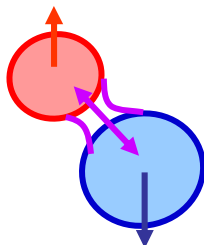


deep-inelastic

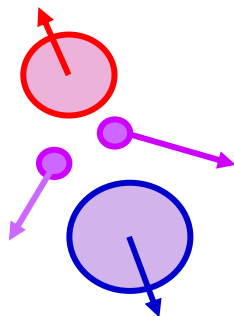


pre-equil. dipole

N/Z of PLF residue = isospin diffusion

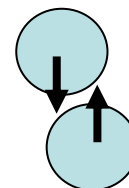


N/Z of neck fragment and velocity correlations

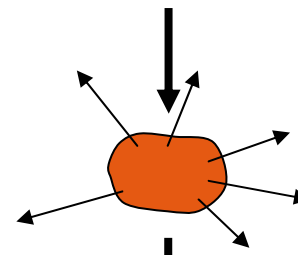


central

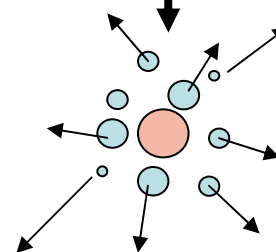
Isospin fractionation, multifragm



pre-equil. light particles



N/Z ratio of IMF's



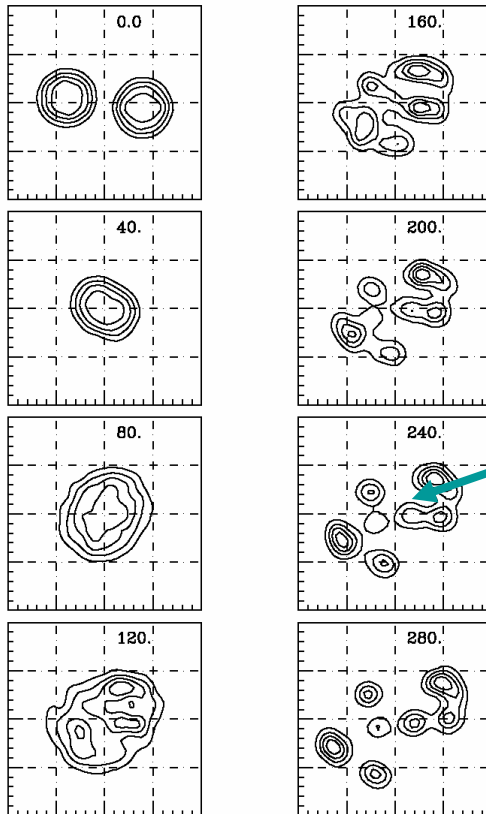
Isospin dynamics at Fermi energies

V. Baran et al.,
NPA703(2002)603
NPA730(2004)329

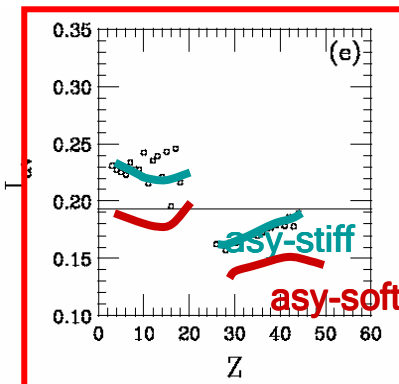
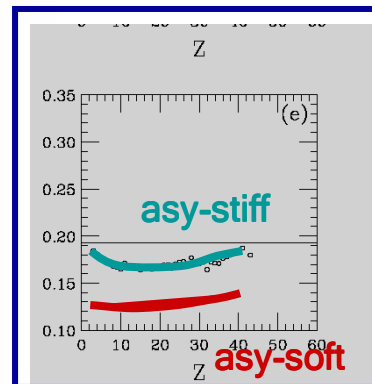
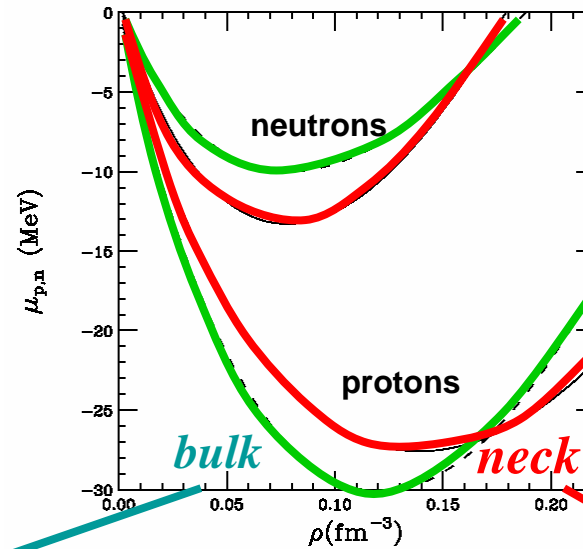
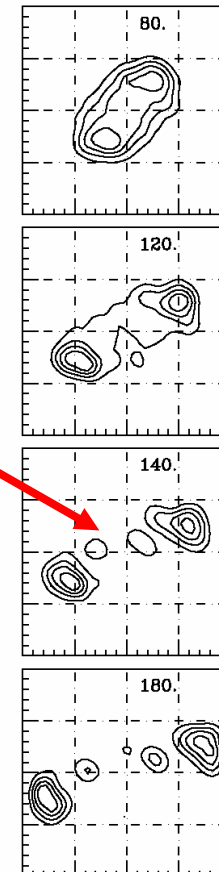
$^{124}\text{Sn} + ^{124}\text{Sn}$, 50 A MeV

Chemical potential: **isostiff**, **isostiff**

Central collision, $b=2$ fm



Peripheral collision, $b=6$ fm

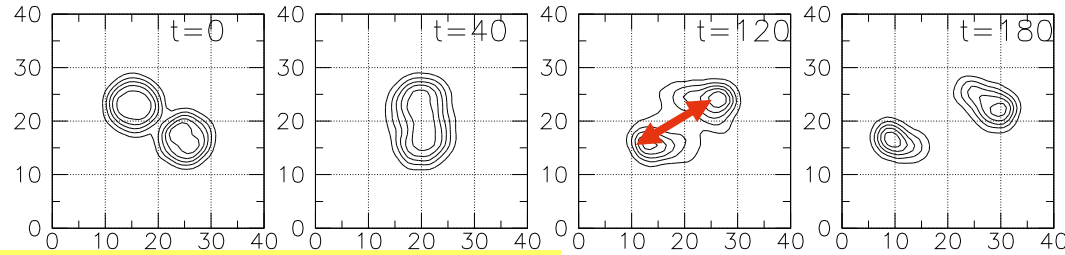
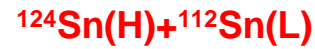


Multifragmentation: Isospin fractionation at low densities

Neck-fragmentation: Isospin migration at interface with normal density

Isopin diffusion

isospin transport through „neck“ in peripheral collisions



Imbalance (or Rami, transport) ratio:

β asymmetry of residue (i=PLF,TLF)
(also for other isospin sens.quantities)

$$R_i = \frac{\beta_i^{mix} - \frac{1}{2}(\beta_i^{HH} + \beta_i^{LL})}{\frac{1}{2}(\beta_i^{HH} - \beta_i^{LL})}$$

Limiting values:

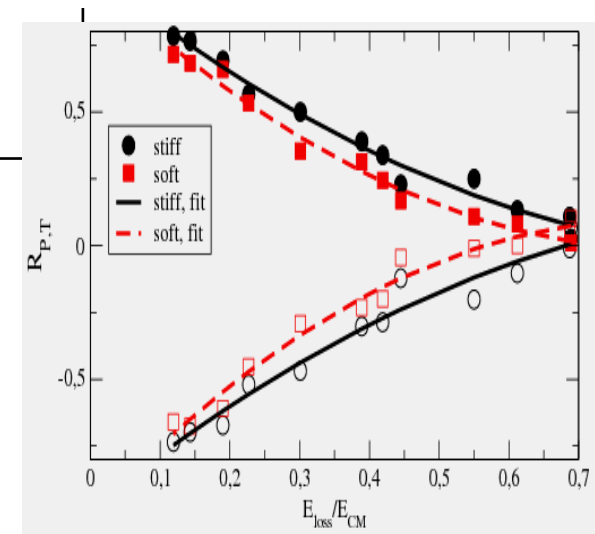
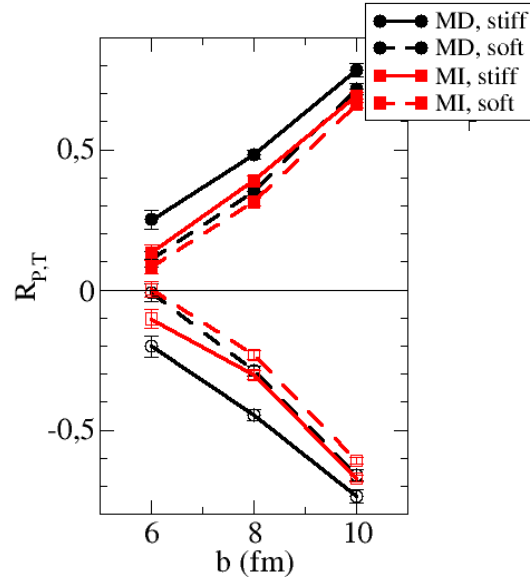
$R=0$ complete equilibration
 $R=-1$, complete transparency

Simple equil. model

$$\beta_{P,T}^M = \beta^{eq} + (\beta^{H,L} - \beta^{eq}) e^{-t/\tau}$$

$$\Rightarrow R_{P,T} = \pm e^{-t/\tau}$$

Ratio det. by interact. and relax. times

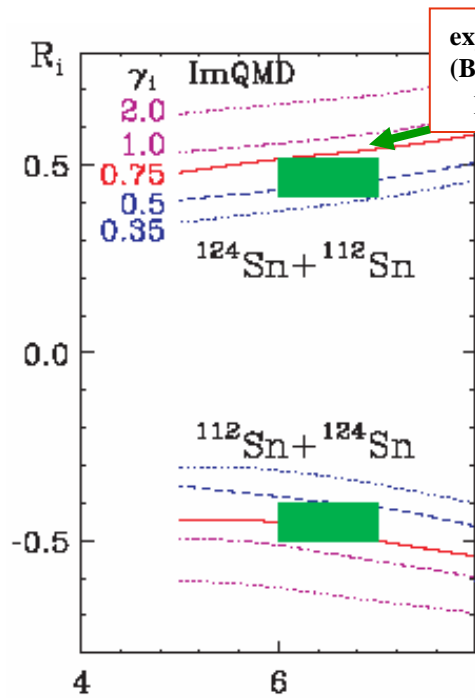


J.Rizzo, et al., Nucl. Phys. A806 (2008) 79

more equilibration (lower R) for longer interaction time ~ correlation with total energy loss

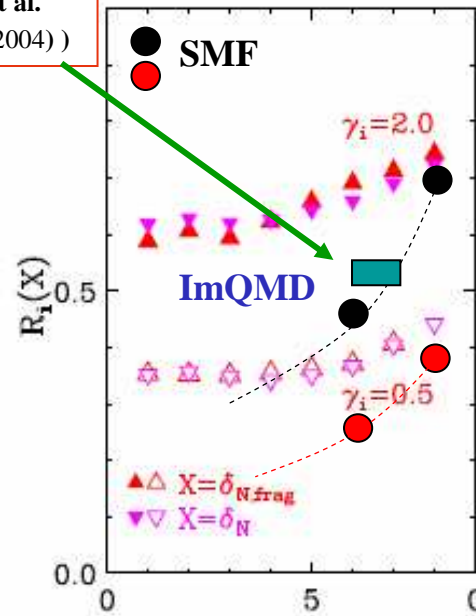
Transport Ratios for Projectile/Target Residues: $^{112,124}\text{Sn} + ^{112,124}\text{Sn}$, 50 MeV

Comparison to other calculation:

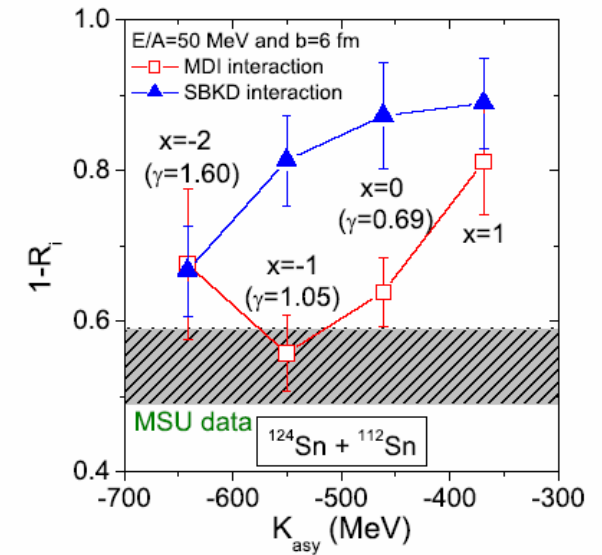


M.B. Tsang, et al., PRL 102 (2008)

experimental data
(B. Tsang et al.
PRL 92 (2004))



J.Rizzo, et al., NPA806 (08) 79

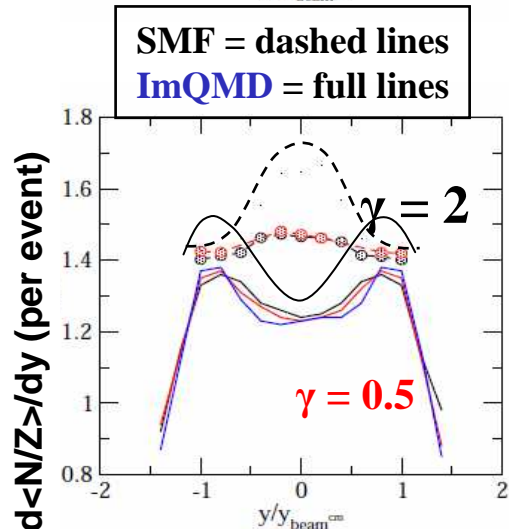
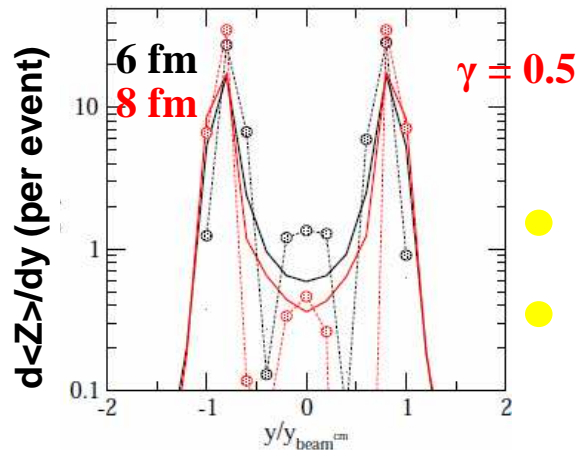


L.W.Chen, C.M.Ko, B.A.Li, PRL 94, 032701 (2005)

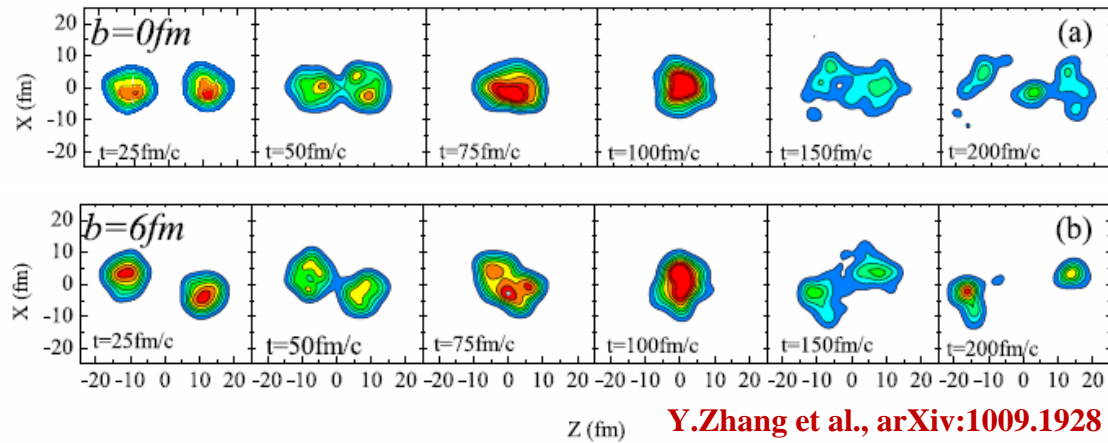
1. Qualitative agreement, but not quantitative
2. different impact parameter dependence
3. perhaps related to different procedures to solve transport eq. (BUU vs. QMD)

Analysis of differences BNV – QMD

→ more 'explosive' dynamics:
more 'transparency'



ImQMD calculations, $^{112}\text{Sn} + ^{112}\text{Sn}$, 50 A MeV

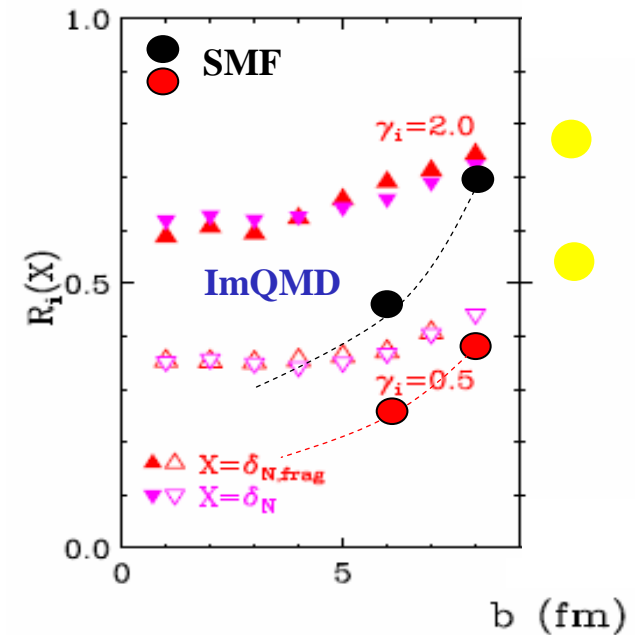


Y.Zhang et al., arXiv:1009.1928

Much less isospin migration in ImQMD,
Other sources of dissipation: Fragment emission, fluctuation?

→ Less dependence on impact parameter.

Similar conclusions in comparison with Antisymmetrized Mol. Dynamics (AMD): Colonna, Ono, Rizzo, PRC (2011)



Influence on imbalance ratio!

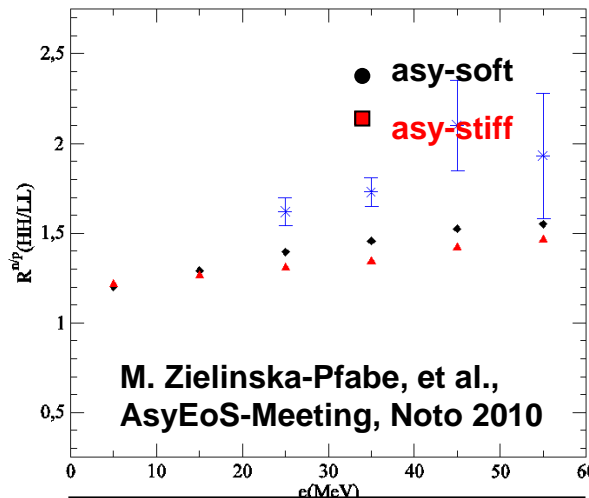
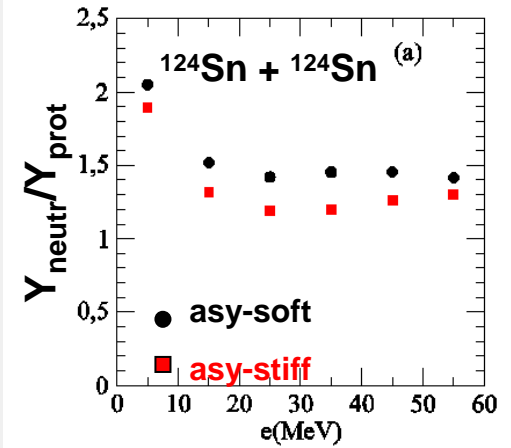
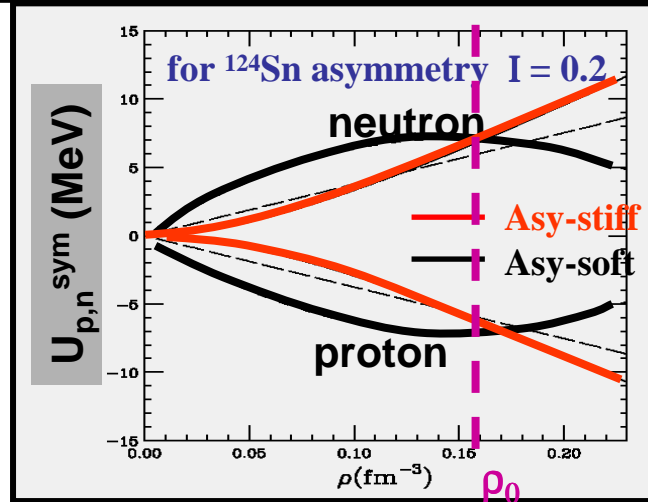
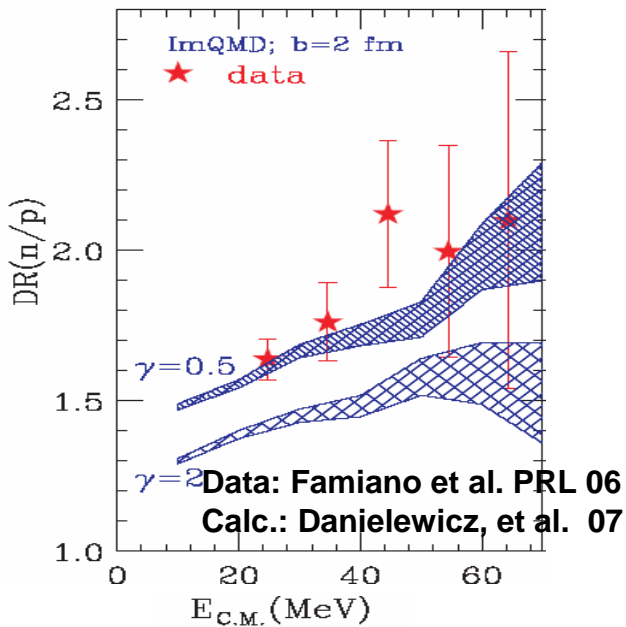
Pre-equilibrium particle emission: n/p ratio

Early emitted neutrons and protons reflect difference in potentials in expanded source, esp. ratio $Y(n)/Y(p)$.

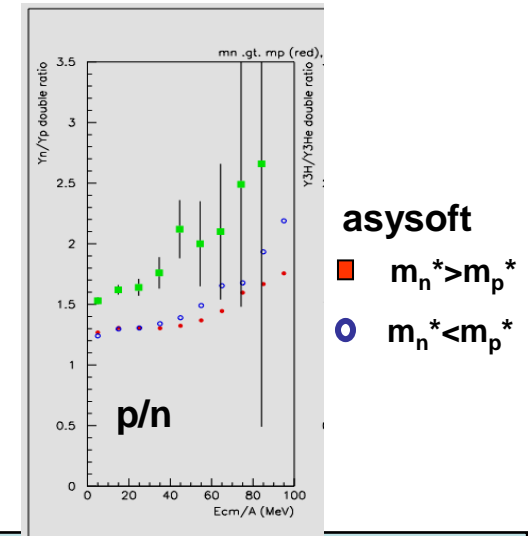
more emission for asy-soft, since symm potential higher

„Double Ratios“

$$\frac{^{124}\text{Sn} + ^{124}\text{Sn}}{^{112}\text{Sn} + ^{112}\text{Sn}}$$



Similar qualitatively but smaller effect

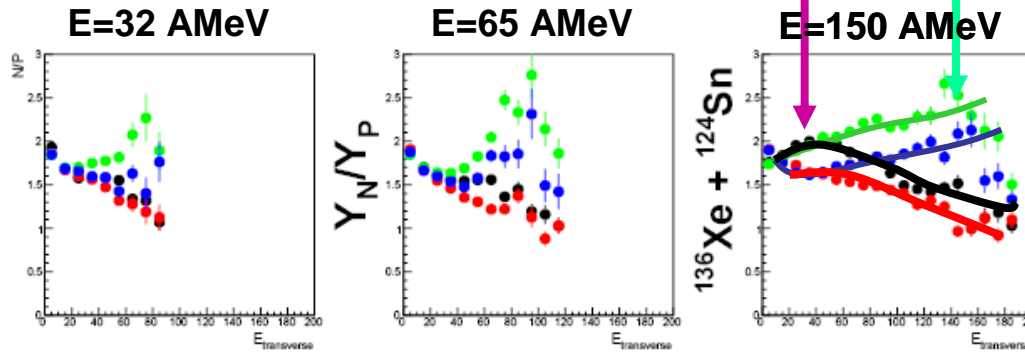


Effect of mass splitting of same magnitude

→ A promising observable, but theoretical discrepancies → systematic study useful

**Study of Light Fragment Emission: $^{136,124}\text{Xe} + ^{124,112}\text{Sn}$, $E = 32, 65, 150$ A MeV ,
Single yield ratios**

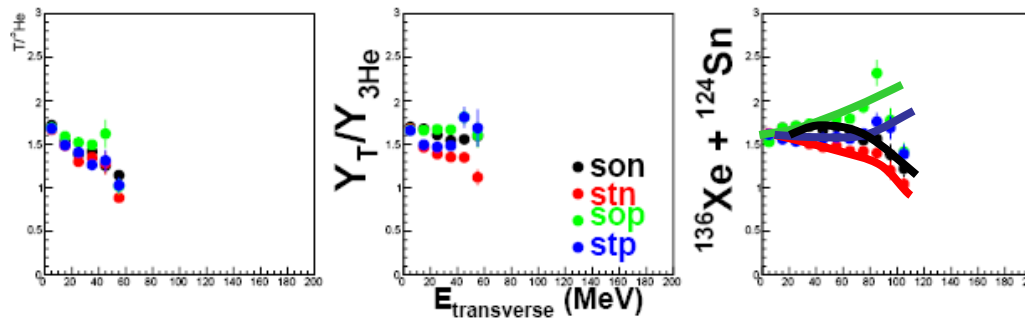
Single ratio n/p
neutron rich



AsyEOS – eff mass dominates

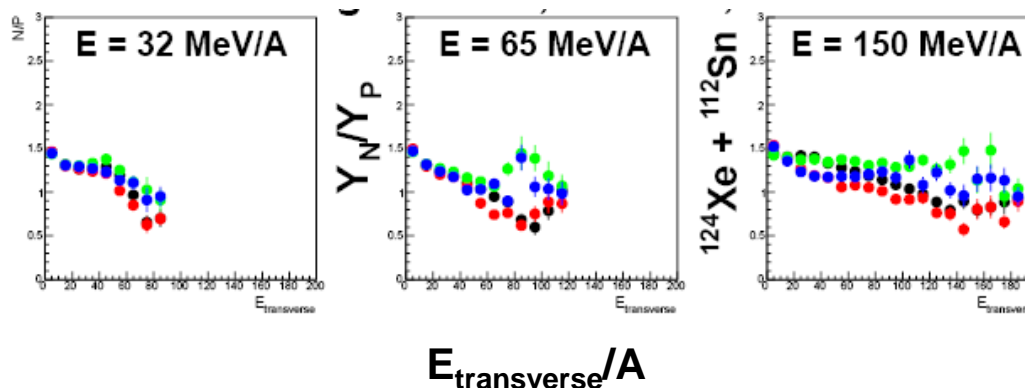
Possibility to separate density and momentum dependence of symmetry energy

Single ratio $t/3\text{He}$
neutron rich



Effects smaller
For light clusters t/He

Single ratio n/p
neutron poor

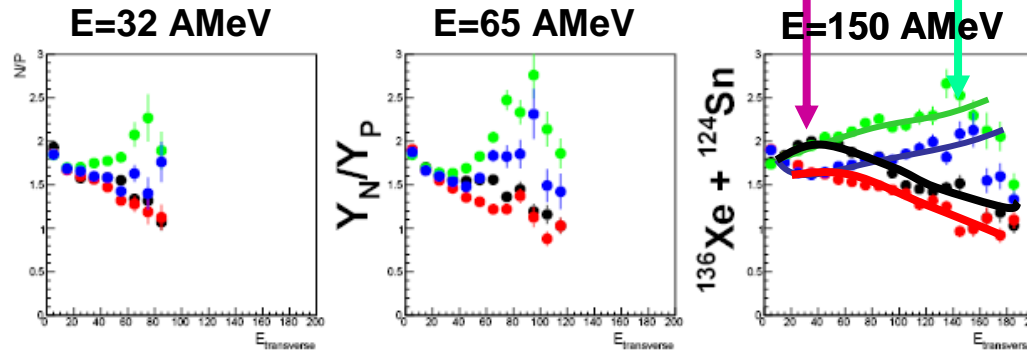


Smaller neutron excess: effects smaller

son: asysoft, $m_n^* > m_p^*$
 stn: asystiff, $m_n^* > m_p^*$
 sop: asysoft, $m_n^* < m_p^*$
 stp: asystiff, $m_n^* < m_p^*$

Study of Light Fragment Emission: $^{136,124}\text{Xe} + ^{124,112}\text{Sn}$, $E = 32, 65, 150$ A MeV , Single yield ratios

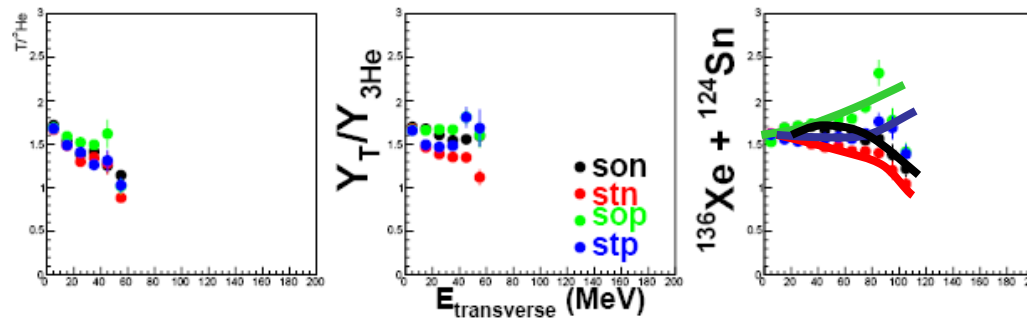
Single ratio n/p
neutron rich



AsyEOS – eff mass dominates

Possibility to separate density and momentum dependence of symmetry energy

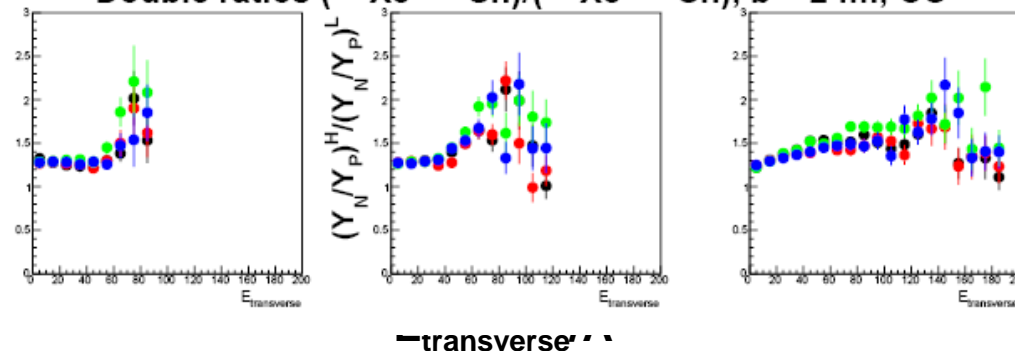
Single ratio $t/3\text{He}$
neutron rich



Effects smaller
For light clusters t/He

Double ratio n/p
neutron rich
neutron poor

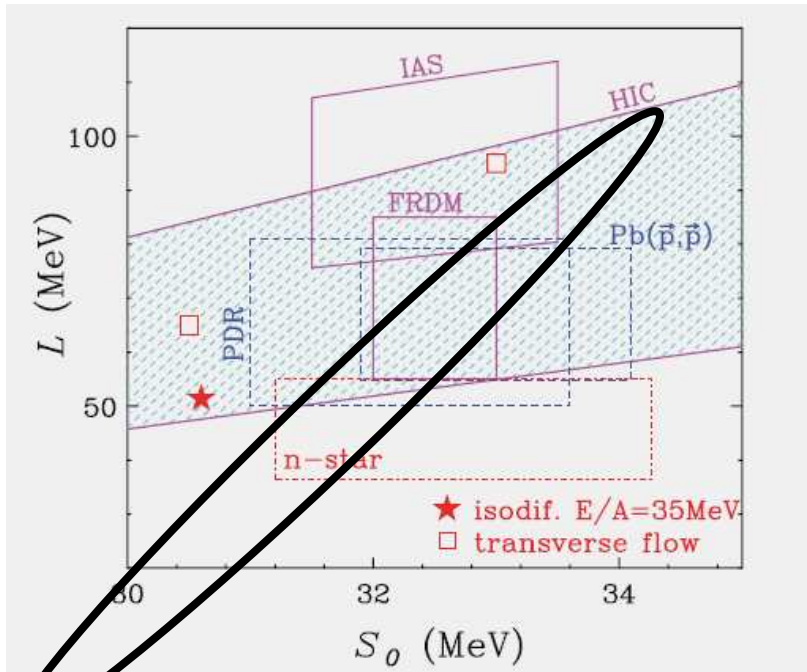
Double ratios $(^{136}\text{Xe} + ^{124}\text{Sn}) / (^{124}\text{Xe} + ^{112}\text{Sn})$, $b = 2$ fm, CO



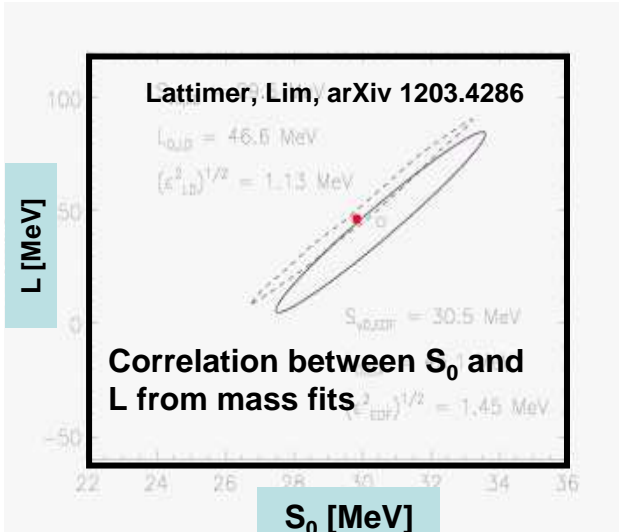
Double ratio also shows effect but less sensitive to symmetry energy

son: asysoft, $m_n^* > m_p^*$
stn: asystiff, $m_n^* > m_p^*$
sop: asysoft, $m_n^* < m_p^*$
stp: asystiff, $m_n^* < m_p^*$

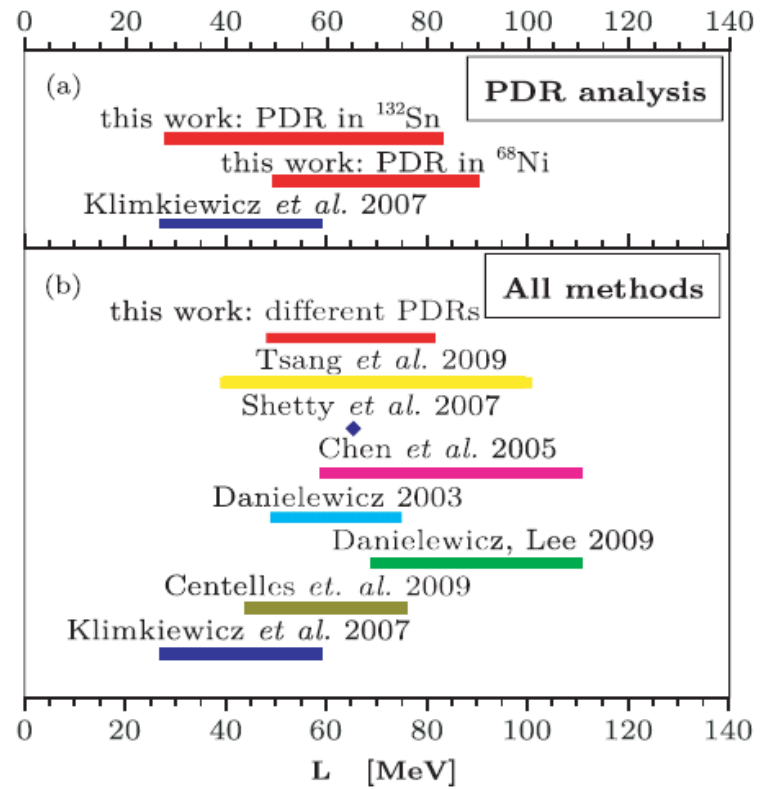
Constraints of SE for $\rho \leq \rho_0$ from Fermi energy collisions



M.B.Tsang, et al., PRC86,015803(2012)



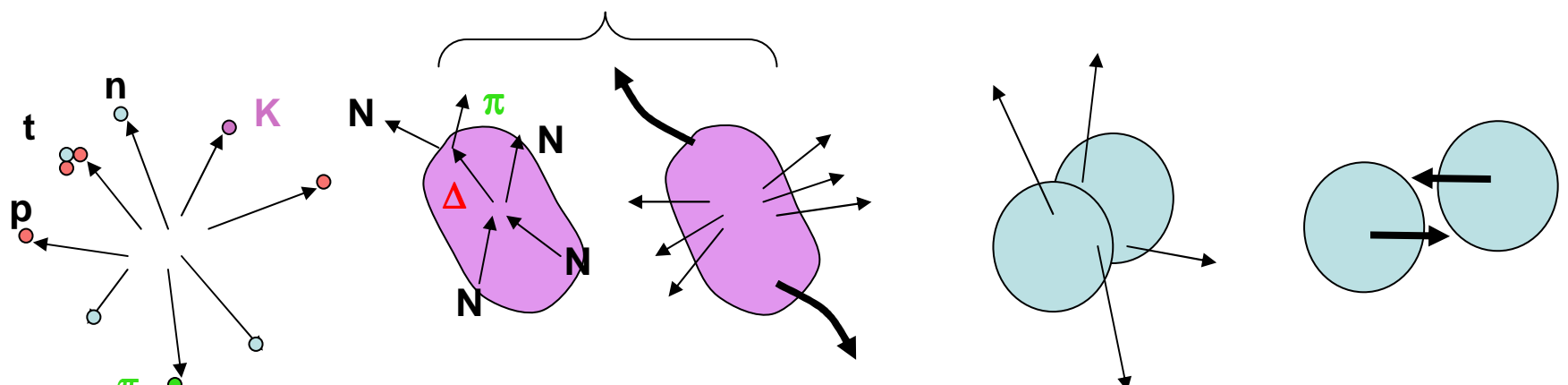
Determinations of L from structure and reactions



A. Carbone, et al., PRC81, 043101 (2010)

The Symmetry Energy at Supra-Saturation Densities

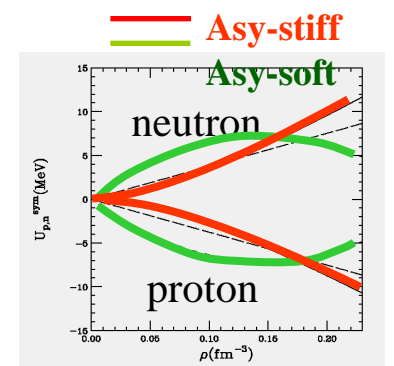
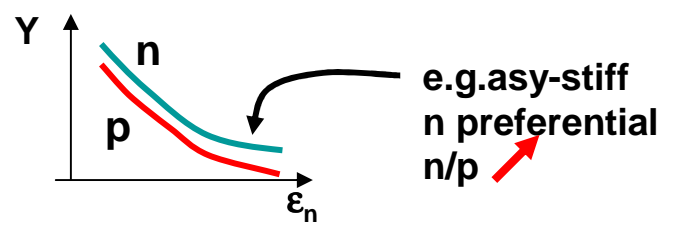
Sketch of reaction mechanism at intermediate energies and observables



disintegration
 Inel. collisions
 Particle product.
 $NN \rightarrow N \Delta \rightarrow N \Delta K$
 $N \pi$
 Flow,
 In-plane, transverse
 Squeeze-out, elliptic
 Pre-equilibr emiss.
 (first chance,
 high momenta)

Yield and spectra of light part.

residual source more symm. n/p

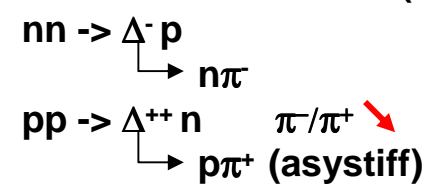


flow

Differential p/n flow (or t/3He)

diff # p,n (asymmetry of system)

Pion production

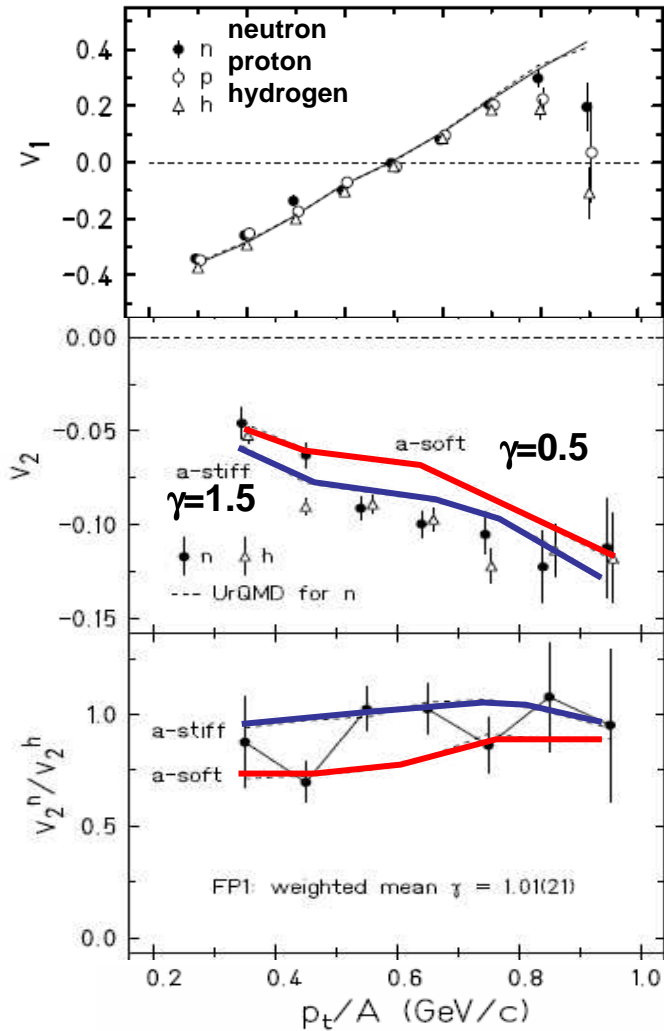


diff. force on n,p

Reaction mechanism can be tested with several observables: Consistency required!

First measurement of isospin flow

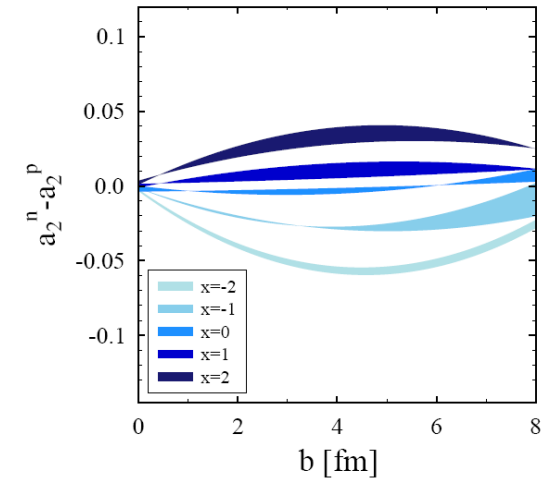
Au+Au @ 400 AMeV, FOPI-LAND (Russotto, et al., PLB 697, 471 (11))



directed flow (v_1) not very sensitive,

but elliptic flow (v_2), originates in compressed zone

determines a rather stiff symmetry energy ($\gamma \sim 1$)



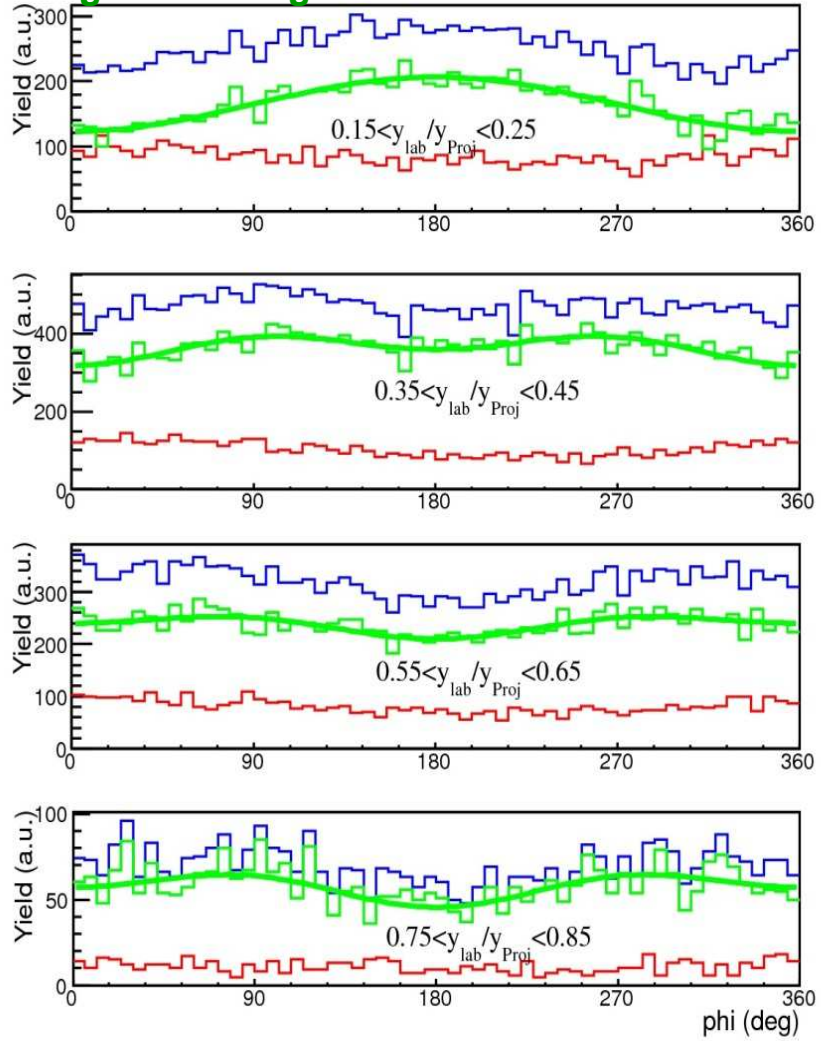
Each band: soft vs. stiff eos of **symmetric** matter, (Cozma, arXiv 1102.2728) \rightarrow robust probe

ASYEOS experiment at GSI
May 2011, being analyzed

ASYEOS Experiment

preliminary

Azimuthal distributions,
green: background subtracted

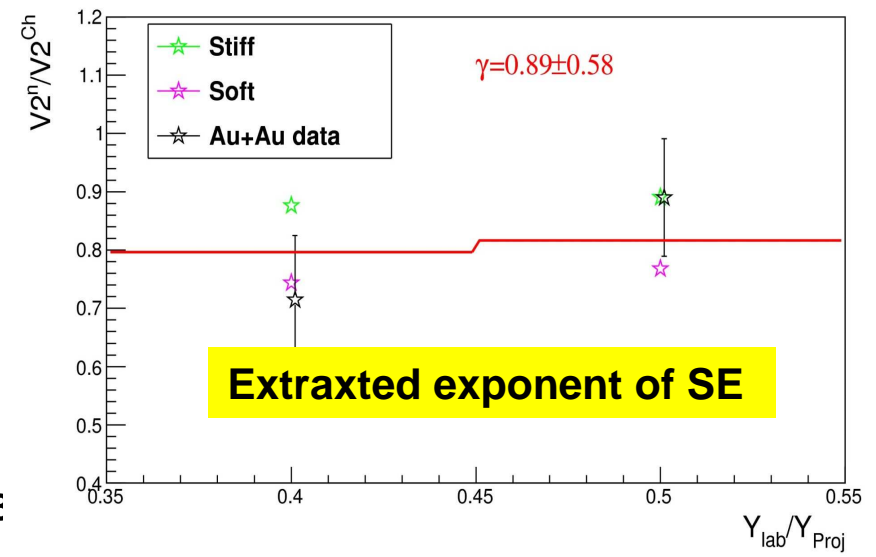
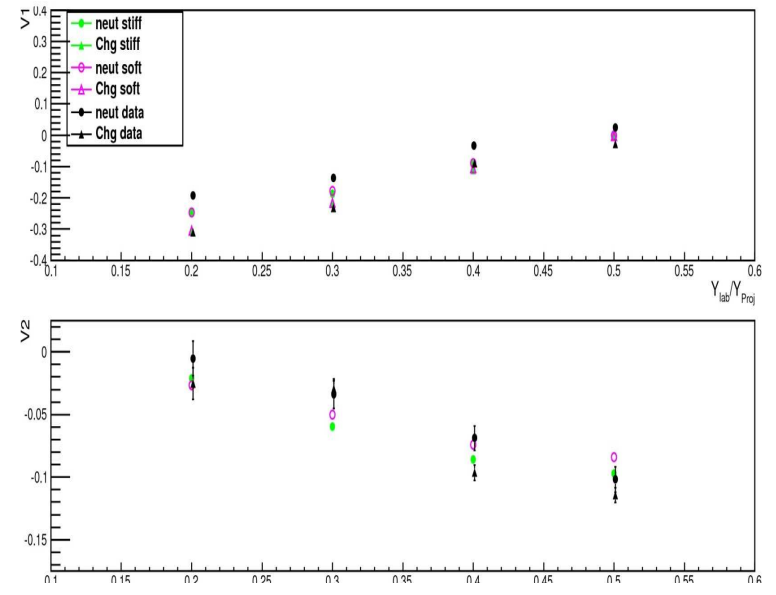


P. Russoto, Thexo Meeting, ECT, Trento, 8.-12.7.13

Au+Au @ 400 AMeV

b < 7.5 fm

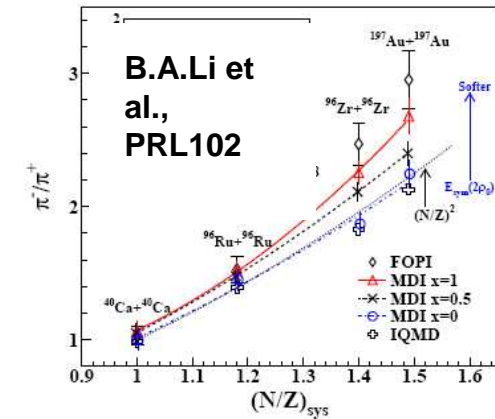
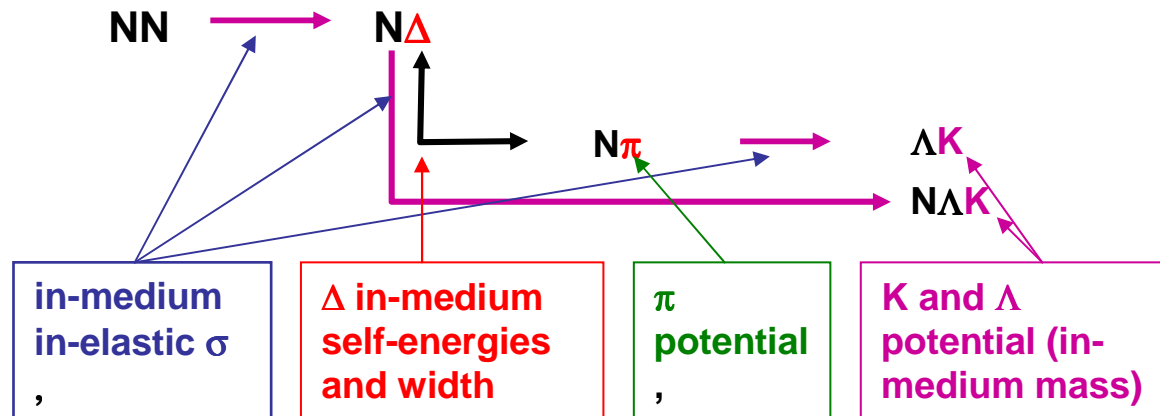
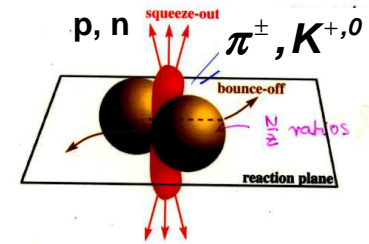
Elliptic flow coefficients (neutrons and Z=1)



Particle production as probe of symmetry energy

Difference in neutron and proton potentials

1. „direct effects“: difference in proton and neutron (or light cluster) emission and momentum distribution
2. „secondary effects“: production of particles, isospin partners π^+, π^-, K^0, K^+



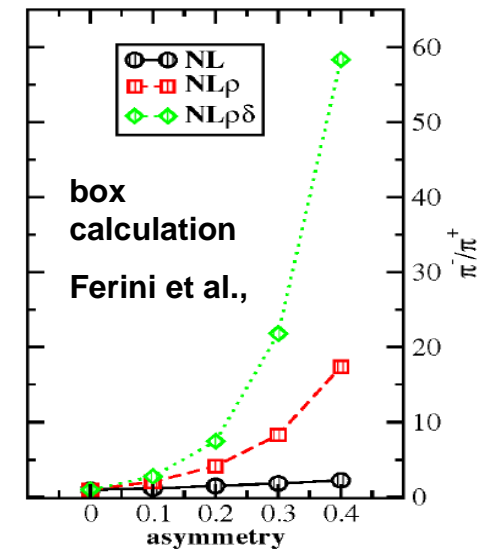
Two limits:

1. isobar model
(yield determined by CG-Coeff of $\Delta \rightarrow N\pi$)

$$\pi^- / \pi^+ = \frac{5N^2 + NZ}{5Z^2 + NZ} \approx \left(\frac{N}{Z}\right)^2$$

2. chemical equilibrium $\pi^- / \pi^+ \propto \exp\left(\frac{2(\mu_n - \mu_p)}{T}\right) = \exp\left(\frac{8\delta E_{sym}(\rho)}{T}\right)$

-> π^-/π^+ should be a good probe!



Particle production as probe of symmetry energy

Two effects:

1. Mean field effect: U_{sym} more repulsive for neutrons, and more for asystiff
 → pre-equilibrium emission of neutron, reduction of asymmetry of residue

$$\frac{n}{p} \downarrow \Rightarrow \frac{Y(\Delta^{0,-})}{Y(\Delta^{+,++})} \downarrow \Rightarrow \frac{\pi^-}{\pi^+} \downarrow$$

decrease with asy – stiffness

2. Threshold effect, in medium effective masses:

Canonical momenta have to be conserved. To convert to kinetic momenta, the self energies enter

$$I_{\text{coll}} = \int d\vec{v}_2 d\vec{v}_1 d\vec{v}_2' v_{12} \sigma_{\text{inel}}(\Omega) (2\pi)^3 \delta(\mathbf{p}_1 + \mathbf{p}_2 - \mathbf{p}_1' - \mathbf{p}_2')$$

$$\times [f_1' f_2' (1 - f_1)(1 - f_2) - f_1 f_2 (1 - f_1')(1 - f_2')]$$

In inelastic collisions, like $nn \rightarrow p\Delta^-$, the selfenergies may change. Simple assumption about self energies of Δ .

$$\begin{aligned} \Sigma_i(\Delta^-) &= \Sigma_i(n), \\ \Sigma_i(\Delta^0) &= \frac{2}{3} \Sigma_i(n) + \frac{1}{3} \Sigma_i(p), \\ \Sigma_i(\Delta^+) &= \frac{1}{3} \Sigma_i(n) + \frac{2}{3} \Sigma_i(p), \\ \Sigma_i(\Delta^{++}) &= \Sigma_i(p), \end{aligned}$$

Yield of pions depends on

$$\sigma = \sigma_{\text{inel}} (\mathbf{s}_{\text{in}} - \mathbf{s}_{\text{th}})$$

Detailed analysis gives

$$\frac{\pi^-}{\pi^+} \uparrow \text{increase with asy – stiffness}$$

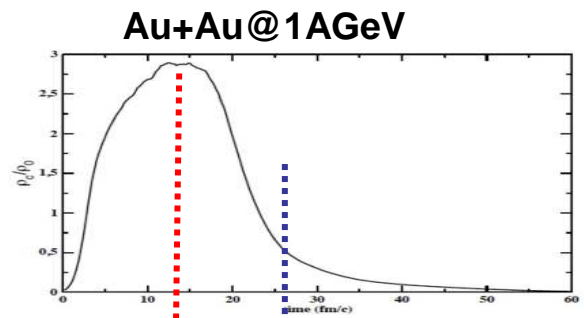
Competing effects!

Not clear, whether taken into account in all works.

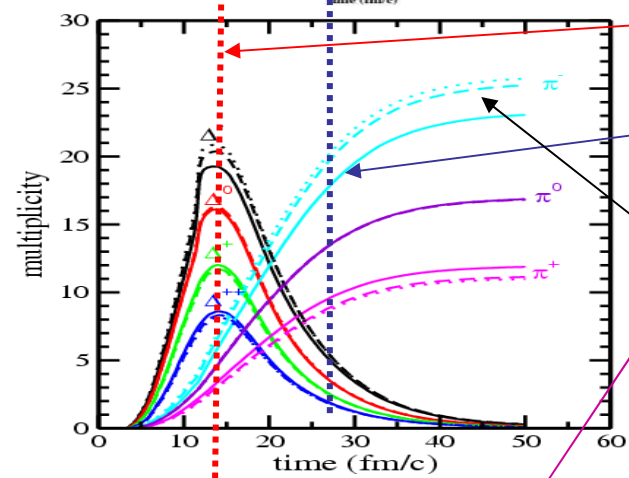
Assumptions may also be too simple.

Dynamics of particle production (Δ, π, K) in heavy ion collisions

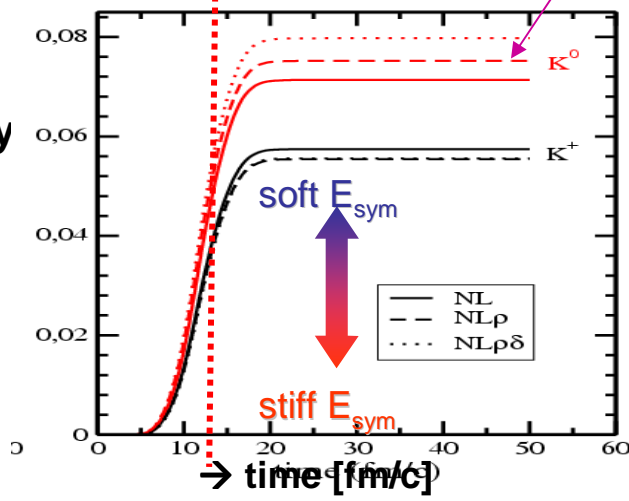
Central density



π and Δ multiplicity



$K^{0,+}$ multiplicity



Δ and K:
production
in high density
phase

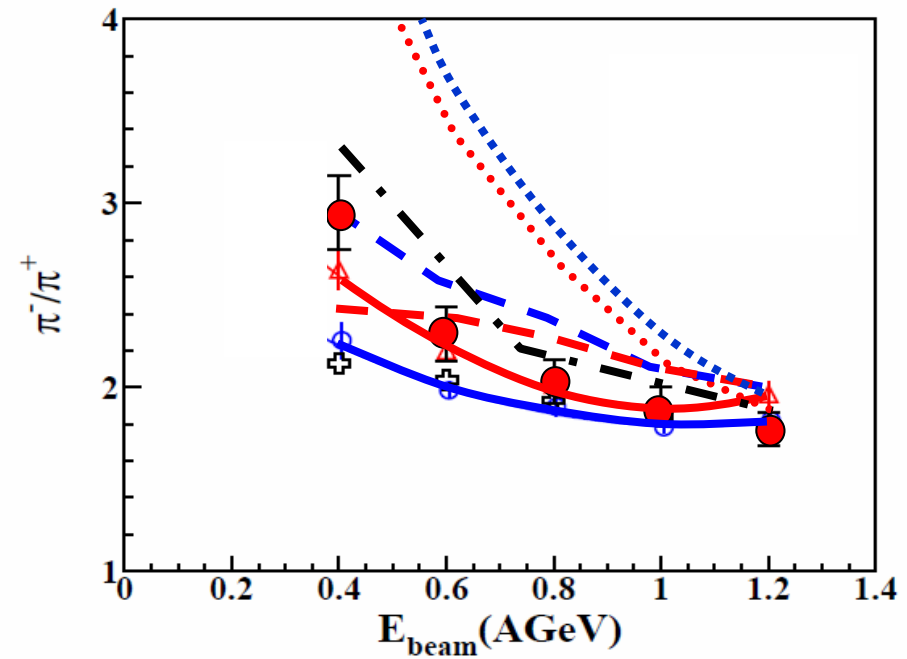
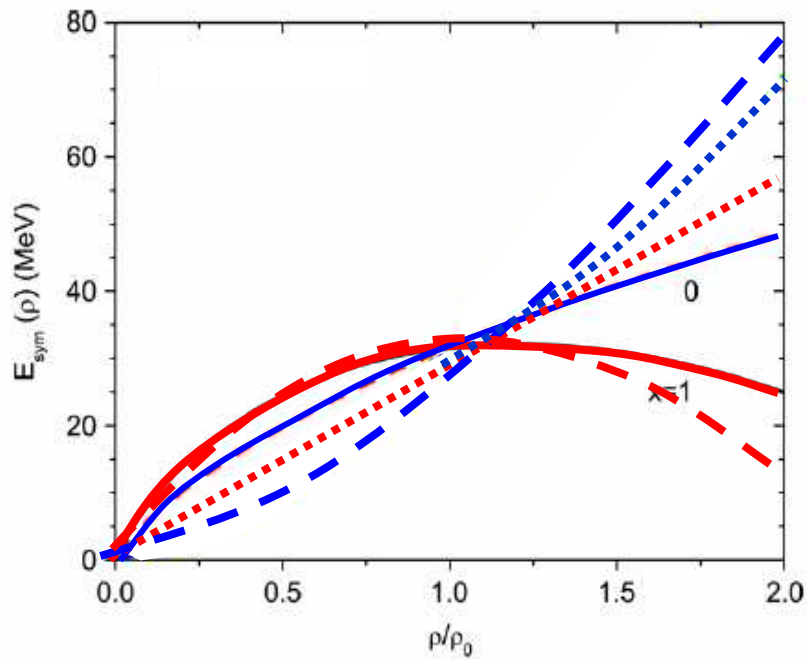
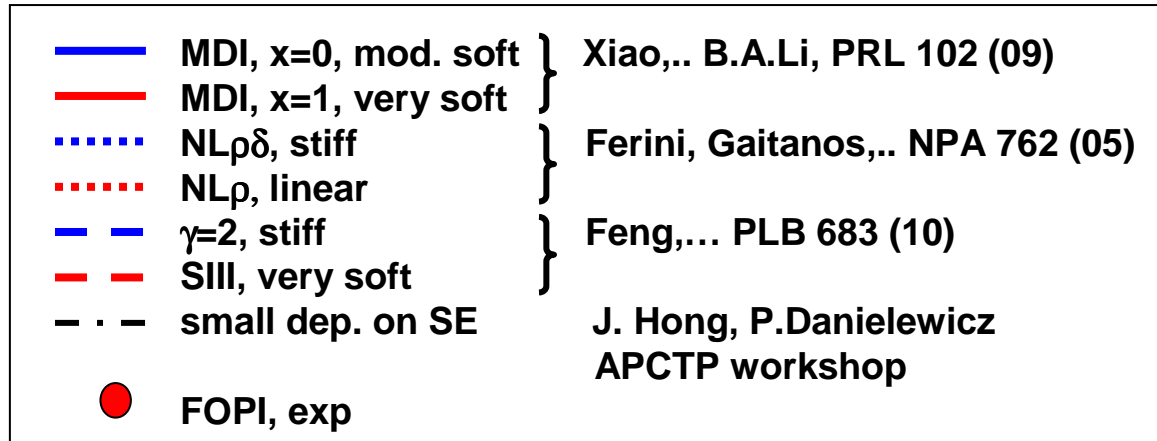
Pions: low and
high density
phase

Sensitivity to asy-
stiffness

Dependence of ratios on asy-stiffness

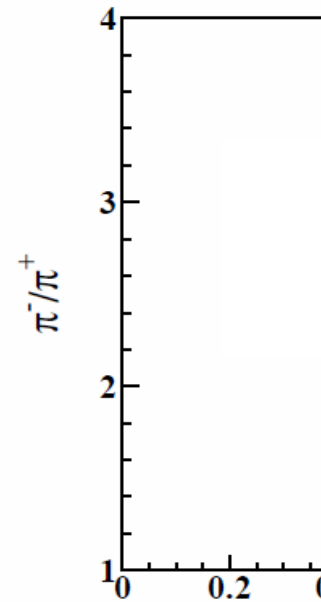
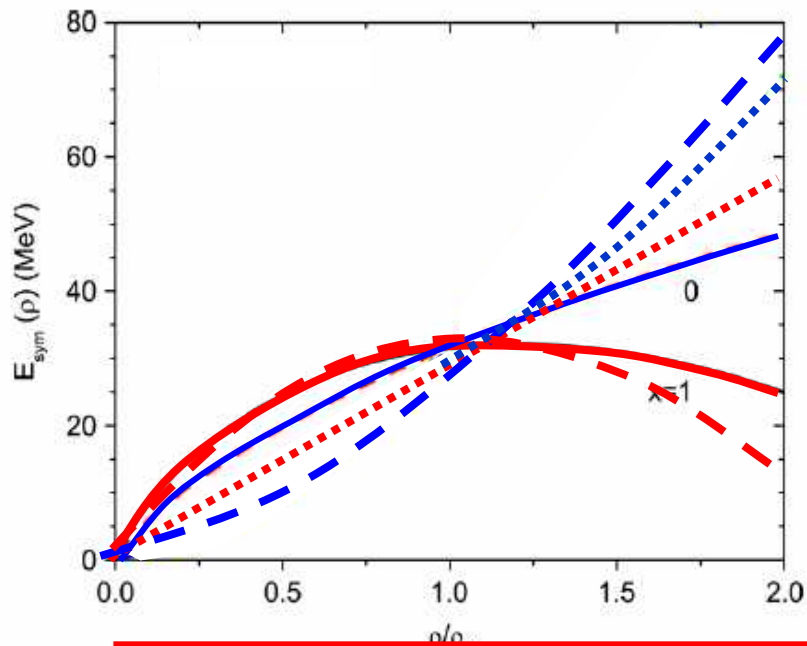
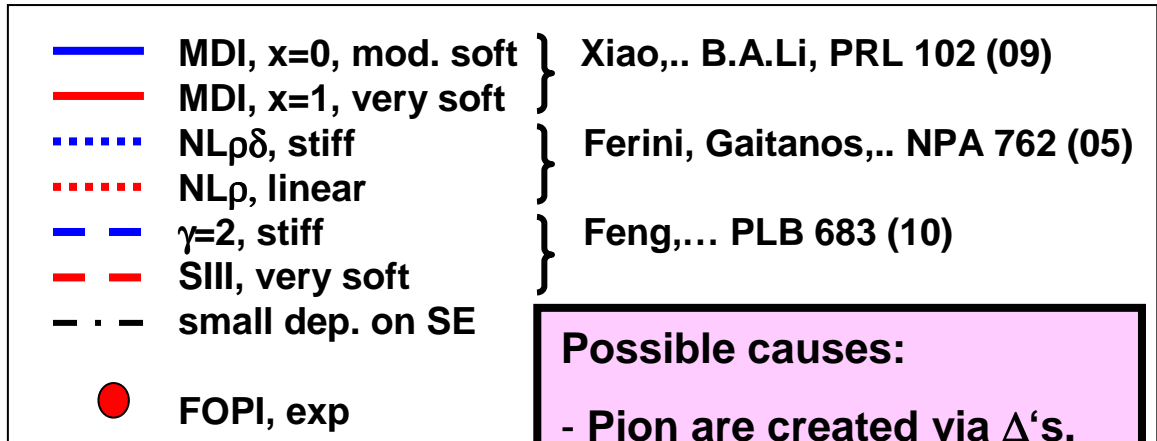
- n/p
- $\rightarrow \Delta^0/\Delta^{+,++}$
- $\rightarrow \pi/\pi^+, K^0/K^+$
- \rightarrow n/p ratio governs particle ratios

Pion ratios in comparison to FOPI data (W.Reisdorf et al. NPA781 (2007) 459)



Contradictory results of different calculations;

Pion ratios in comparison to FOPI data (W.Reisdorf et al. NPA781 (2007) 459)



Contradictory results of different calculations;

Possible causes:

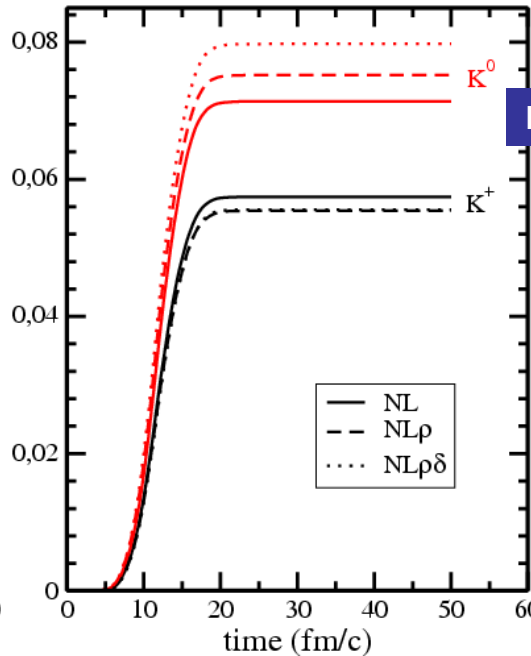
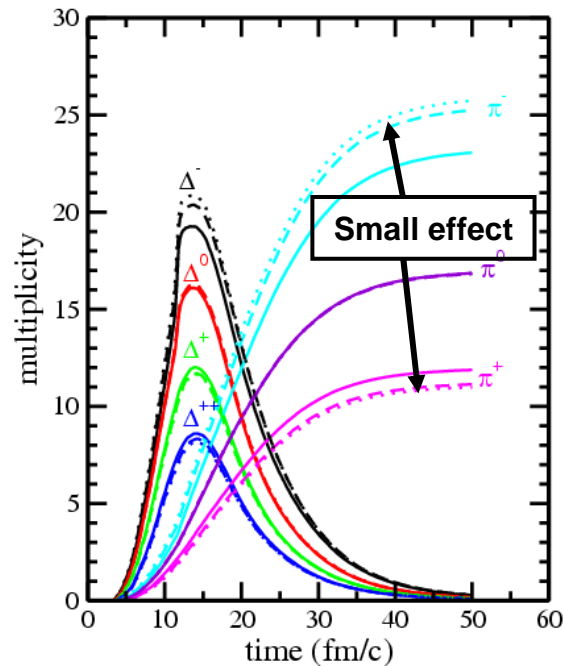
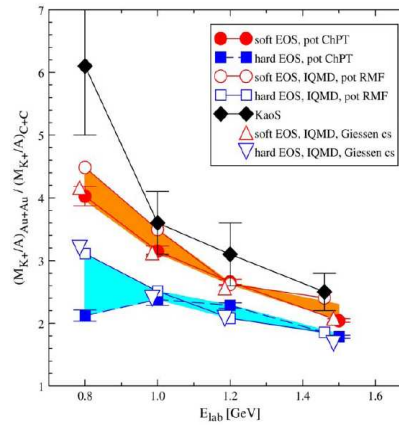
- Pion are created via Δ 's. Δ dynamics in medium (potential, width, etc) largely unknown.
- Threshold and mean field effects
- Pion potential: $U_\pi=0$ in most calculations. OK?
- differences in simulations, esp. collision term
- **Urgent problem to solve!!!**

Strangeness production in HIC: Kaons

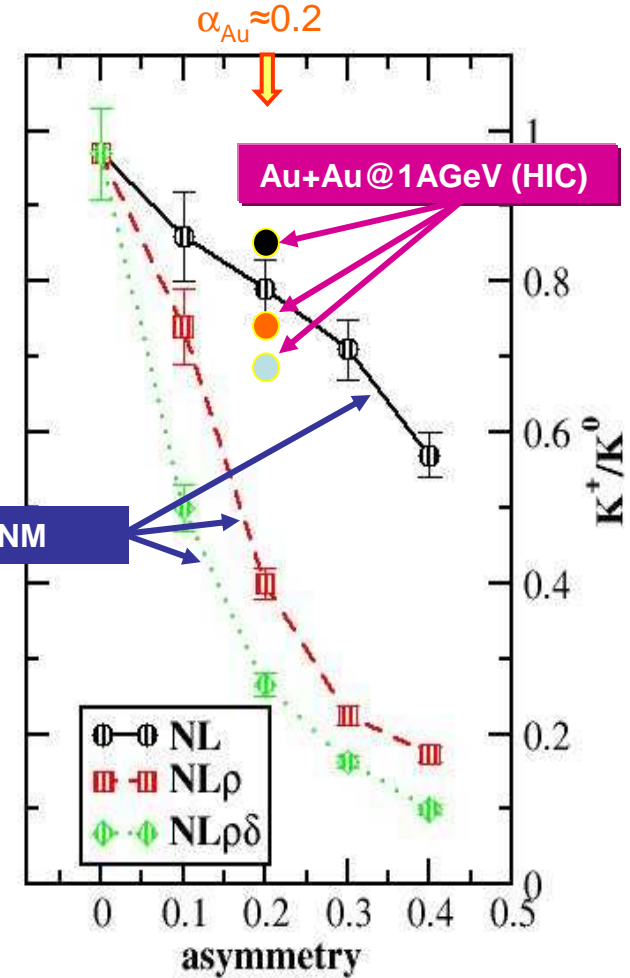
Kaons were a decisive observable to determine the symmetric EOS;

perhaps also useful for SE?

Kaons are **closer to threshold**, come only from **high density**, have **large mean free path**, **small width**:

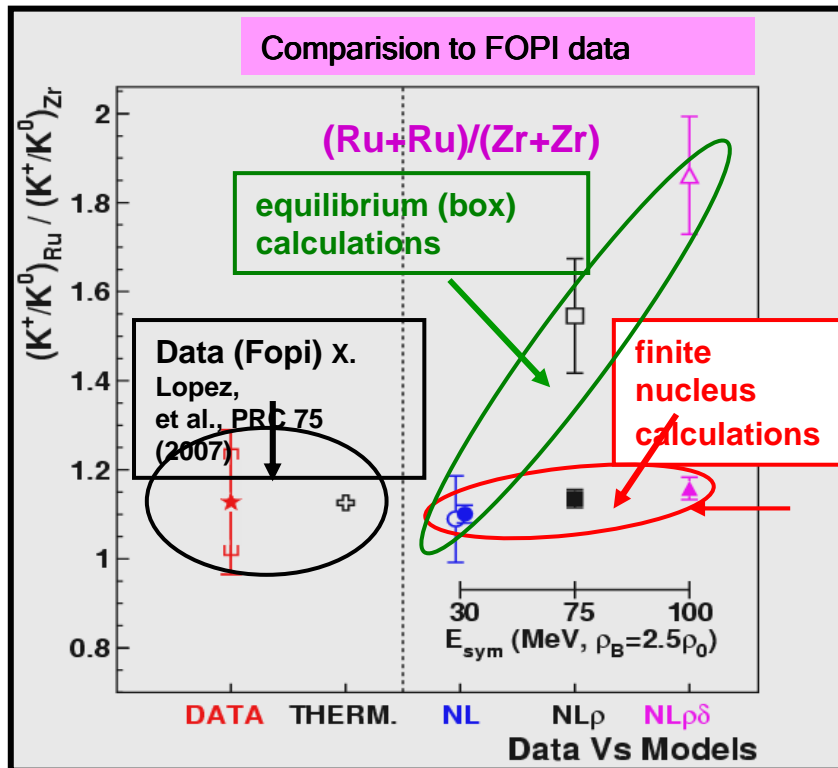


Larger (or equally large) effect for kaons, which come directly from high density region



Dynamic reduction of asymmetry in HIC, thus reduction of sensitivity rel. to nuclear matter

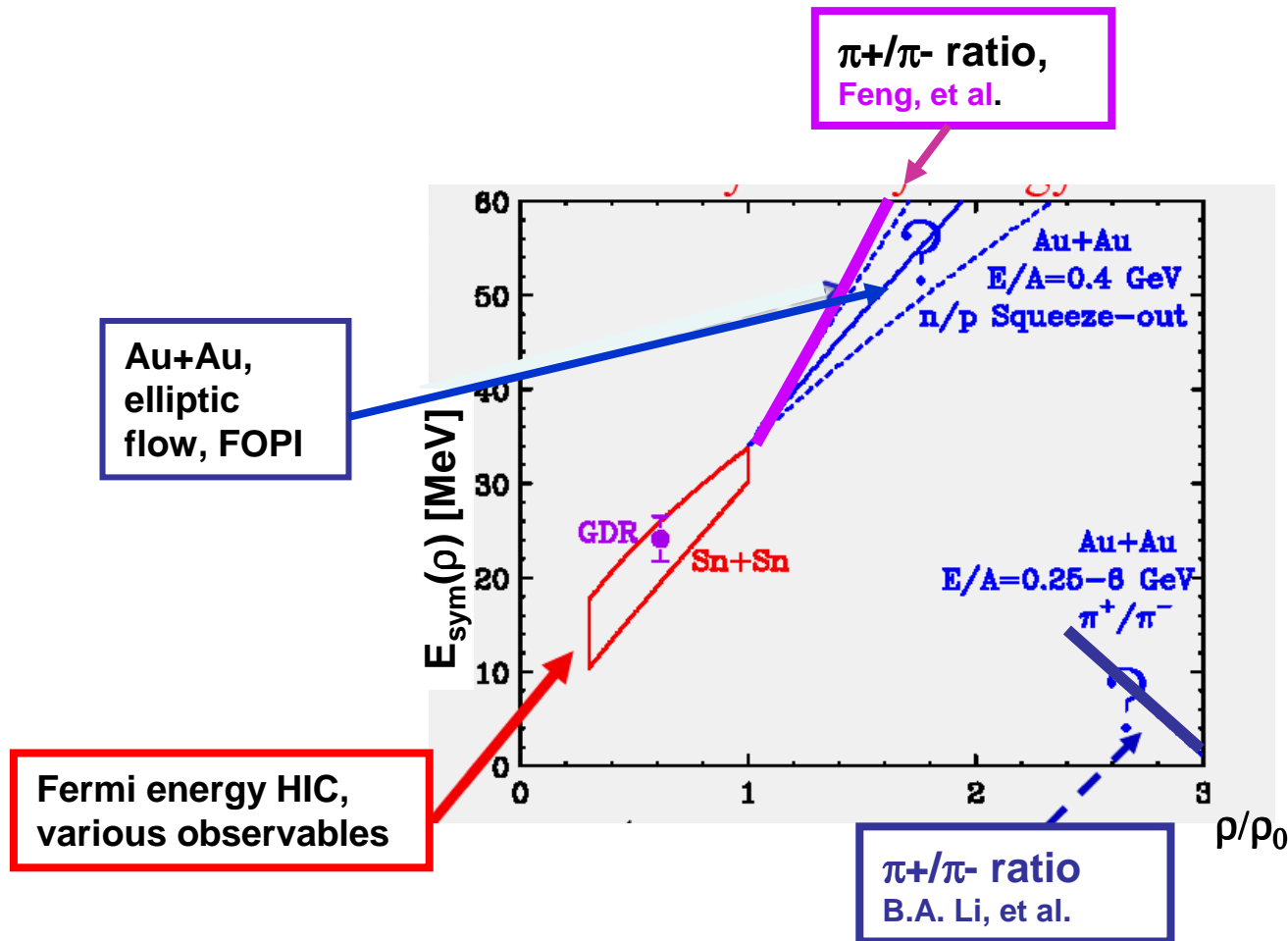
Kaon ratios in HIC



G. Ferini, et al., NPA762(2005) 147

- single ratios more sensitive
- enhanced in larger systems

Present constraints on the symmetry energy from heavy ion collisions



Moving towards a determination of the symmetry energy in HIC but at higher density few data and some difficulty with consistent results of simulations for pion observables.

Conclusion:

**There is a lot to know about the symmetry energy ...
and anyway, this talk was only to start of a discussion**

**I thank you for the attention
and I look forward to an exciting workshop**