

# Electric Dipole Response of $^{208}\text{Pb}$ and Constraints on the Symmetry Energy

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and RCNP-E282 Collaboration

NuSym13, July 22-26, 2013, NSCL

# Contents

- Electric dipole response of  $^{208}\text{Pb}$  has been precisely measured.

Method: proton inelastic scattering, electro-magnetic probe

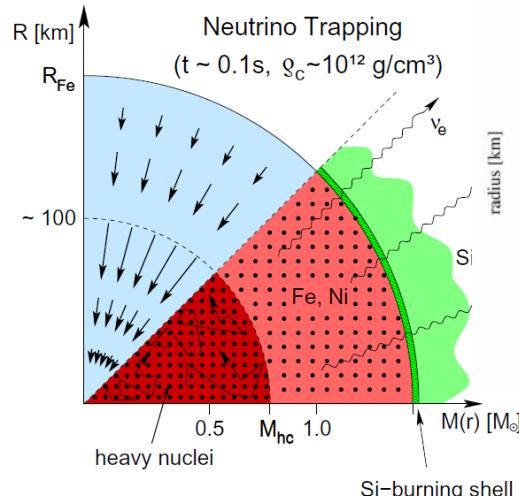
Extracted data: dipole polarizability, PDR strength

- Constraints on the symmetry energy has been determined.

with a help of mean-field calculations

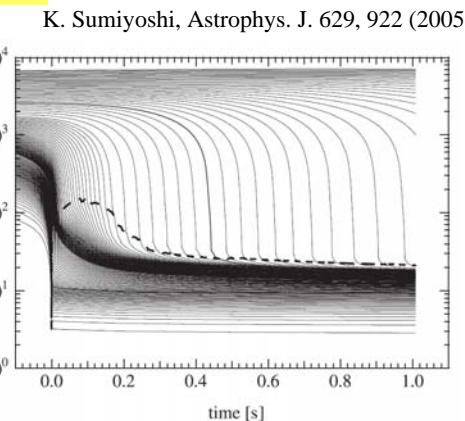
# Determination of the Symmetry Energy Term in EOS.

## Core-Collapse Supernova



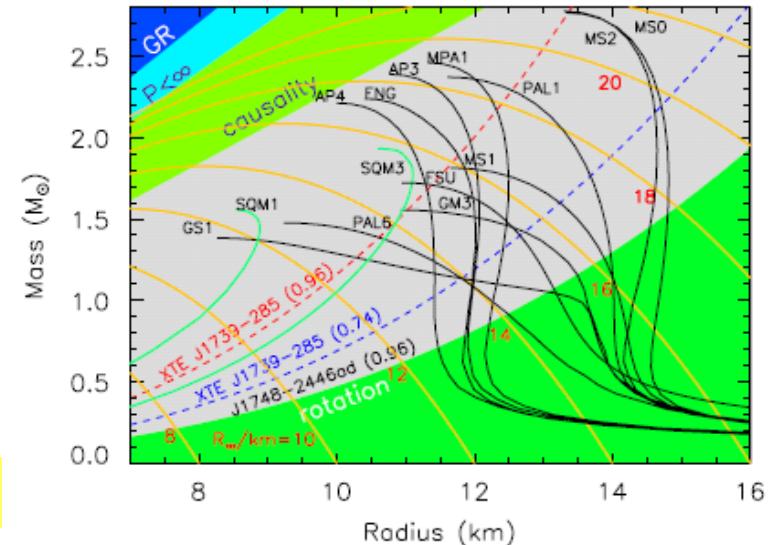
Langanke and Martinez-Pinedo

## Nucleosynthesis



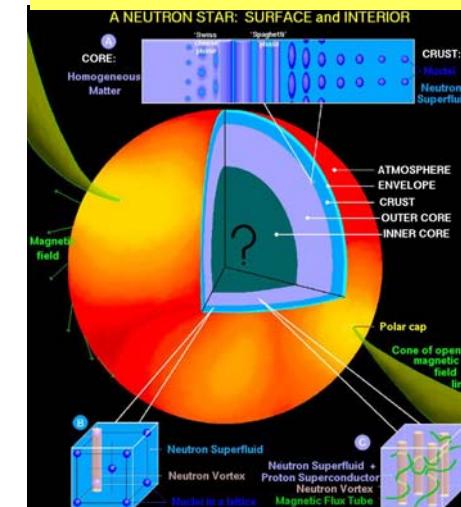
## Neutron Star Cooling

## Neutron Star Mass and Radius



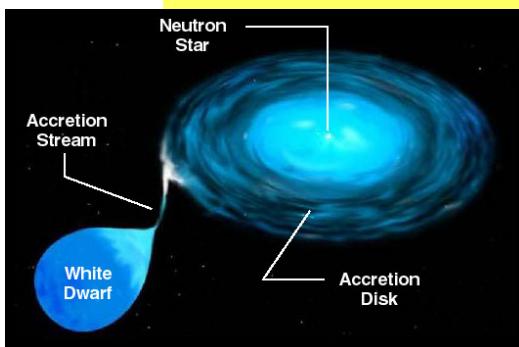
Lattimer et al., Phys. Rep. 442, 109(2007)

## Neutron Star Structure



<http://www.astro.umd.edu/~miller/nstar.html>

## Accreting neutron star/white dwarf, X-Ray burst, Superburst



# Nuclear Equation of State (EOS)

EOS for Energy per nucleon

$$\frac{E}{A}(\rho, \delta) = \frac{E}{A}(\rho, 0) + S(\rho)\delta^2 + \dots$$

Symmetry energy

$$S(\rho) = J + \frac{L}{3\rho_0}(\rho - \rho_0) + \frac{K_{sym}}{18\rho_0^2}(\rho - \rho_0)^2 + \dots$$

$$\rho(r) = \rho_n(r) + \rho_p(r)$$

$$\delta(r) = \frac{\rho_n(r) - \rho_p(r)}{\rho_n(r) + \rho_p(r)}$$

Saturation Density  
 $\sim 0.16 \text{ fm}^{-3}$   
 $\rho_0$ :

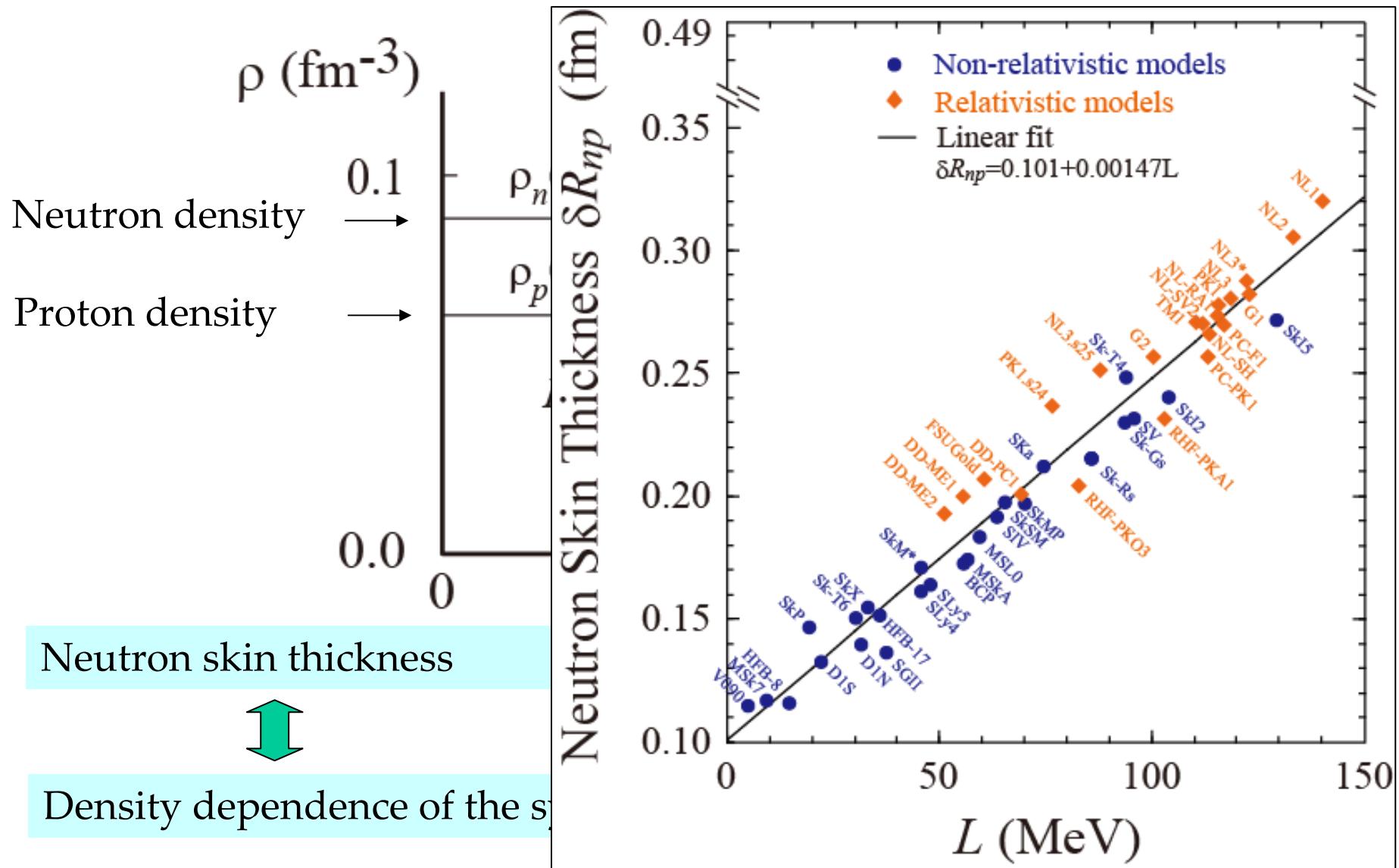
$L \propto P \propto R_{\text{n-star}}^4$

(Baryonic Pressure)

# Neutron Skin and the Density Dependence of the Symmetry Energy

X. Roca-Maza *et al.*, PRL 106, 25250

X. Roca-Maza *et al.*, PRL106, 252501 (2011)



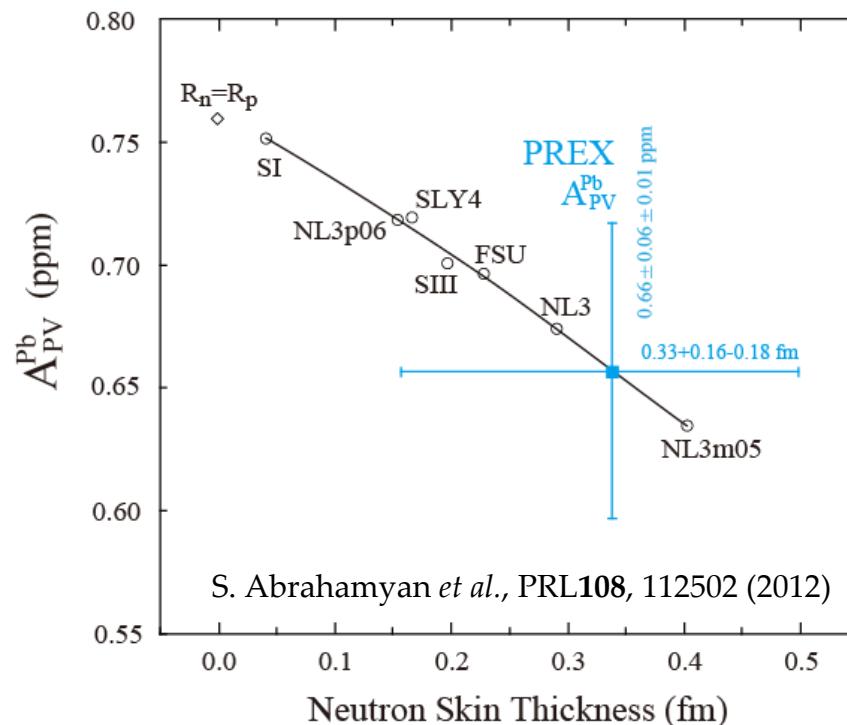
# Neutron Skin Thickness Measurement by Electroweak Interaction

**PREX at J-Lab:**  $Z^0$  of weak interaction : sees the neutrons

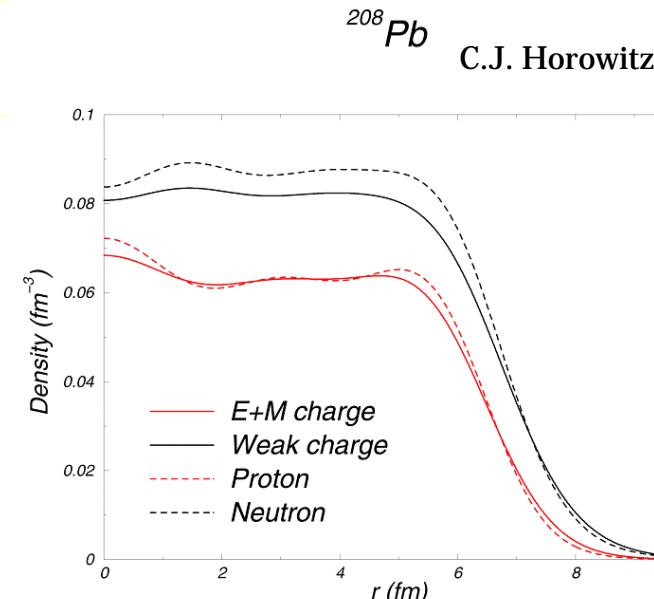
	p	n
Electric charge	1	0
Weak charge	0.08	1

$$A = \frac{\left(\frac{d\sigma}{d\Omega}\right)_R - \left(\frac{d\sigma}{d\Omega}\right)_L}{\left(\frac{d\sigma}{d\Omega}\right)_R + \left(\frac{d\sigma}{d\Omega}\right)_L} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ 1 - 4\sin^2\theta_W - \frac{F_N(Q^2)}{F_P(Q^2)} \right]$$

$$A = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ 1 - 4\sin^2\theta_W - \frac{F_N(Q^2)}{F_P(Q^2)} \right]$$



**Parity Violating Asymmetry**

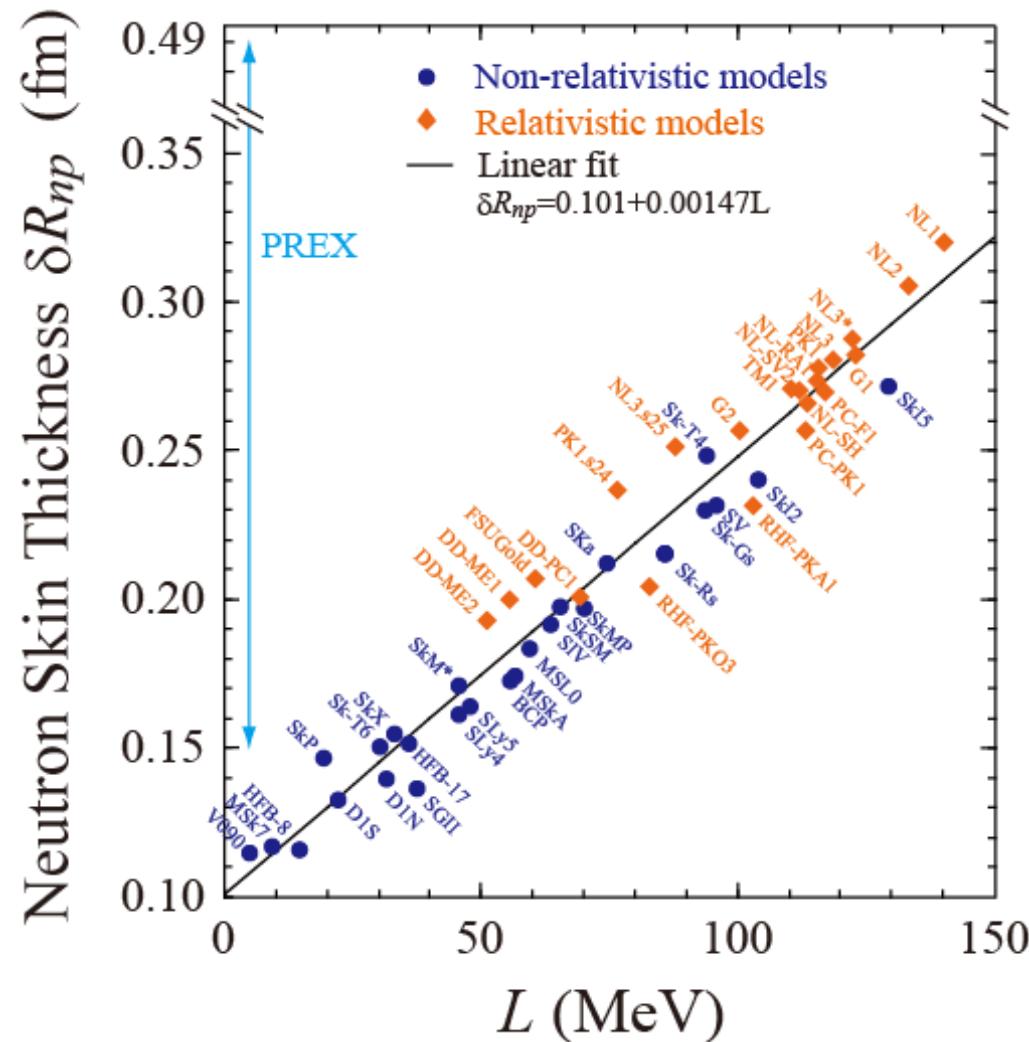


Talk by K. Kumar Thursday

Model independent determination of the neutron skin thickness

# Neutron Skin Thickness Measurement by Electroweak Interaction

**PREX**



REX Result: S. Abrahamyan *et al.*,  
RL108, 112502 (2012)

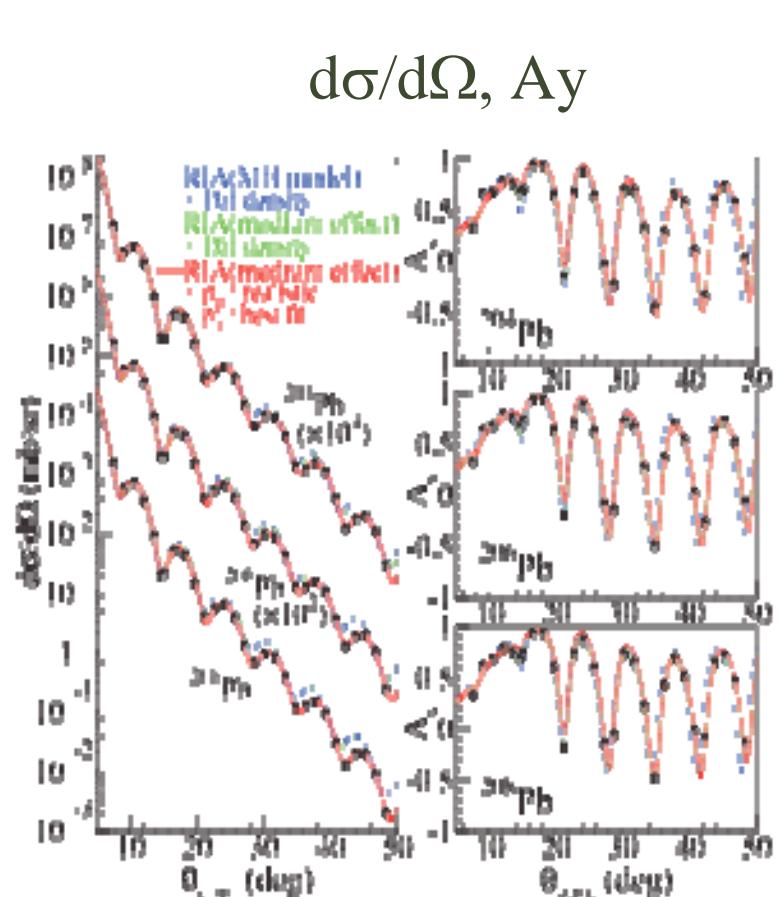
Theor. Calc.: X. Roca-Maza *et al.*,  
PRL106, 252501 (2011)

The model independent determination of  $\delta R_{np}$  by PREX is important but the present accuracy is limited.

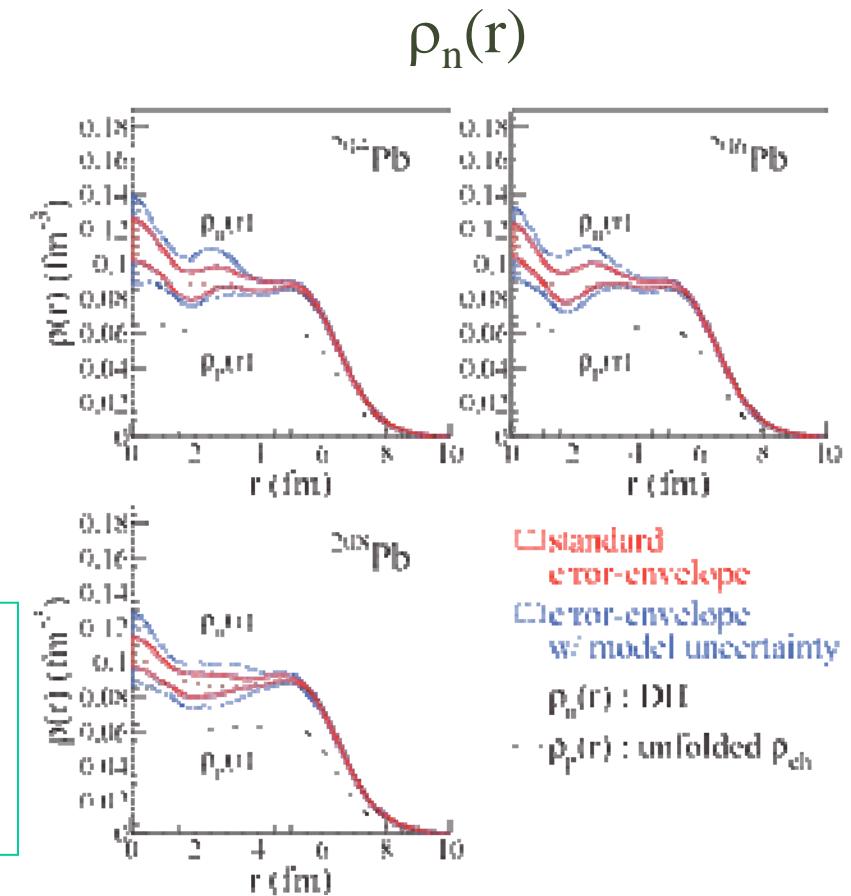
# Determination of Neutron Density Distribution by Strong Interaction

Polarized proton elastic scattering at 295 MeV (RCNP, Osaka University)

Analysis with relativistic impulse approximation (RIA), medium modification fixed with  $^{58}\text{Ni}$  data



RIA  
+  
Medium  
Effect

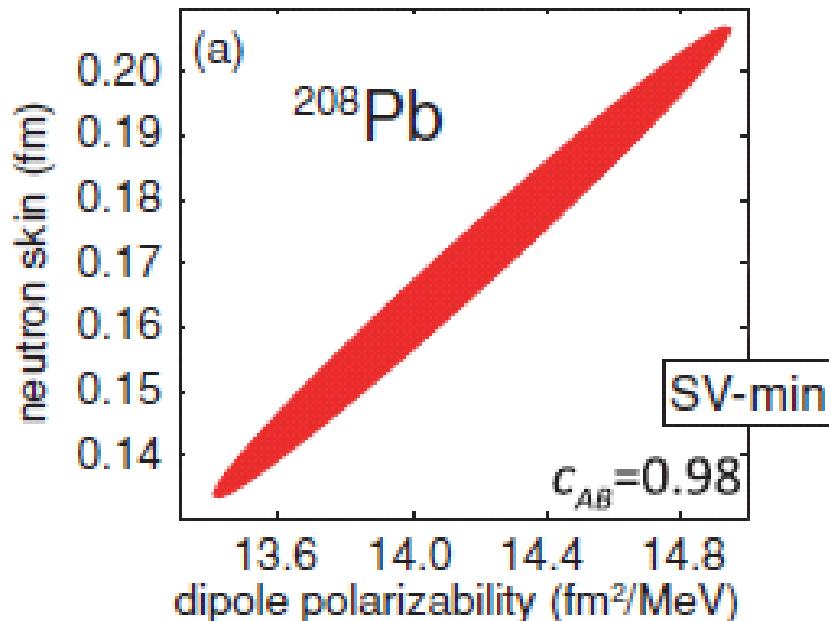


J.Zenhiro et al., PRC 82, 044611 (2010)

Poster presentation by J. Zenihiro

neutron skin thickness of  $^{208}\text{Pb}$ :  
 $0.211+0.054-0.063$  fm

# Neutron Skin Thickness Measurement by Electromagnetic Interaction

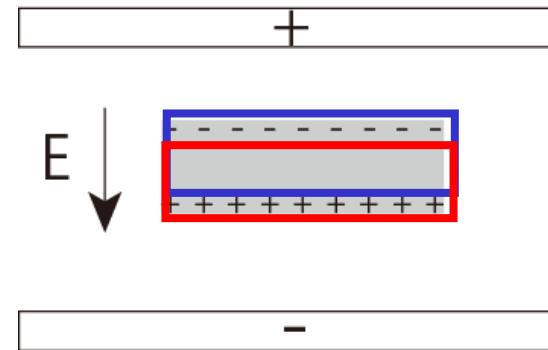
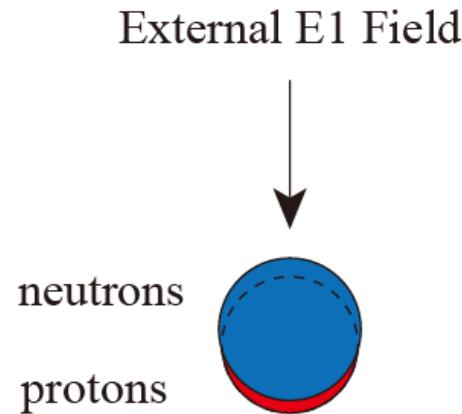


Covariance analysis of energy density functional calculations with Skrym SV-min effective interaction.

P.-G. Reinhard and W. Nazarewicz, PRC 81, 051303(R) (2010).

Strong correlation between the (electric) dipole polarizability and the neutron skin of  $^{208}\text{Pb}$

# (Electric) Dipole Polarizability



Electric Dipole Polarizability

Electric Dipole Polarization

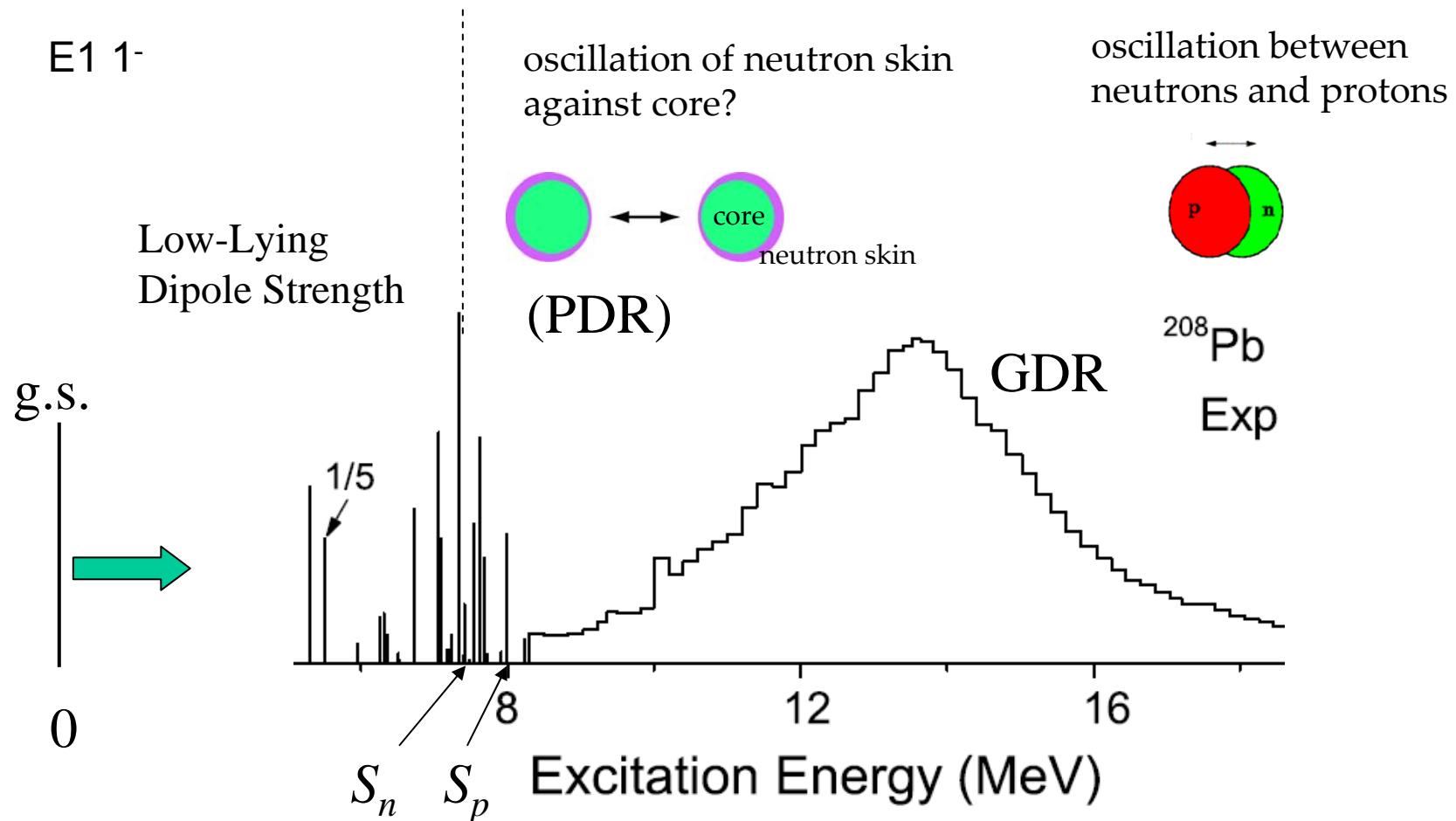
$$\mathbf{P} = \alpha \mathbf{E}$$

Inversely energy weighted sum-rule of  $B(E1)$

$$\alpha_D = \frac{\hbar c}{2\pi^2} \int \frac{\sigma_{abs}}{\omega^2} d\omega = \frac{8\pi}{9} \int \frac{dB(E1)}{\omega}$$

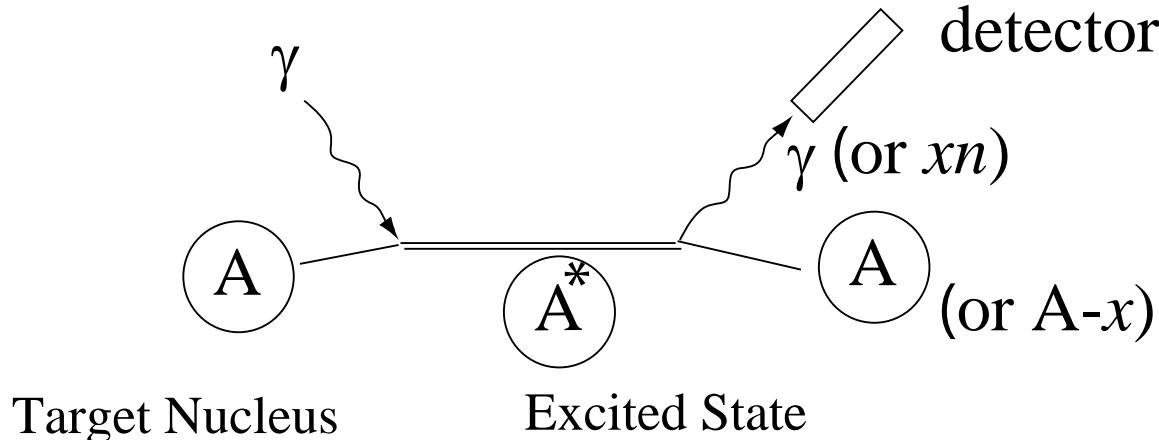
# Electric Dipole (E1) Response

Particle (neutron) separation energy



# Probing EM response of the target nucleus

- Real Photon Measurements, NRF and  $(\gamma, xn)$

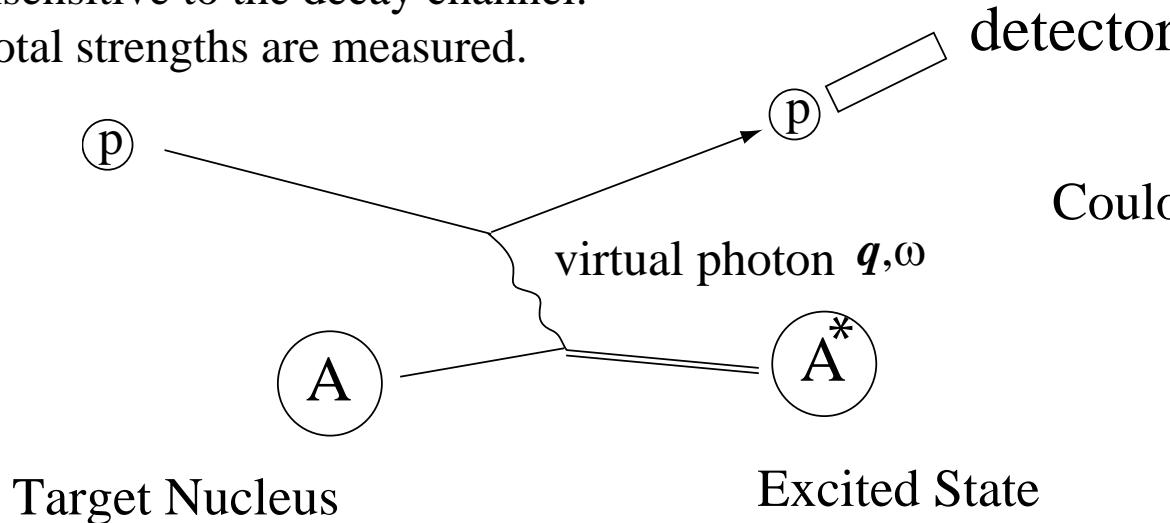


**Decay  $\gamma$ -rays or neutrons are measured.**

- Missing Mass Spectroscopy with Virtual Photon

Insensitive to the decay channel.

Total strengths are measured.



**Only the scattered protons are measured.**

Select low momentum transfer ( $q \sim 0$ ) kinematical condition, i.e. at zero degrees

Coulomb Excitation at 0 deg.

EM Interaction is well known (model independent)

# Proton Inelastic Scattering at Forward Angles

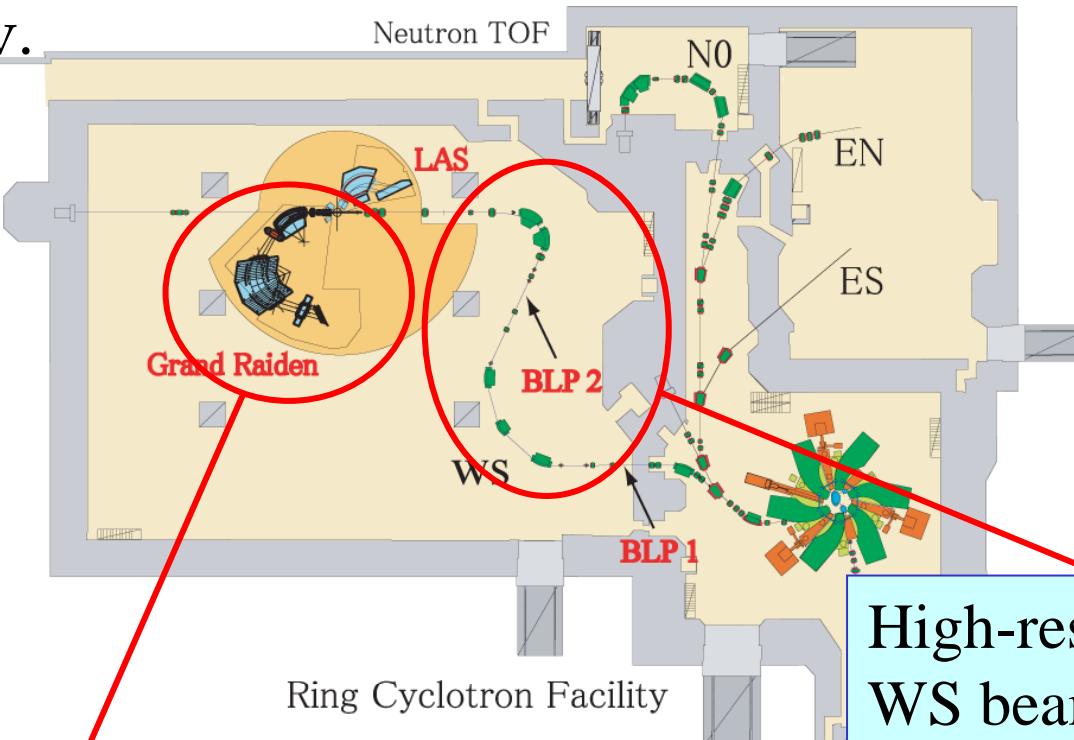
- An **electromagnetic** probe (Coulomb excitation)
- **High-resolution** (20-30keV), **high** (~90%)/**uniform efficiency**
- Covers a broad **Ex of 5-25MeV**
- Insensitive to the decay property
- Requires **small amount of target** (several mili-gram) and a few days of beam time
- Applicable to stable nuclei

# Experimental Method

High-resolution polarized ( $p,p'$ ) measurement  
at zero degrees and forward angles

# Research Center for Nuclear Physics, Osaka Univ.

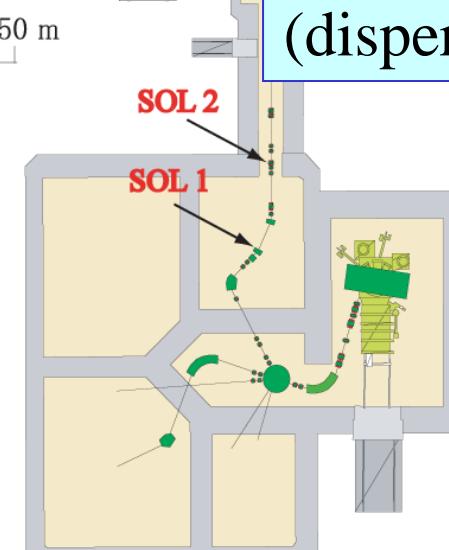
NuSym13, July 22-26, 2013 at NSCL



High-resolution Spectrometer

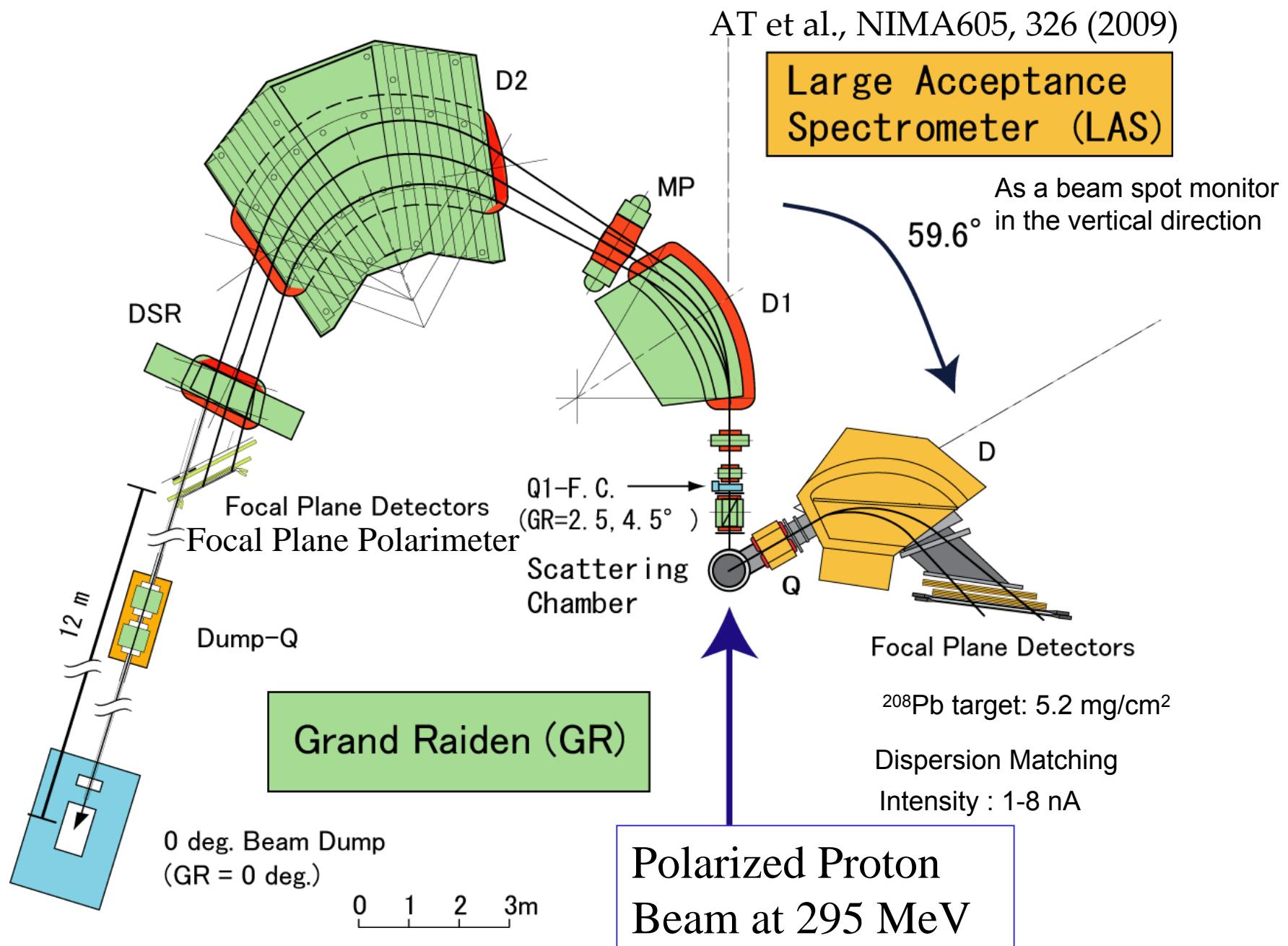
Grand Raiden

High-resolution  
WS beam-line  
(dispersion matching)



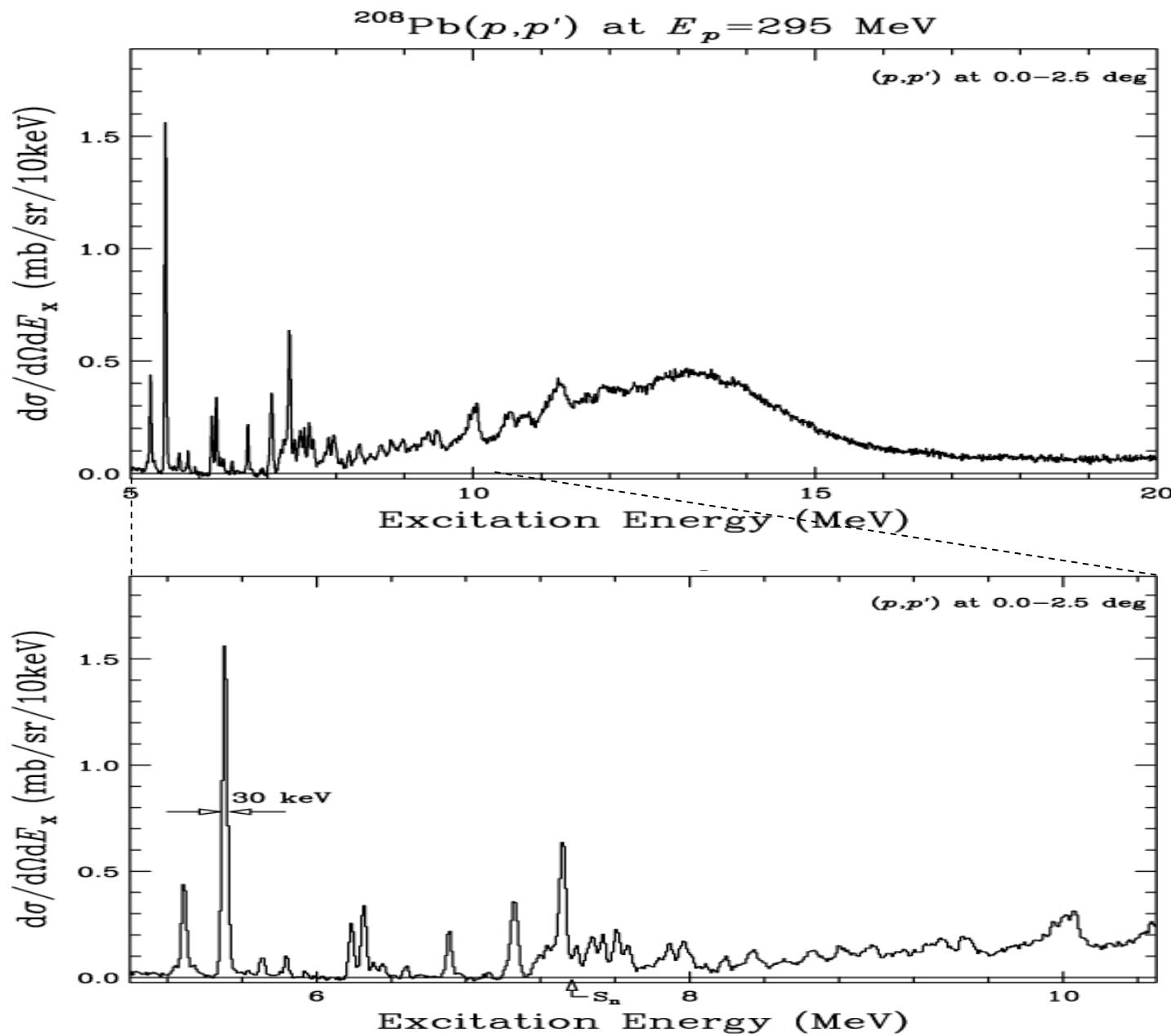
AVF Cyclotron Facility

# Spectrometers in the 0-deg. experiment setup

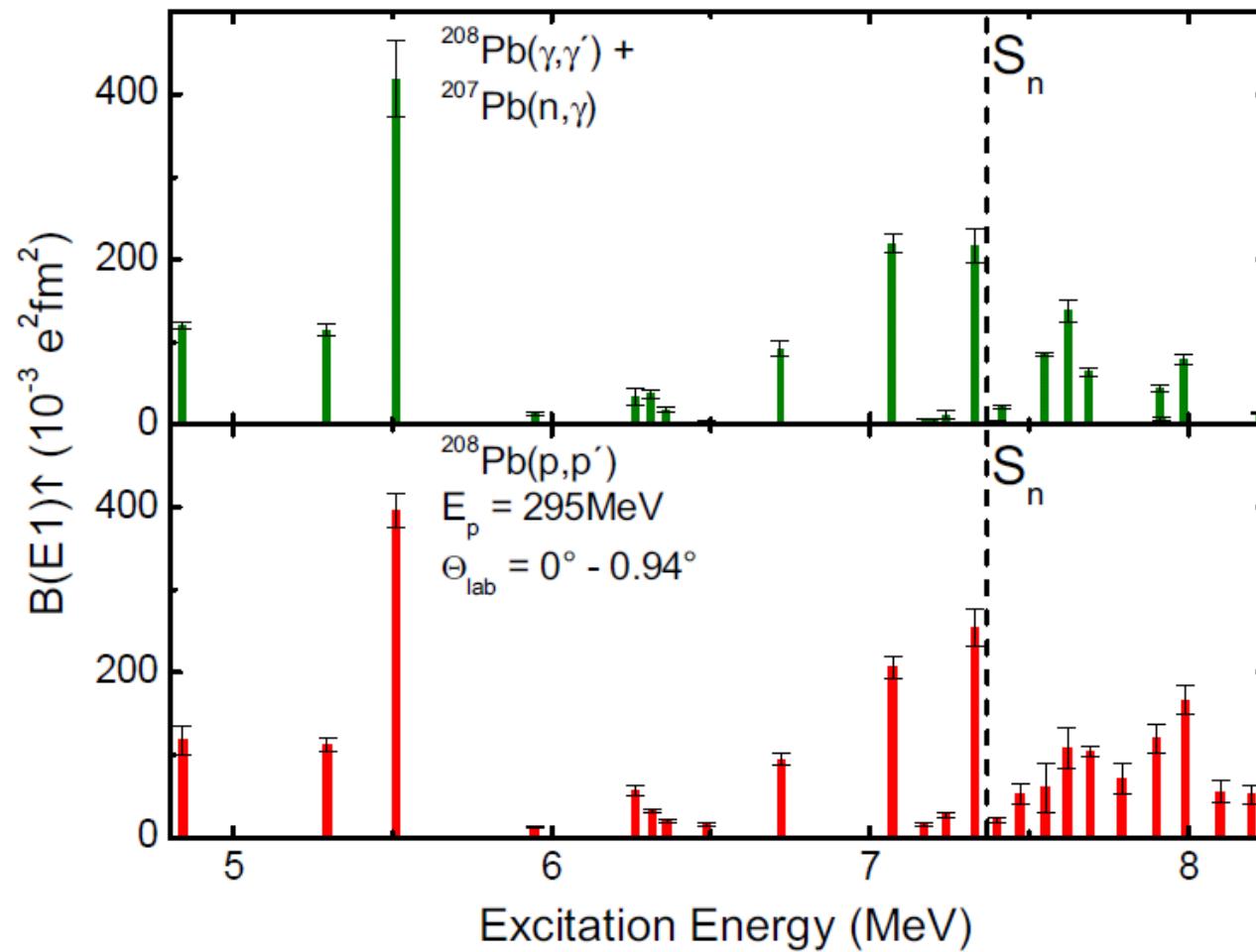


# Setup for E282&E316





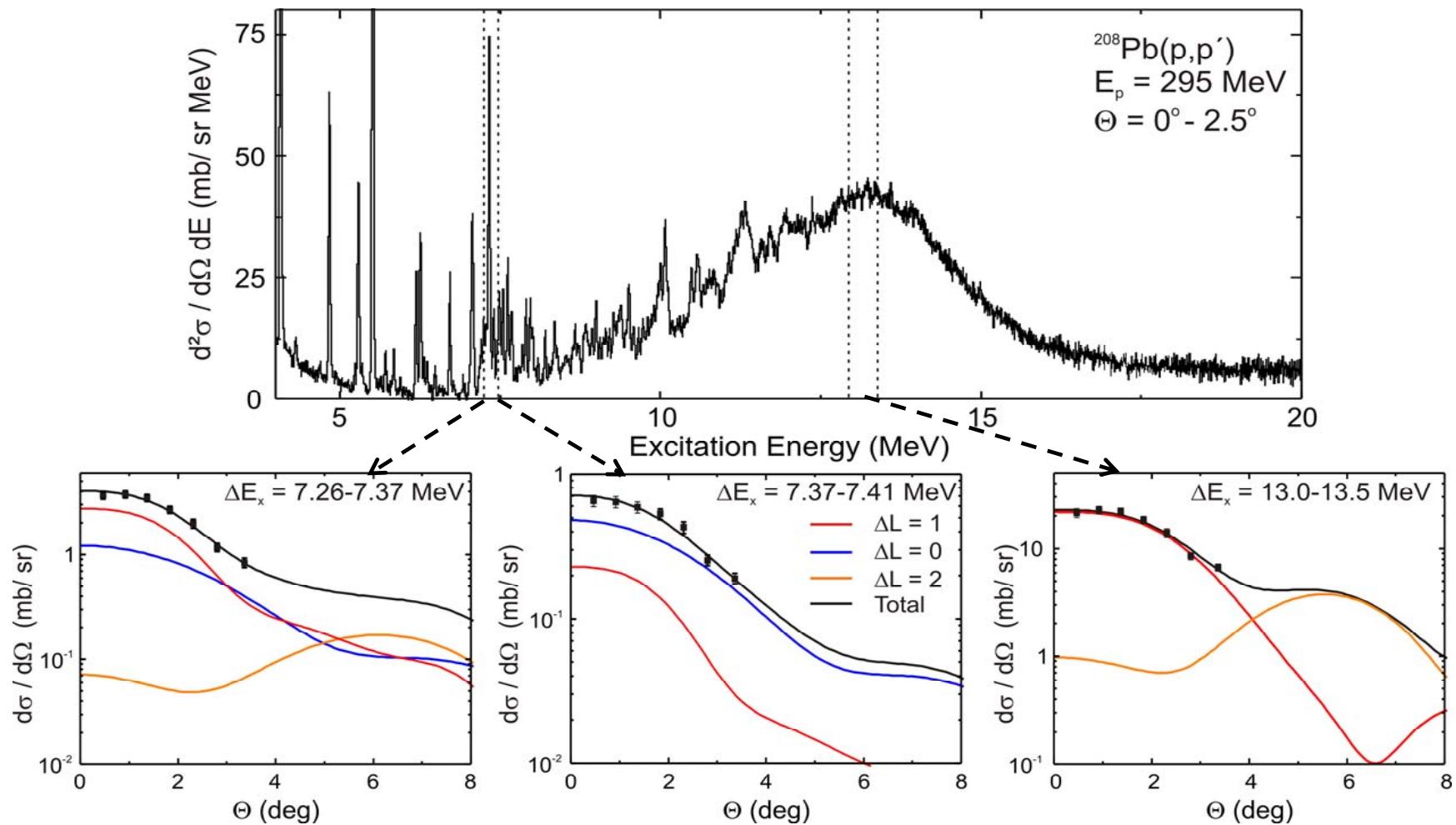
# $B(E1)$ : low-lying discrete states



Excellent agreement between  $(p, p')$  and  $(\gamma, \gamma')$  below  $\sim S_n$

# B(E1): continuum and GDR region

## Method 1: Multipole Decomposition



- Neglect of data for  $\Theta > 4^\circ$ : ( $p,p'$ ) response too complex
- Included E1/M1/E2 or E1/M1/E3 (little difference)

# B(E1): continuum and GDR region

## Method 2: Decomposition by Spin Observables

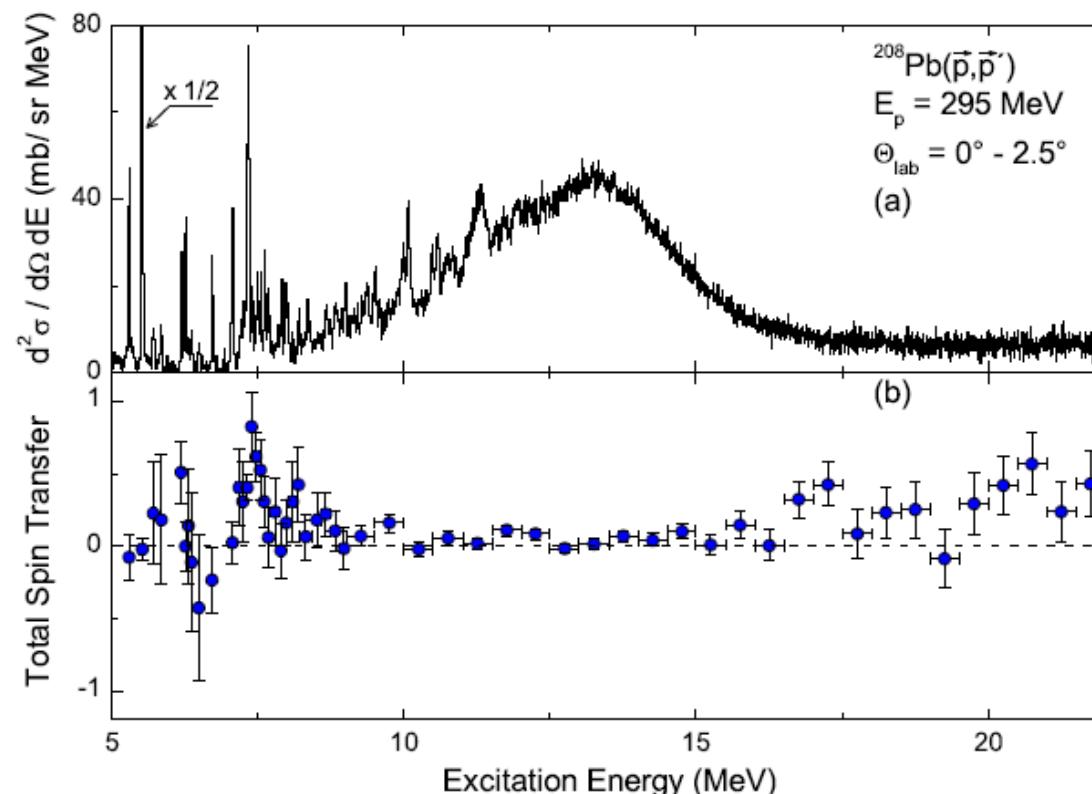
● Polarization observables at  $0^\circ$   spinflip / non-spinflip separation

model-independent

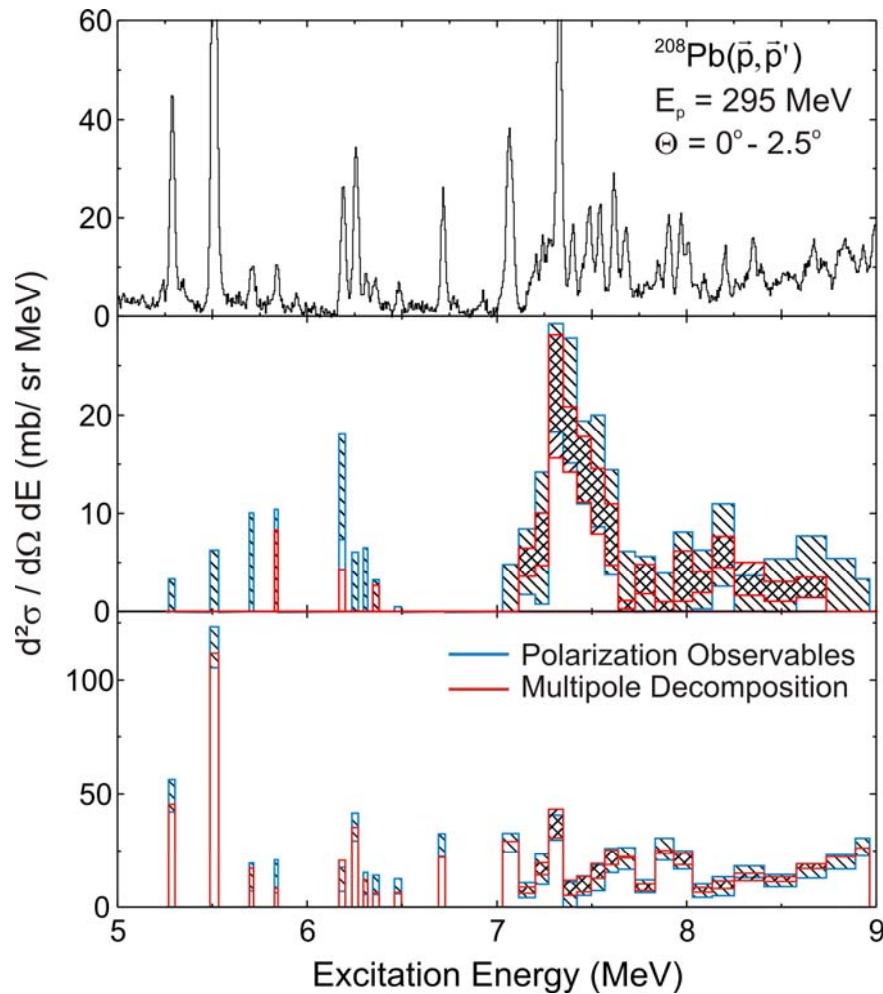
E1 and M1 decomposition

T. Suzuki, PTP 103 (2000) 859

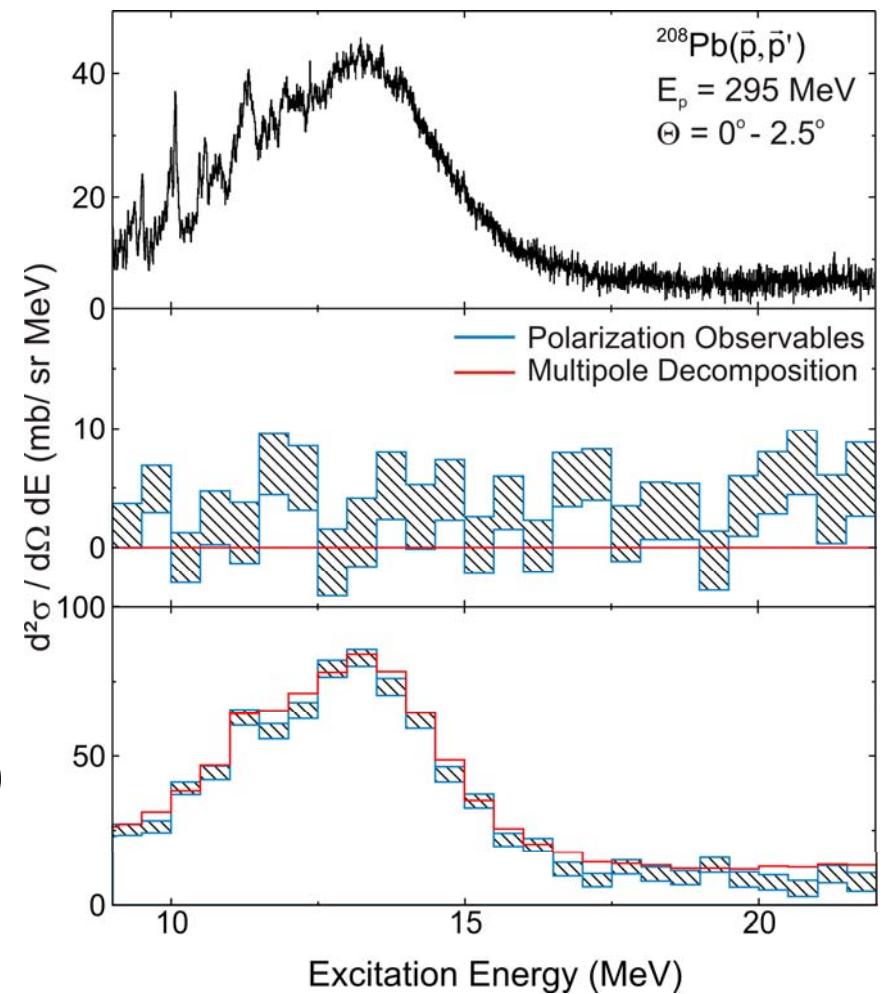
$$\text{Total Spin Transfer } \Sigma \equiv \frac{3 - (2D_{SS} + D_{LL})}{4} = \begin{cases} 1 & \text{for } \Delta S = 1 \quad \text{M1} \\ 0 & \text{for } \Delta S = 0 \quad \text{E1} \end{cases}$$

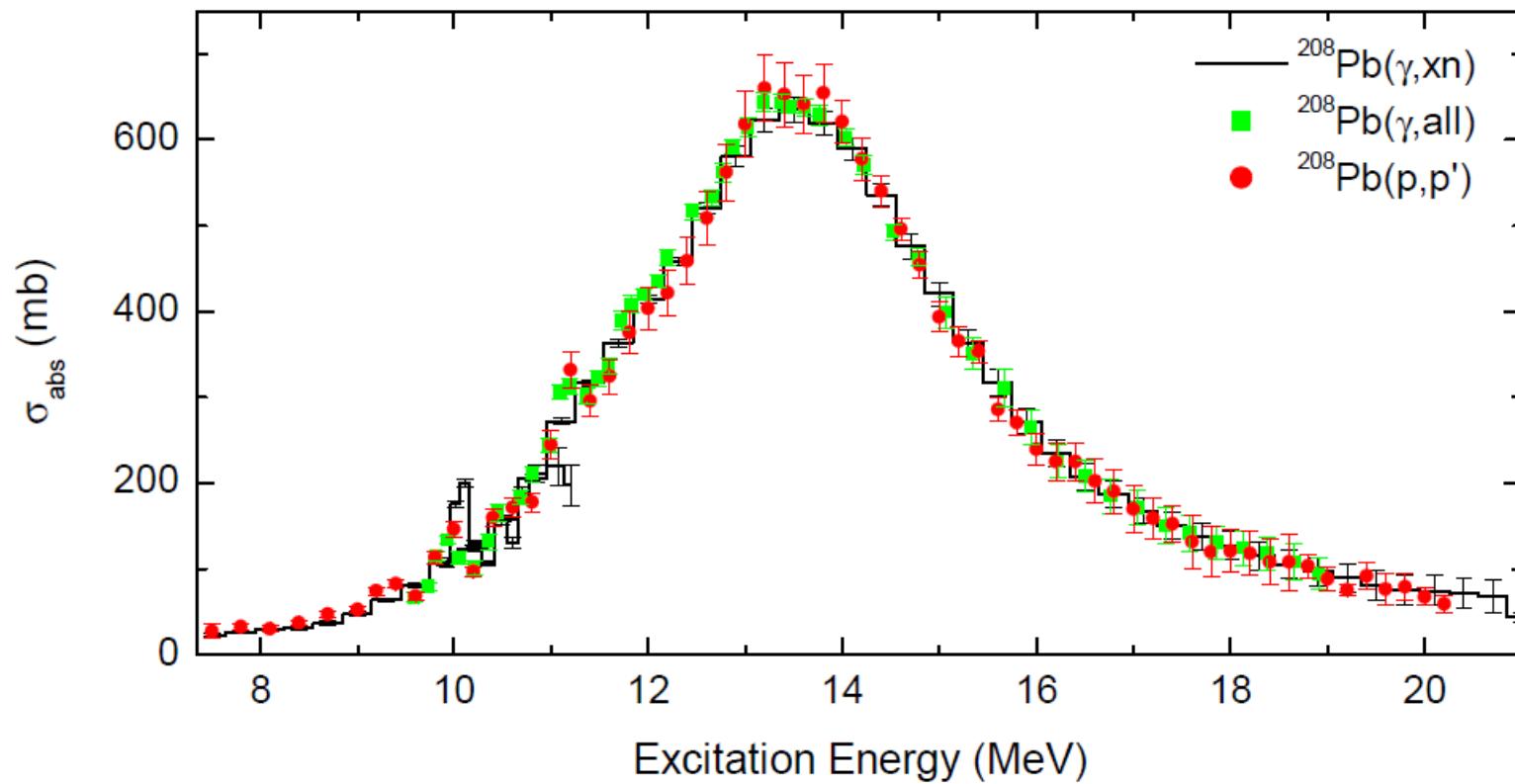


# Comparison between the two methods



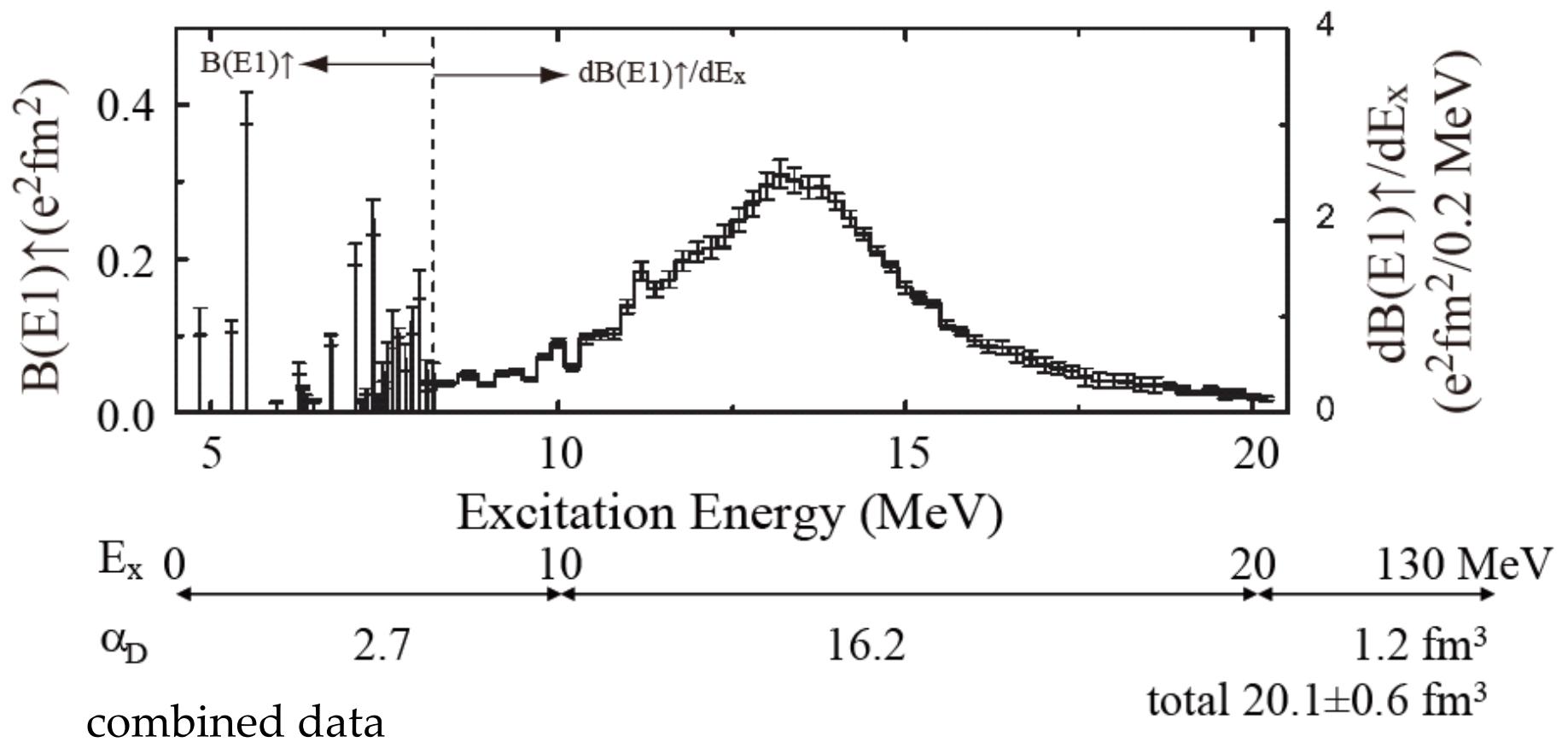
Total

 $\Delta S = 1$  $\Delta S = 0$ 



Excellent agreement among three measurements  
around the GDR bump region

## E1 Response of $^{208}\text{Pb}$ and $\alpha_D$



The dipole polarizability of  $^{208}\text{Pb}$  has been precisely determined.

# Abstract

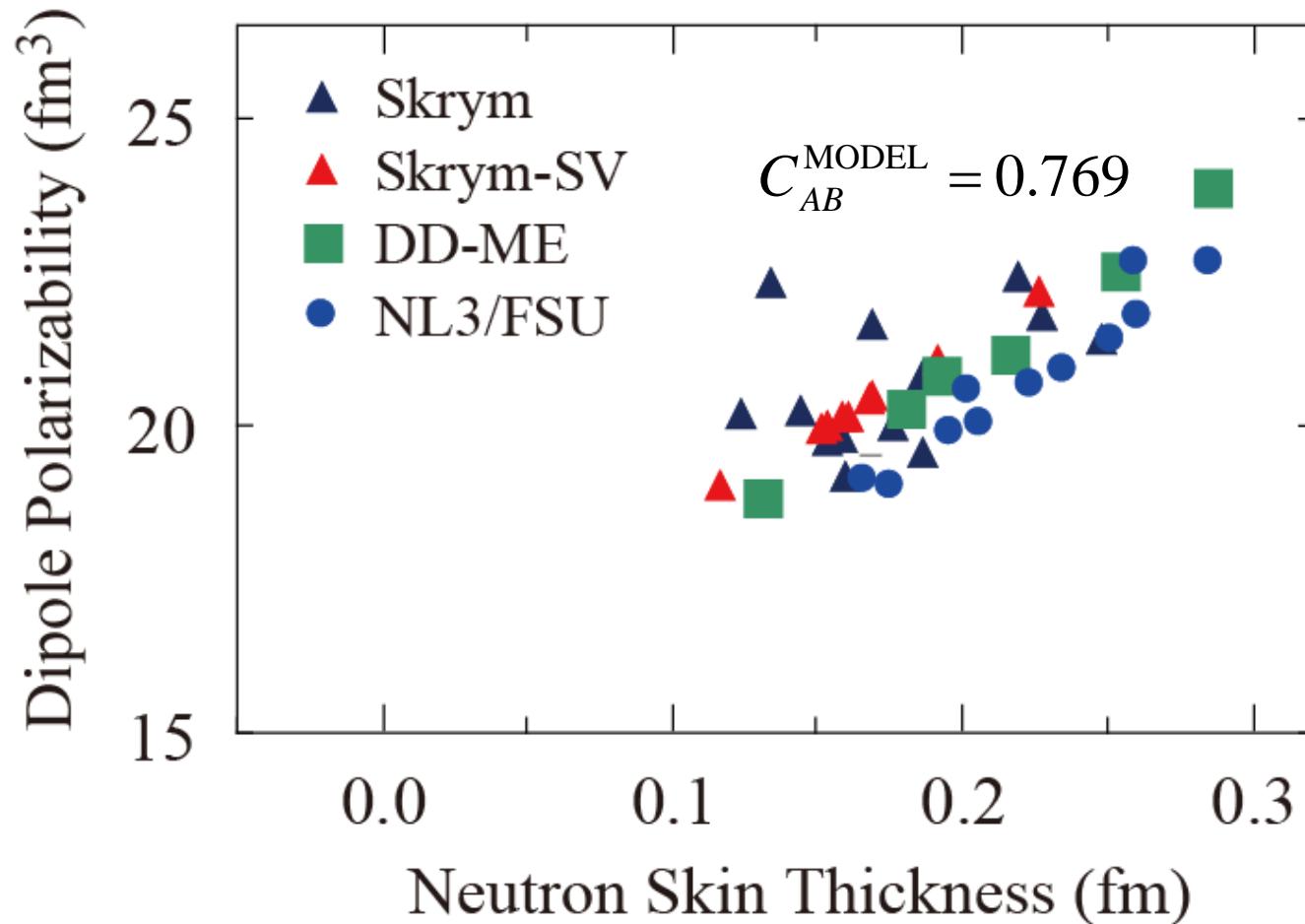
B(E1) distribution of  $^{208}\text{Pb}$  has been precisely determined.

Dipole polarizability:  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$

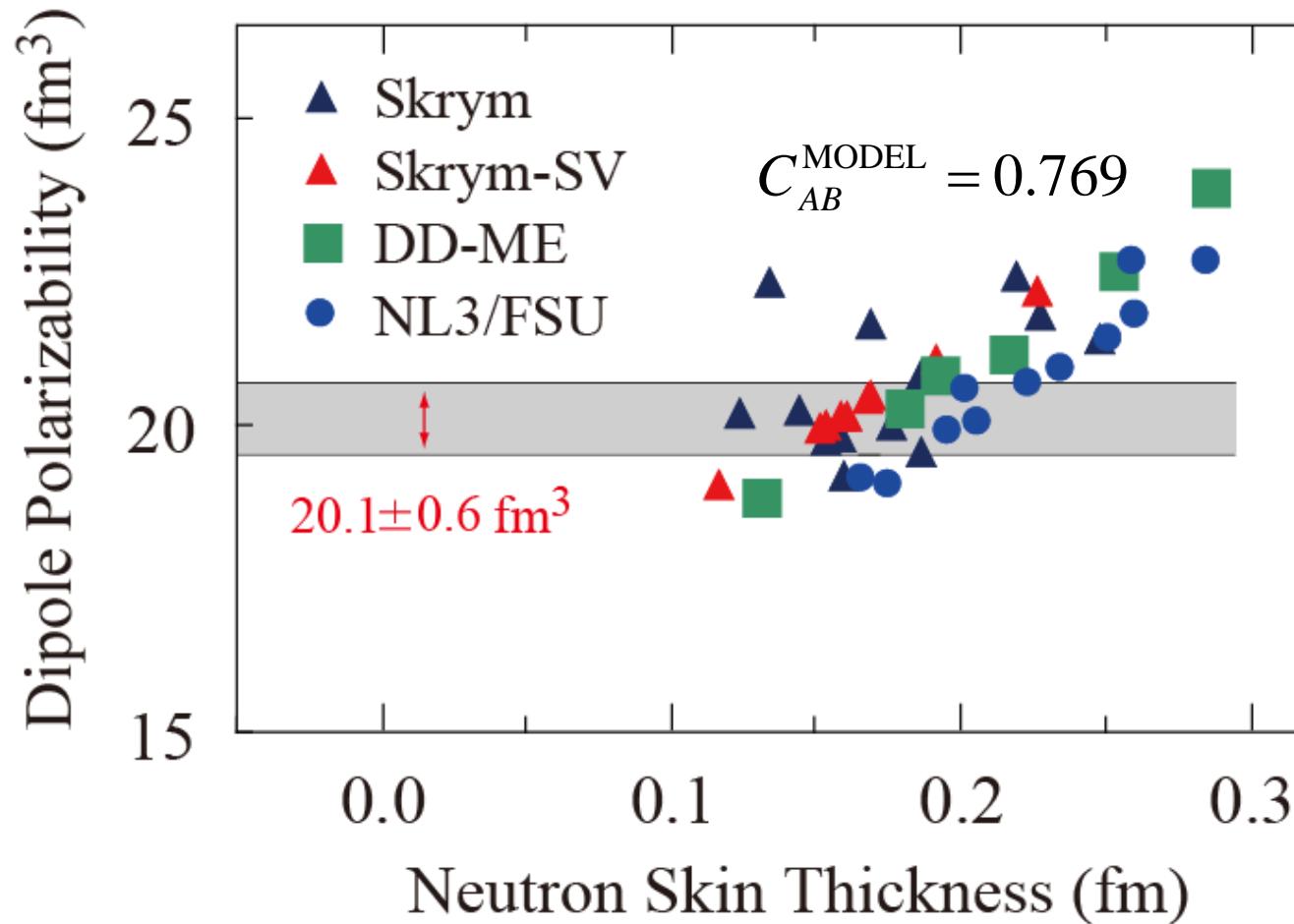
Constraints on the symmetry energy

with a help of theoretical models

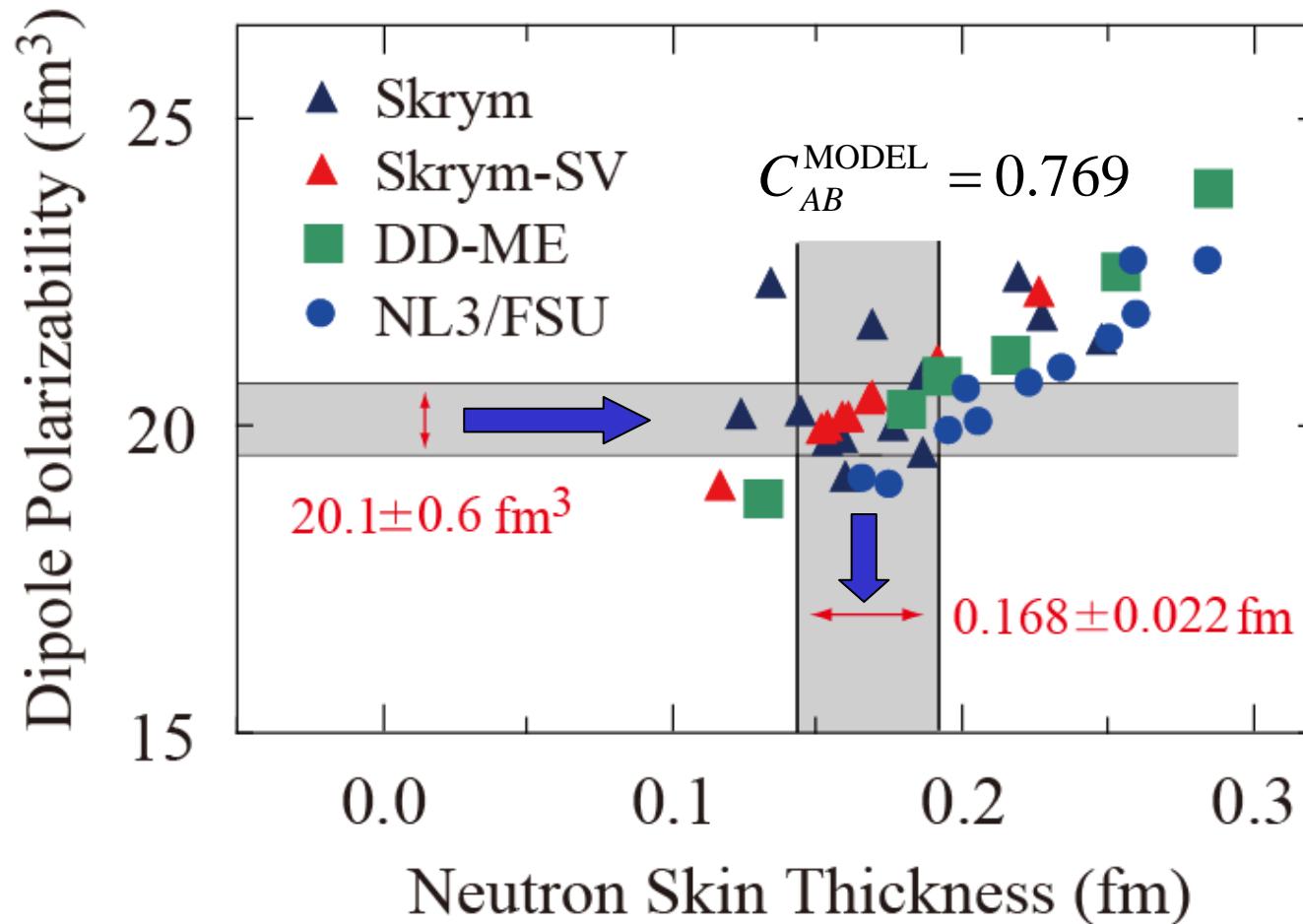
# Correlation Between Dipole Polarizability and Neutron Skin Thickness



# Correlation Between Dipole Polarizability and Neutron Skin Thickness

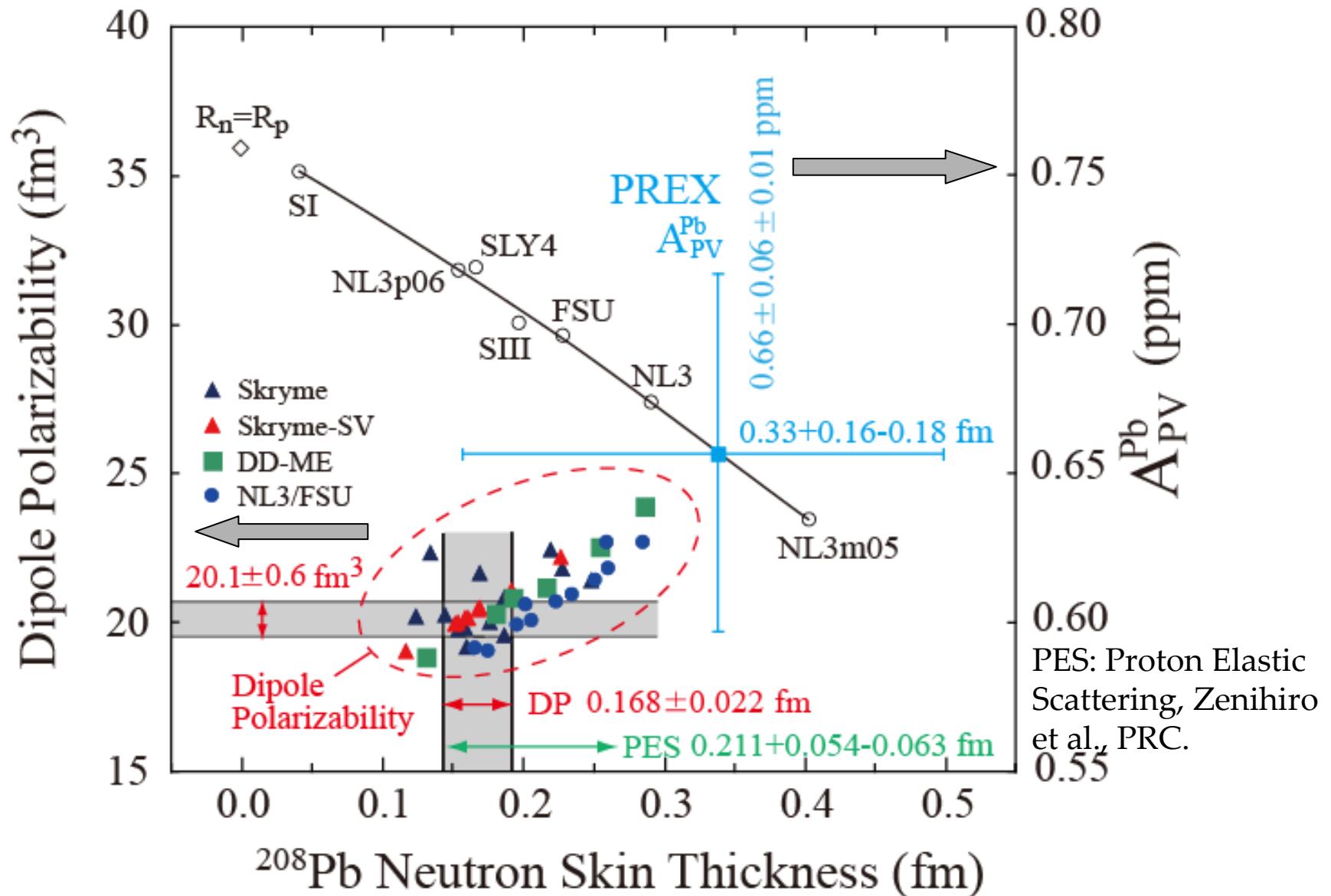


# Correlation Between Dipole Polarizability and Neutron Skin Thickness

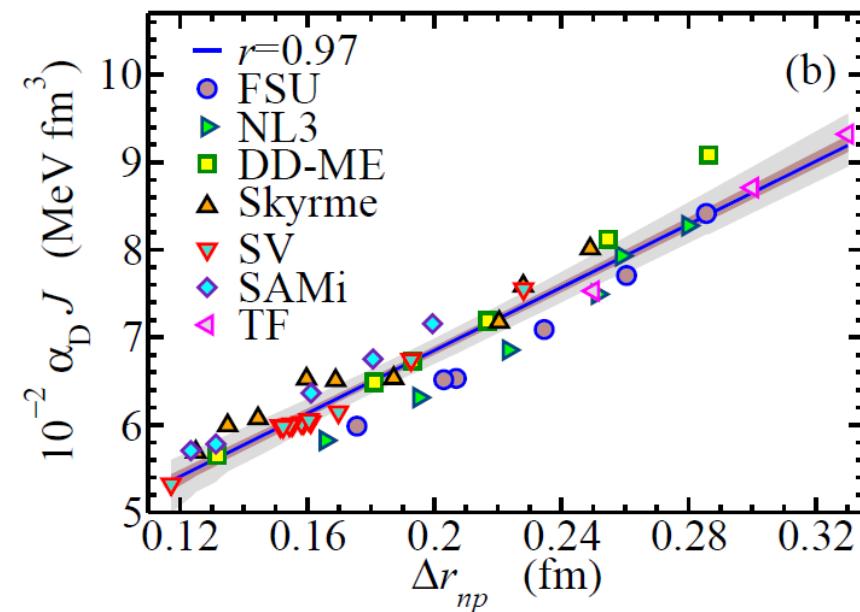
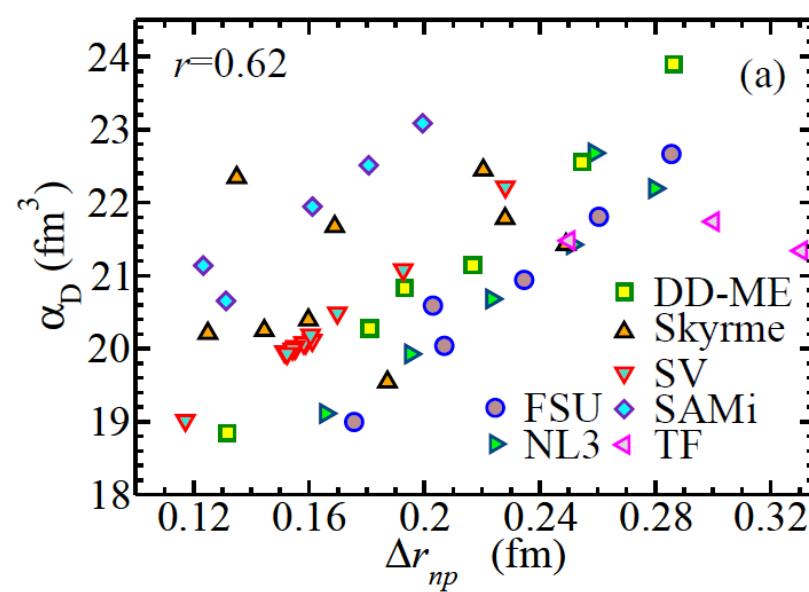


$(0.168 \pm 0.022)$  fm in <sup>208</sup>Pb

# Neutron Skin Thickness Measurement by Electromagnetic Interaction



X. Roca-Maza et al., arXiv:1307.4806



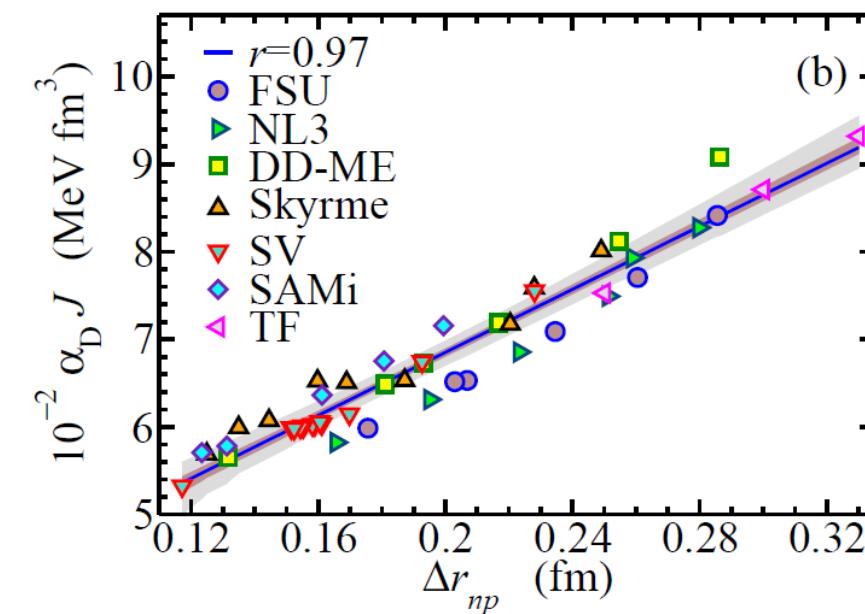
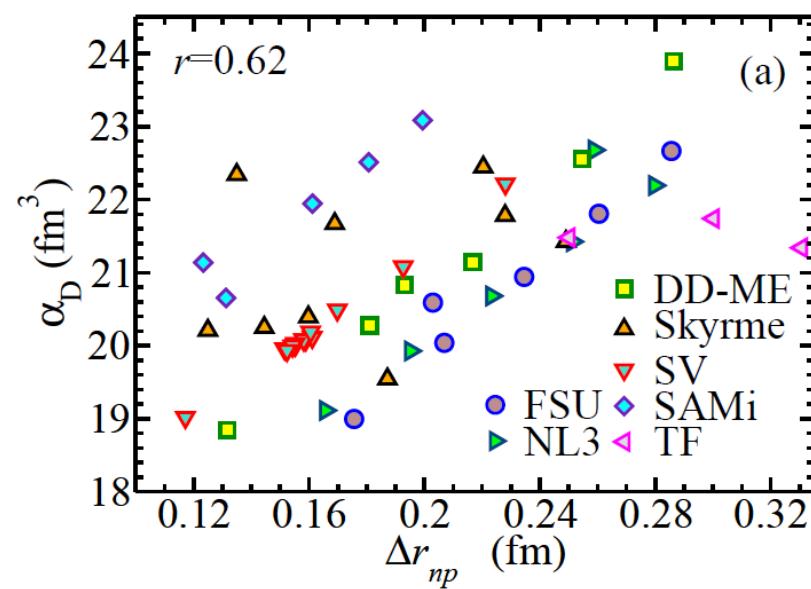
$$10^{-2} \alpha_D J = (3.25 \pm 0.14) + (17.99 \pm 0.70) \Delta r_{np}$$

$\alpha_D J$  is a strong isovector indicator.

Insights from the droplet model  $\alpha_D^{\text{DM}} \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[ 1 + \frac{5}{3} \frac{L}{J} \epsilon_A \right]$

Talk by X. Roca-Maza (next session)

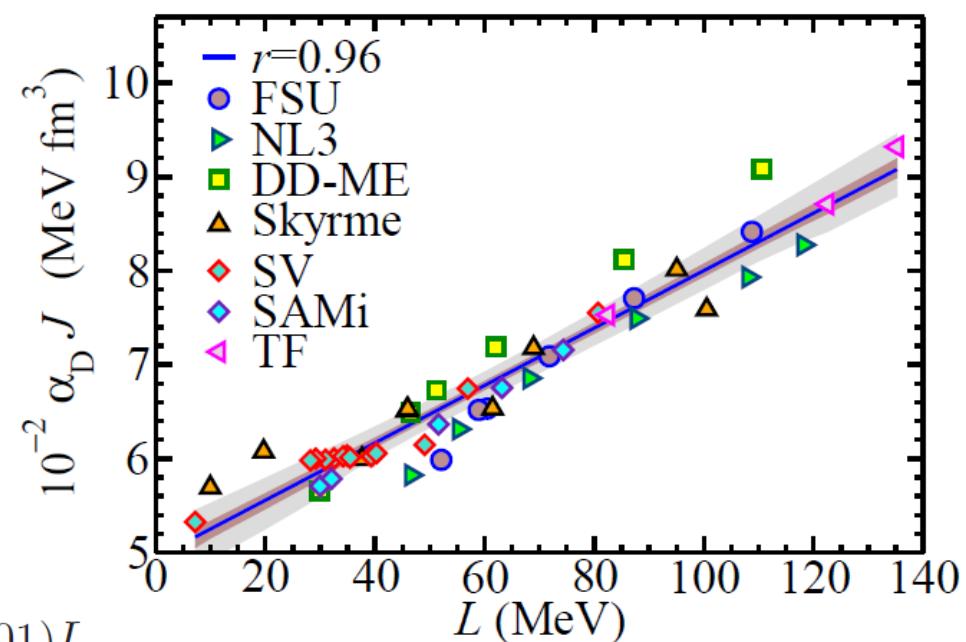
X. Roca-Maza et al., arXiv:1307.4806



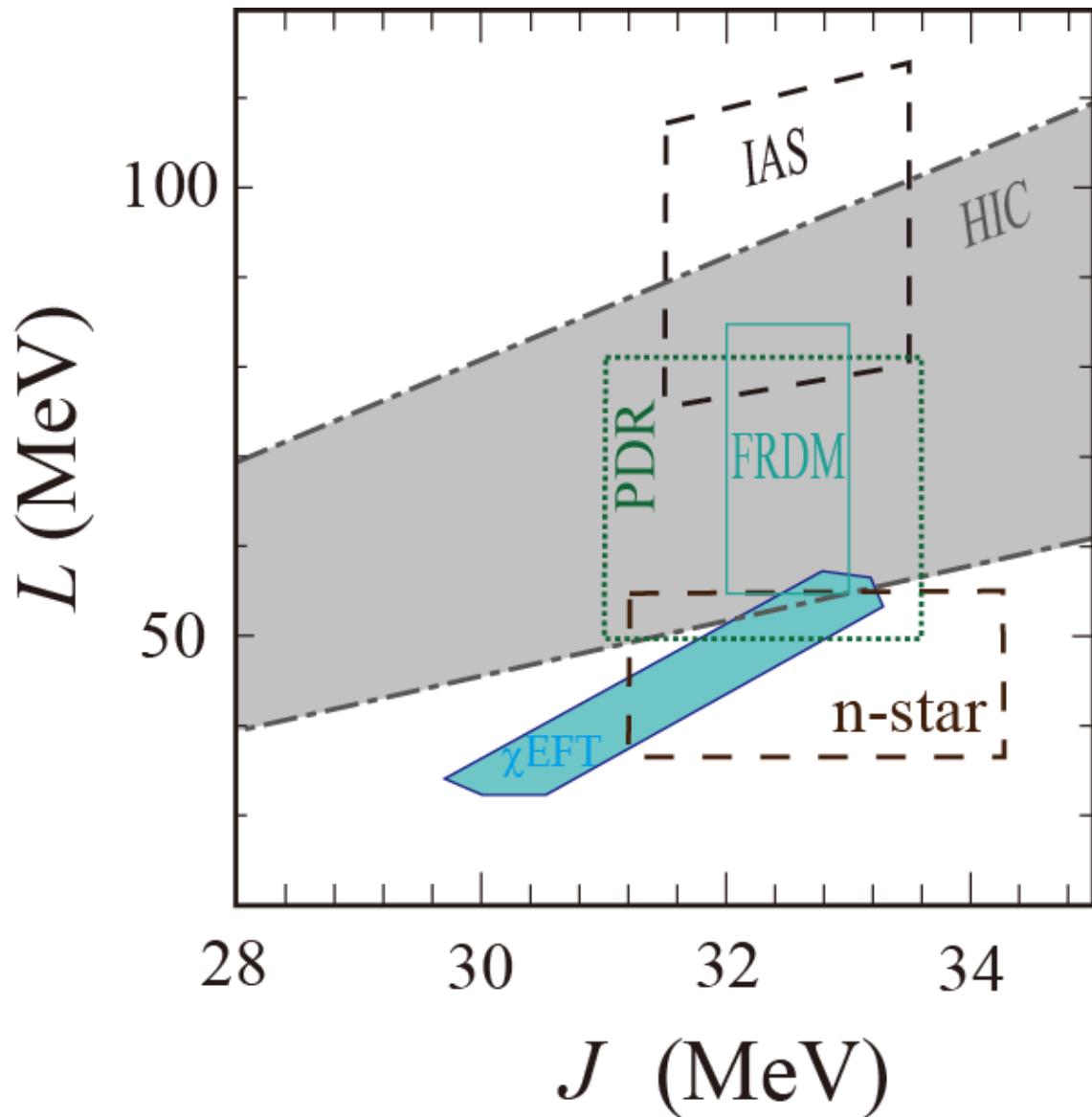
It would be better to use the correlation between  $\alpha_D J$  and L (or  $\Delta_{np}$ ) than use the correlation between  $\alpha_D$  and L (or  $\Delta_{np}$ ) to extract constraints.

We have used the correlation between  $\alpha_D J$  and L (gray band in the right figure) to extract a constraint band in the J-L plane.

$$10^{-2} \alpha_D J = (4.94 \pm 0.09) + (0.031 \pm 0.001)L$$



# Constraints on J and L

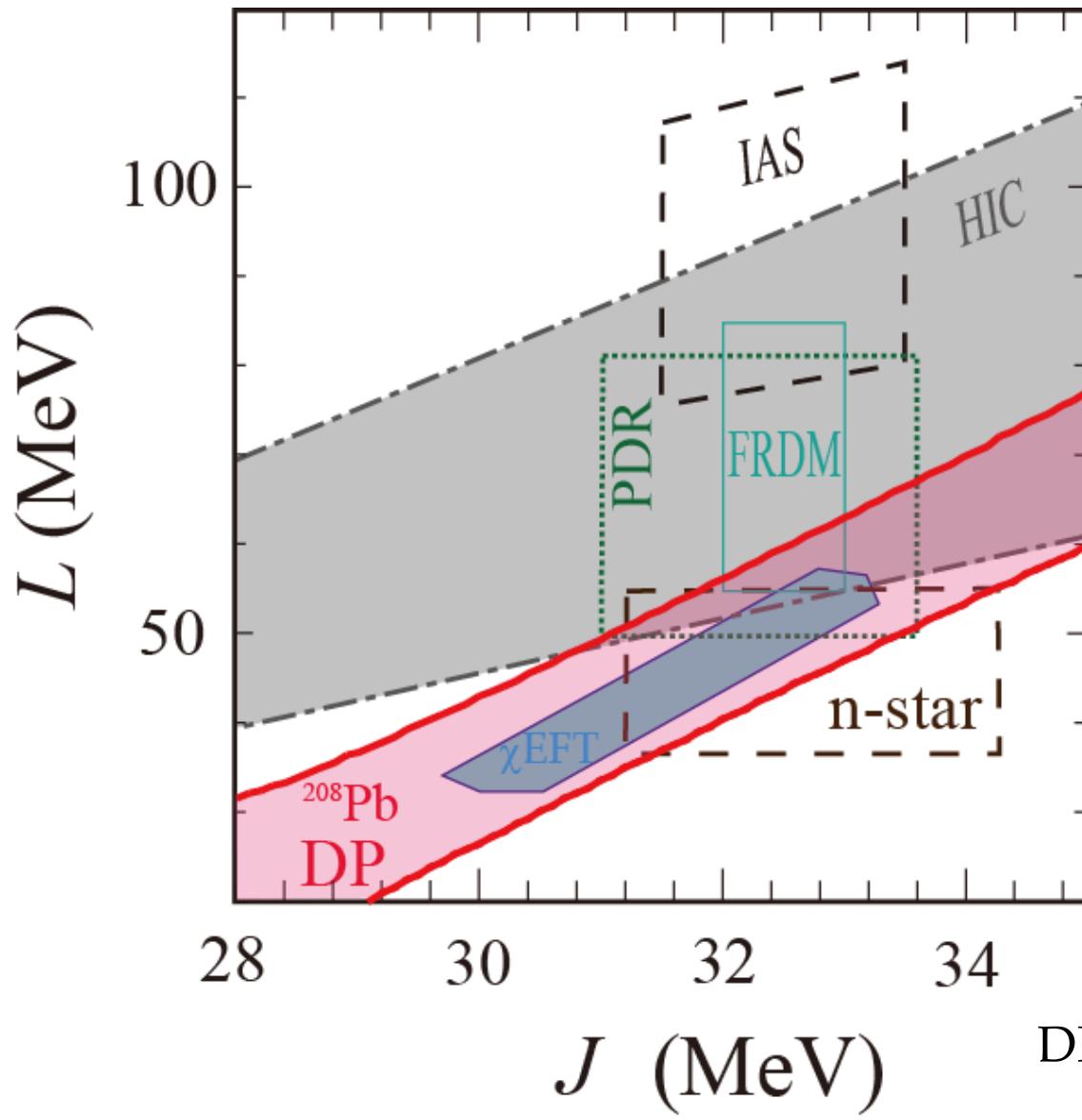


M.B. Tsang *et al.*,  
PRC86, 015803 (2012).

I. Tews *et al.*, PRL110,  
032504 (2013)

DP: Dipole Polarizability  
 HIC: Heavy Ion Collision  
 PDR: Pygmy Dipole Resonance  
 IAS: Isobaric Analogue State  
 FRDM: Finite Range Droplet Model (nuclear mass analysis)  
 n-star: Neutron Star Observation  
 $\chi$ EFT: Chiral Effective Field Theory

# Constraints on J and L



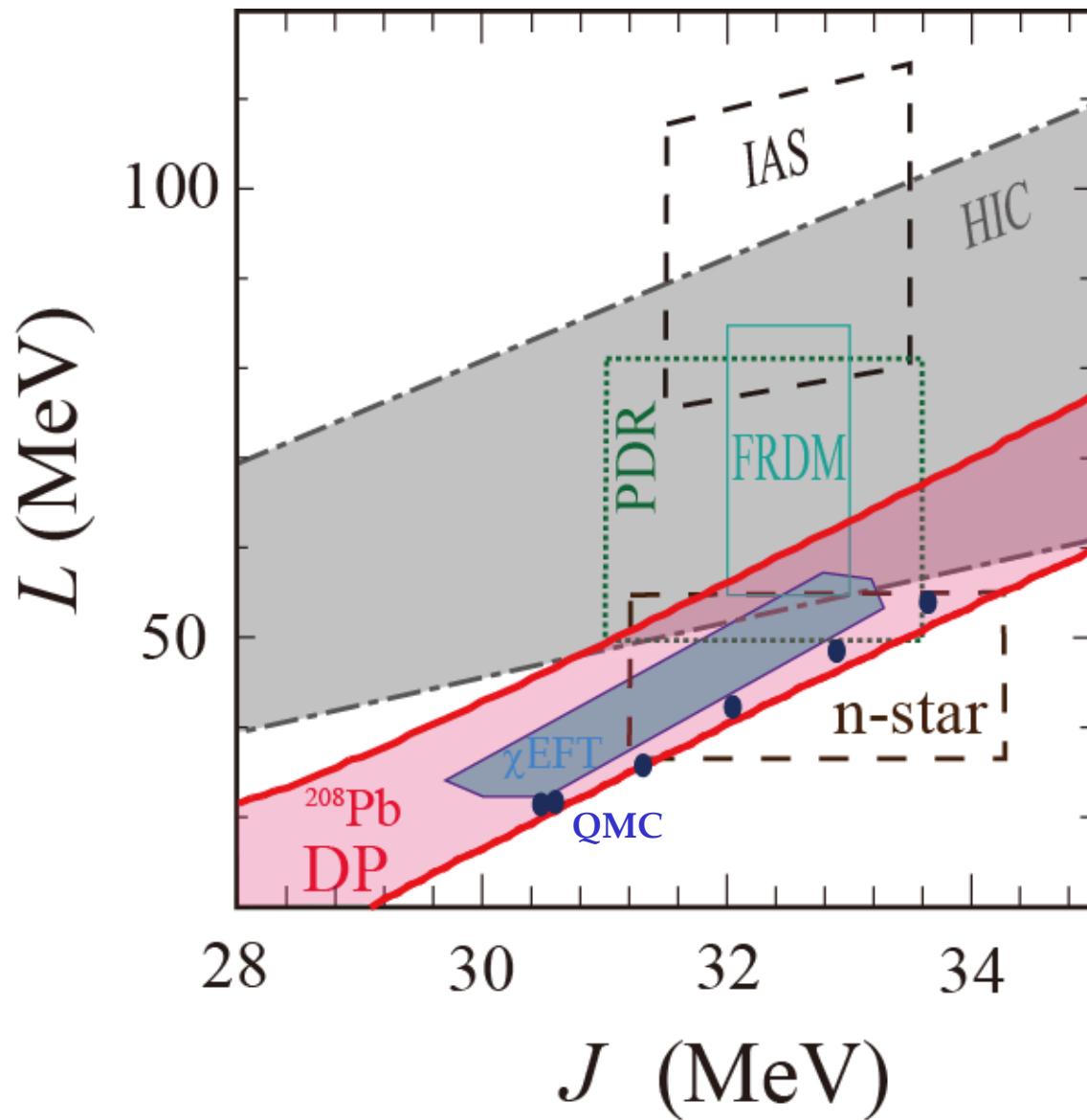
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DP:  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3$   
 + theoretical uncertainty

# Constraints on J and L



M.B. Tsang *et al.*,  
PRC86, 015803 (2012).

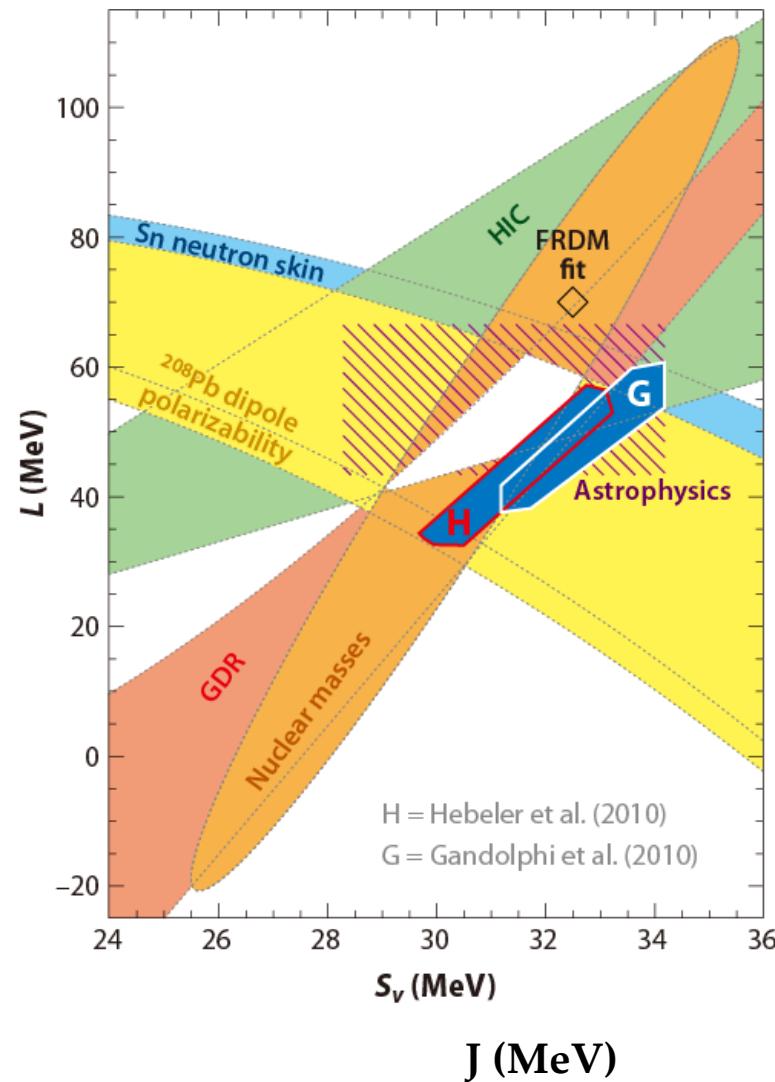
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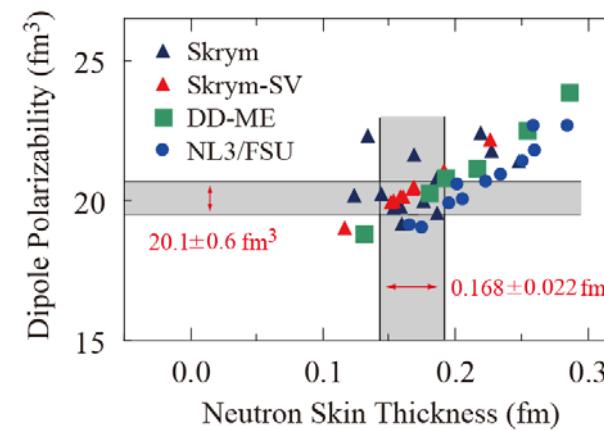
QMC by S. Gandolfi *et al.*,  
talk on Tuesday

# A short note

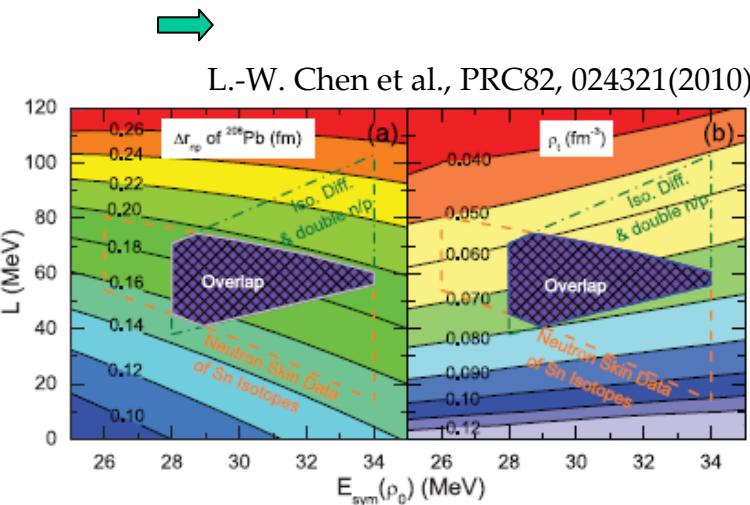
J. Lattimer Ann. Rev. Nucl. Part. Sci. 62, 485 (2012): talk on Tuesday



different correlation from the two-step evaluation



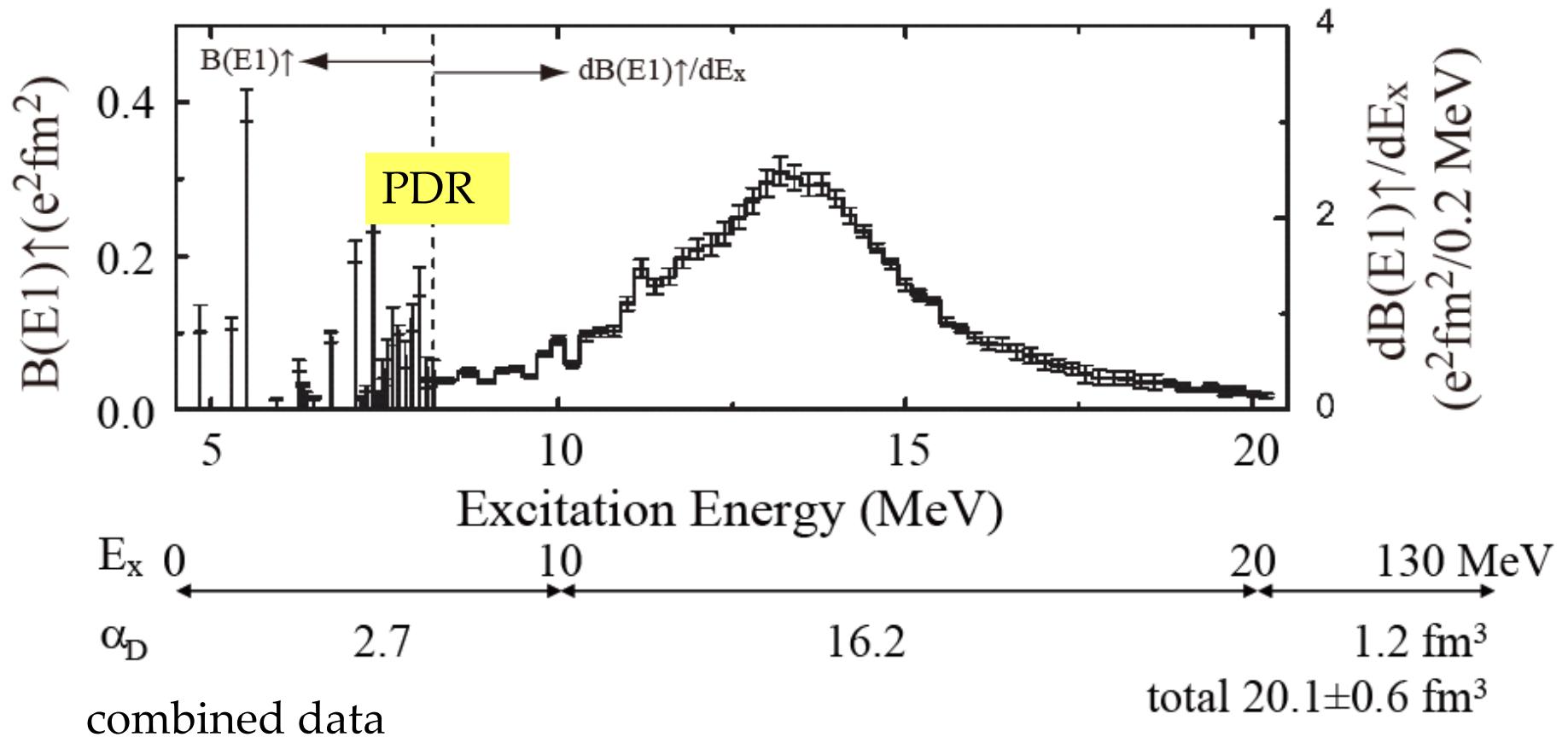
$^{208}\text{Pb}$  Dipole Polarizability  
 $^{208}\text{Pb}$  neutron skin thickness



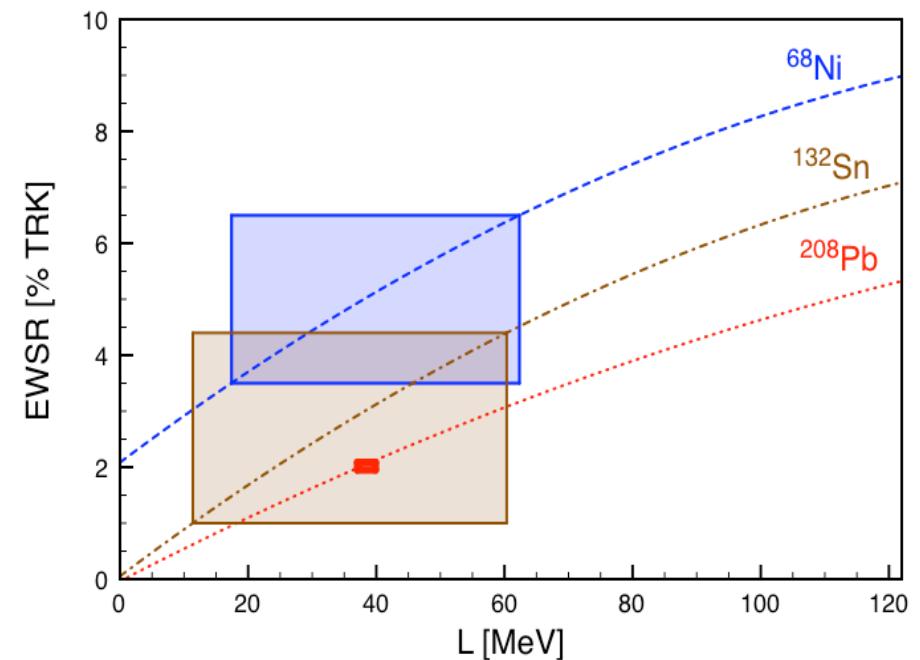
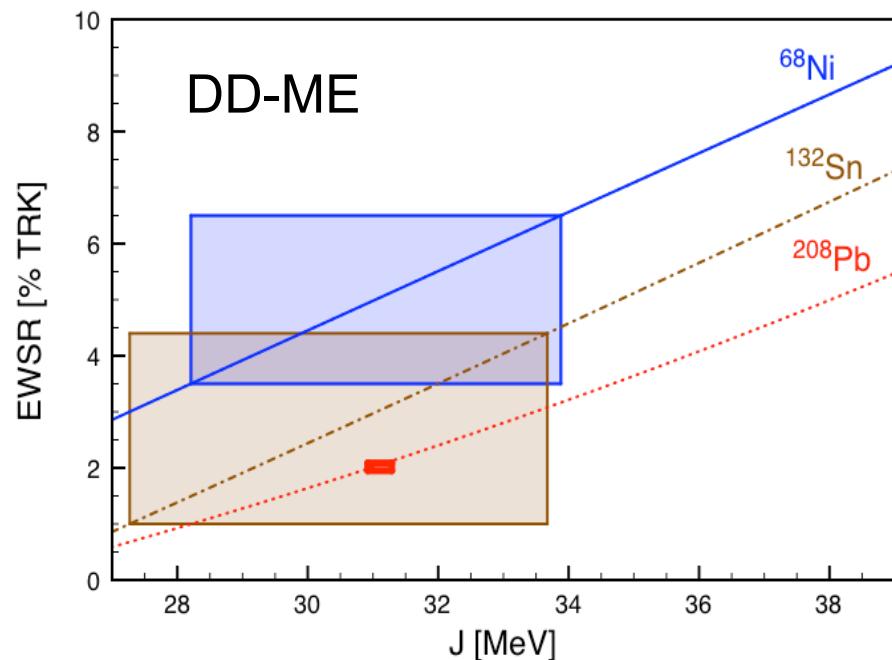
$^{208}\text{Pb}$  neutron skin thickness  
→ Constraints on the L-J plane

# PDR strength

## E1 Response of $^{208}\text{Pb}$ and $\alpha_D$



- Theoretical dependences of pygmy EWSR on  $J$  and  $L$  are determined using relativistic energy density functionals spanning the range of  $J$  and  $L$  values. Available experimental data provide constraints on theoretical models.



Similar approach but different theory → A. Carbone et al, PRC 81, 041301(R) (2010)

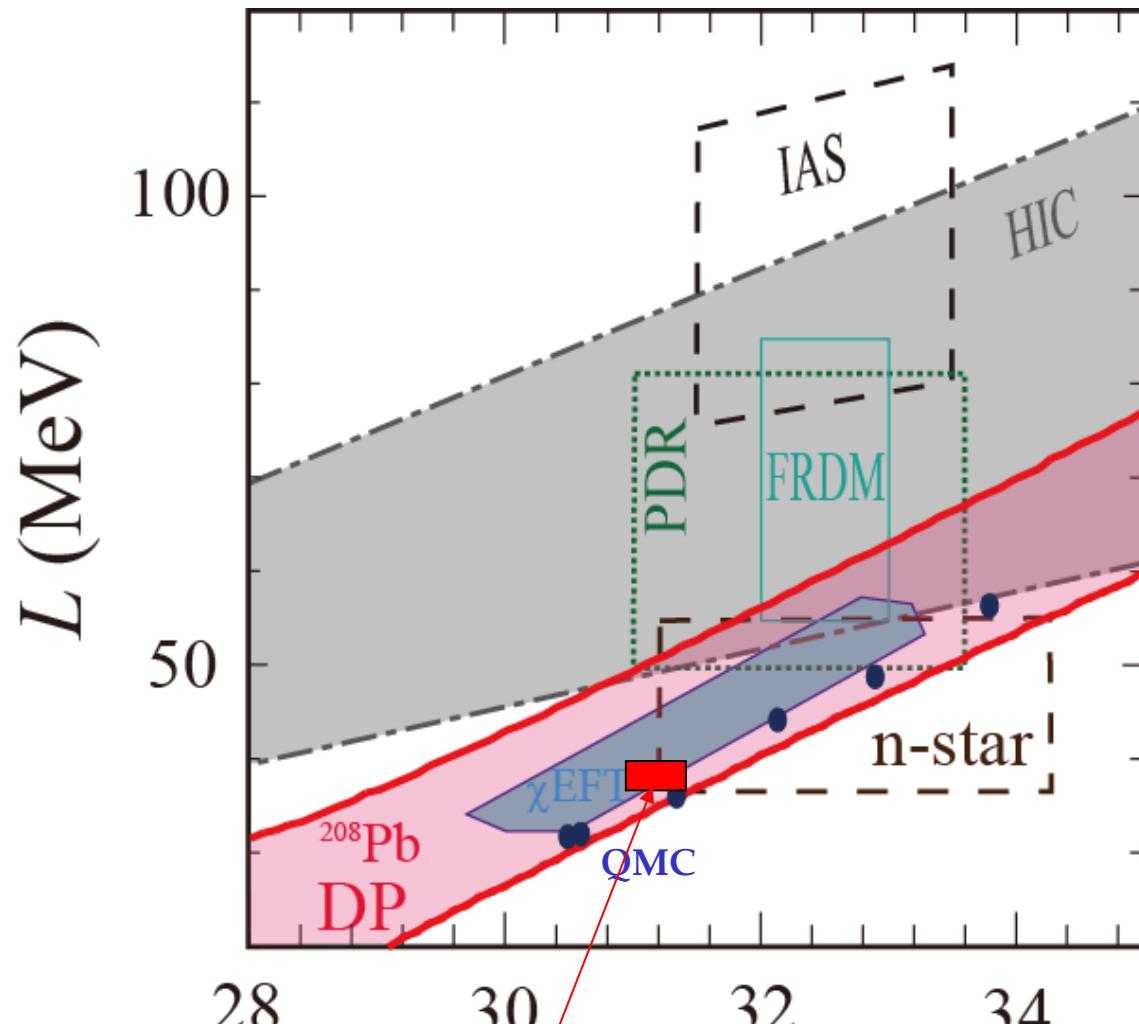
Exp. Data:  $^{68}\text{Ni}$  : O. Wieland et al, PRL 102, 092502 (2009)

$^{132,130}\text{Sn}$ : A. Klimkiewicz et al., PRC 76, 051603 (R) (2007)

$^{208}\text{Pb}$ : I. Poltoratska et al., PRC 85, 041304 (R) (2012)

Courtesy of N. Paar

# Determination of Symmetry Energy



$^{208}\text{Pb}$  PDR EWSR Analysis  
with DD-ME by N. Paar

We should take care of the model uncertainty.

M.B. Tsang *et al.*,  
PRC86, 015803 (2012).

I. Tews *et al.*, PRL110,  
032504 (2013)

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# Summary

NuSym13, July 22-26, 2013 at NSCL

- The electric dipole response of  $^{208}\text{Pb}$  has been precisely measured by using proton inelastic scattering as an electromagnetic probe.  
as  $\alpha_D = 20.1 \pm 0.6 \text{ fm}^3/\text{e}^2$
- Constraints on the symmetry energy parameters have been extracted with a help of theoretical calculations.
- A lot of data under analysis:
  - $^{96}\text{Mo}$  (DCS and PT): D. Martin
  - $^{48}\text{Ca}$  (DCS): J. Birkhan
  - $^{90}\text{Zr}$  (DCS): C. Iwamoto (PDR-region, published in PRL **108**, 262501 (2012))
  - $^{120}\text{Sn}$  (DCS and PT): A.M. Krumbholtz, T. Hashimoto
  - $^{154}\text{Sm}$  (DCS and PT): A. Krugmann
  - $^{88}\text{Sr}, ^{92}\text{Mo}$  (DCS): C. Iwamoto
  - $^{70}\text{Zn}$  (DCS):

## Collaborators

RCNP-E282

*RCNP, Osaka University*

NuSym13, July 22-26, 2013 at NSCL

A. Tamii, H. Fujita, Y. Fujita, K. Hatanaka,  
H. Sakaguchi Y. Tameshige and M. Yosoi

*IKP, TU-Darmstadt*

P. von Neumann-Cosel, A-M. Heilmann,  
Y. Kalmykov, I. Poltoratska, V.Yu. Ponomarev,  
A. Richter and J. Wambach

*RIKEN*

H. Matsubara and J. Zenihiro

*Dep. of Phys., Kyoto University*  
T. Kawabata

*KVI, Univ. of Groningen*

T. Adachi and L.A. Popescu

*IFIC-CSIC, Univ. of Valencia*

B. Rubio and A.B. Perez-Cerdan

*Sch. of Science Univ. of Witwatersrand*

J. Carter and H. Fujita

*iThemba LABS*

F.D. Smit

*Texas A&M Commerce*

C.A. Bertulani

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E. Litvinova

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K. Nakanishi,  
Y. Shimizu and Y. Sasamoto

*CYRIC, Tohoku University*

M. Itoh and Y. Sakemi

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M. Dozono

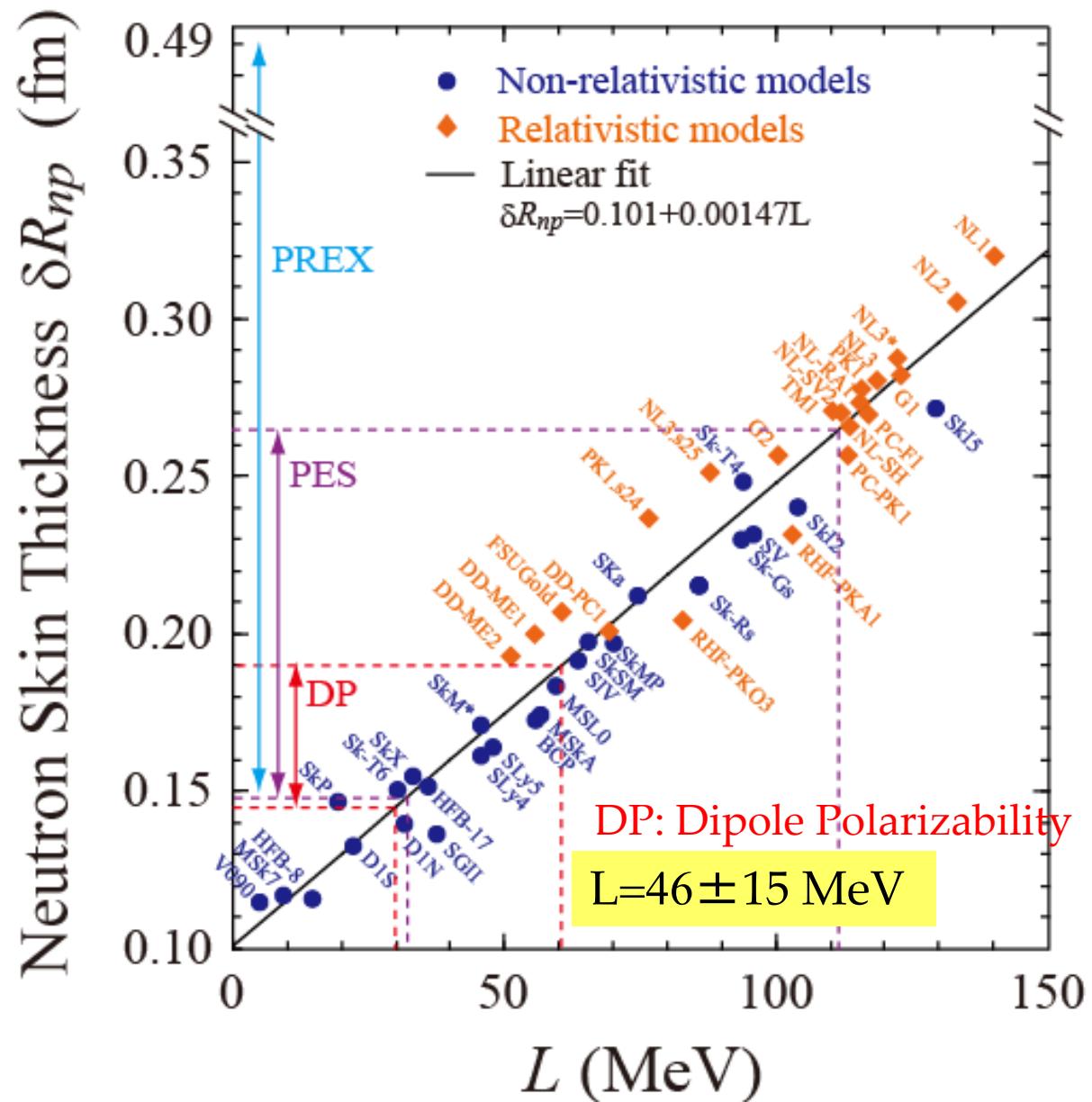
*Dep. of Phys., Niigata University*

Y. Shimbara

# *Thank You*

Special thanks to:

X. Roca-Maza, J. Piekarewicz, W. Nazarewicz,  
and N. Paar



Based on the work by X. Roca-Maza *et al.*, PRL106, 252501 (2011)

# Medium modification of RLF $NN$ interaction

## Medium effect

$$g_j^2 \rightarrow g_j^{*2} \equiv \frac{g_j^2}{1 + a_j \rho(r) / \rho_0},$$

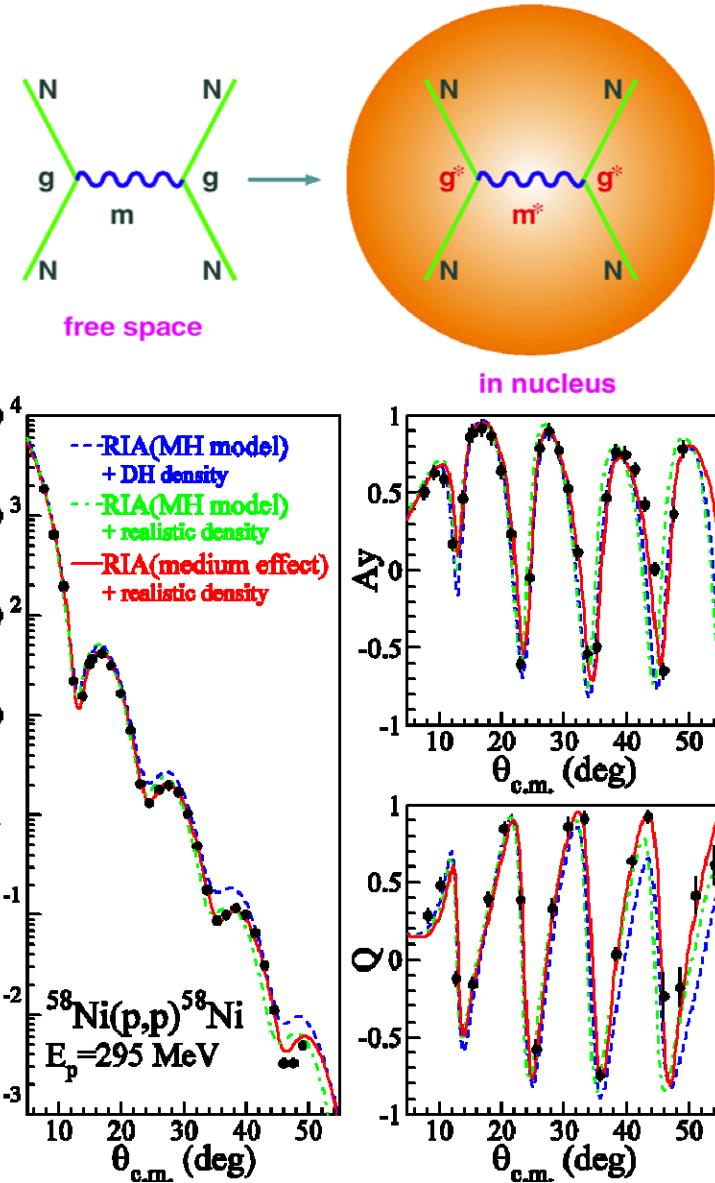
$$m_j \rightarrow m_j^* \equiv m_j \left(1 + b_j \rho(r) / \rho_0\right)$$

$$j = \sigma, \omega.$$

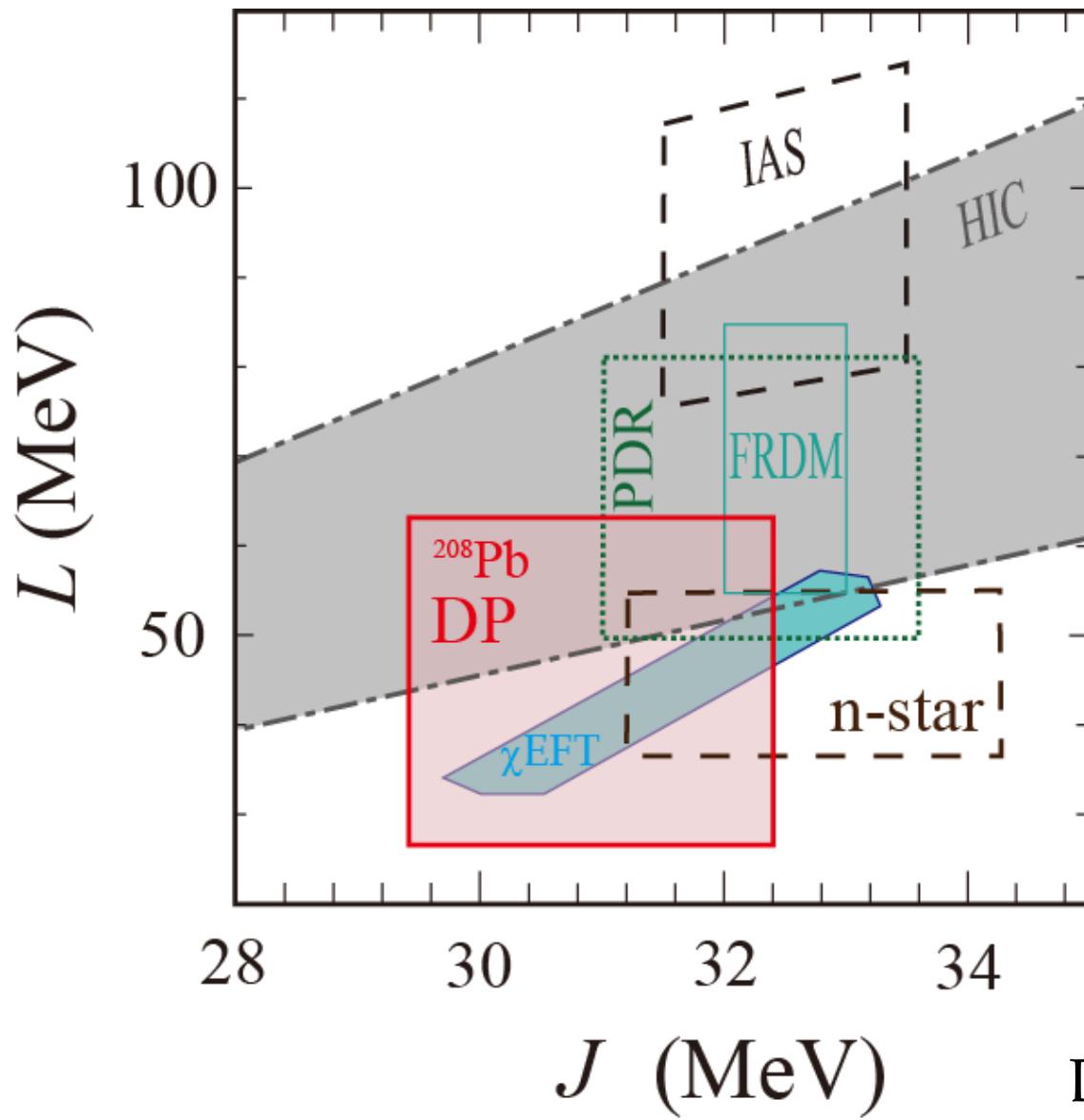
- Phenomenological parameters;  $a_j, b_j$
- Universal form of density-dependent terms
- At  $\rho=0$ , same as free  $NN$  interaction

Need to calibrate with real data

H. Sakaguchi et al., PRC57, 1749.



# Determination of Symmetry Energy



M.B. Tsang *et al.*,  
PRC86, 015803 (2012).

I. Tews *et al.*, PRL110,  
032504 (2013)

and this work

DP: Dipole Polarizability  
 HIC: Heavy Ion Collision  
 PDR: Pygmy Dipole Resonance  
 IAS: Isobaric Analogue State  
 FRDM: Finite Range Droplet Model (nuclear mass analysis)  
 n-star: Neutron Star Observation  
 $\chi\text{EFT}$ : Chiral Effective Field Theory

DP:  $L=45 \pm 18 \text{ MeV}$   
 $J=30.9 \pm 1.5 \text{ MeV}$

$$10^{-2}\alpha_D J = (4.94 \pm 0.09) + (0.031 \pm 0.001)L$$

$$L = -145 \pm (9)_{\text{theo.}} + [6.07 \pm (0.18)_{\text{exp.}} \pm (0.26)_{\text{theo.}}]J,$$

$$\Delta r_{np} = 0.168 \pm (0.009)_{\text{exp.}} \pm (0.019)_{\text{theo.}} \pm (0.021)_{\text{est.}} \text{fm}$$