

# Determination of ${}^8\text{B}(p,\gamma){}^9\text{C}$ Reaction Rate from ${}^9\text{C}$ Breakup

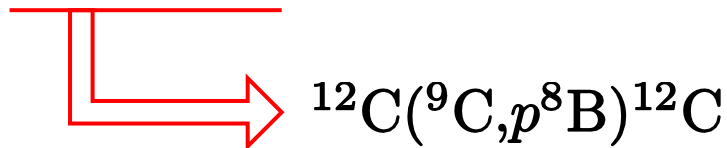
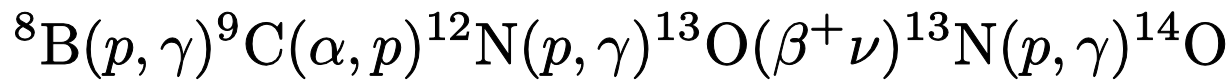
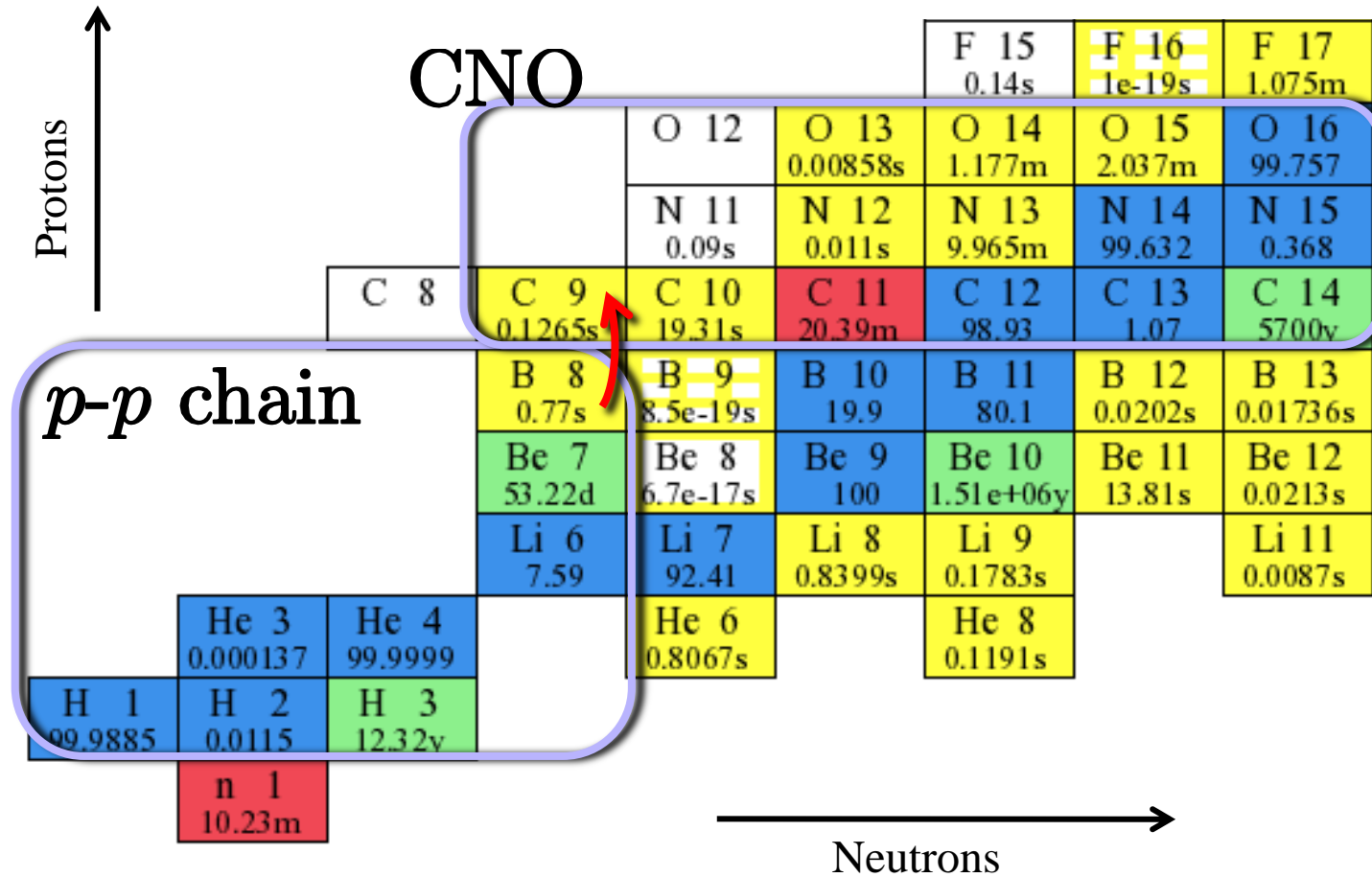
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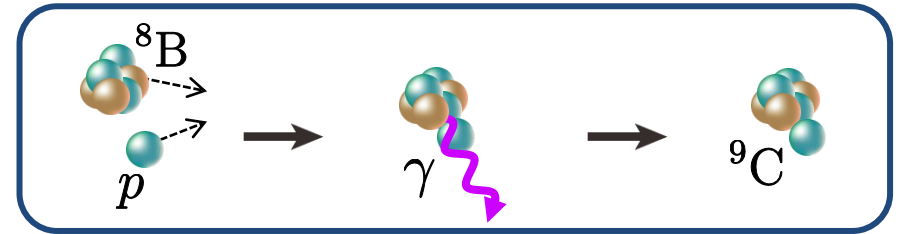
# Introduction

# Why ${}^8\text{B}(p,\gamma){}^9\text{C}$ ?



E $\lambda$  transition cross section

$$\sigma_{E\lambda} \propto \left| \left\langle I(\mathbf{r}) \left| \hat{O}_{E\lambda}(\mathbf{r}) \right| \psi_{pB}(\mathbf{r}) \right\rangle \right|^2$$

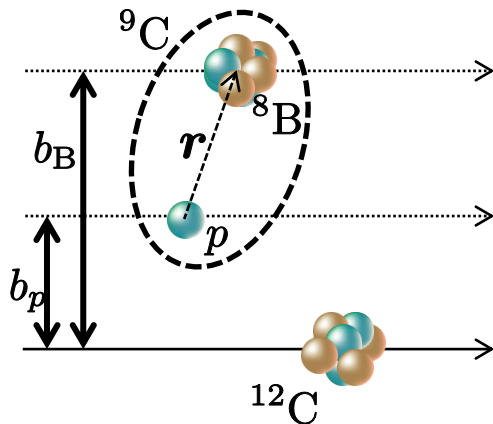


Overlap function

$$I(\mathbf{r}) \equiv \langle \phi_C(\mathbf{r}, \xi_p, \xi_B) | \phi_p(\xi_p) \phi_B(\xi_B) \rangle, \quad I(r) \xrightarrow{r \gg r_N} \frac{CW(r)}{r}$$

Determine the  $C$   
from Breakup reaction:  $^{12}\text{C}(^9\text{C}, p)^8\text{B}$

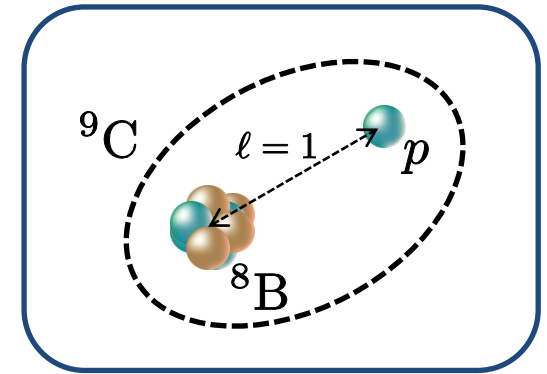
**Peripheral Reaction !!**



- If  $b_p$  is large, there will be no Breakup because of the short-range property of Nuclear interaction.
- If  $b_B$  is small, there will be no Breakup because of the absorption.

## Ground state wave function

$$\phi_C^{\text{g.s.}}(\mathbf{r}) = \sum_{S=3/2,5/2} \frac{\varphi^{\text{g.s.}}(r)}{r} \left[ [\eta_{1/2} \otimes \Phi_2]_S \otimes Y_1(\hat{\mathbf{r}}) \right]_{3/2, J_z}$$

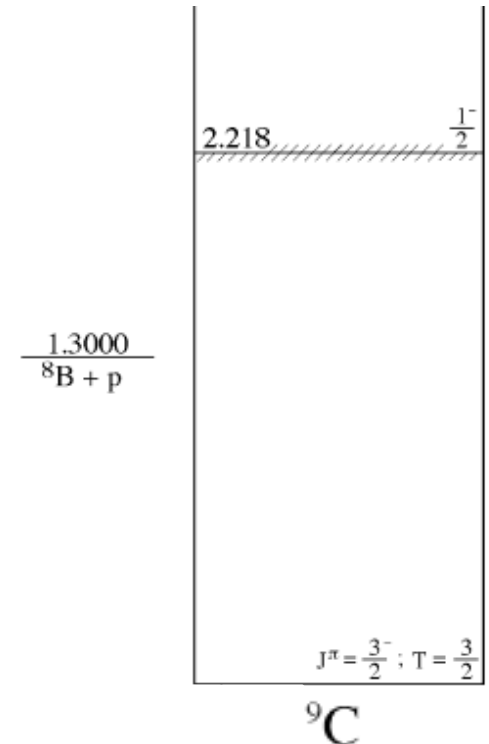


## Resonance state wave function

$$\phi_C^{\text{res}}(\mathbf{r}) = \frac{\varphi^{\text{res}}(r)}{r} \left[ [\eta_{1/2} \otimes \Phi_2]_{3/2} \otimes Y_1(\hat{\mathbf{r}}) \right]_{1/2, J_z}$$

↓  
S conservation  
 ↓

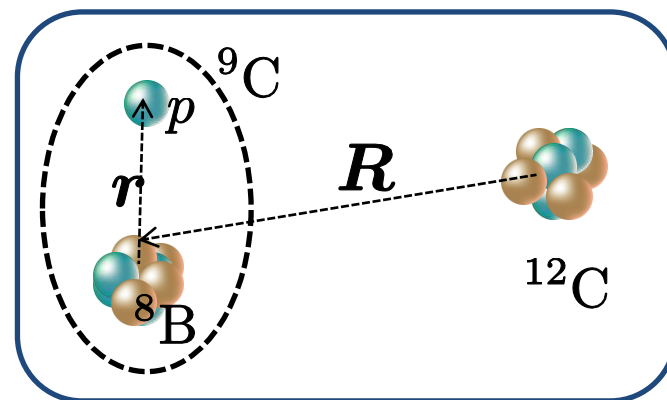
$$\sigma_{\text{BU}} = S_{\text{exp}}^{(3/2)} \sigma_{\text{BU}}^{(3/2)} + S_{\text{exp}}^{(5/2)} \sigma_{\text{BU}}^{(5/2)}$$



3-body Schrödinger eq.

$$(H_{3b} - E)\Psi(\mathbf{r}, \mathbf{R}) = 0$$

$$H_{3b} = T_r + V_{pB} + T_R + U_{pC} + U_{BC}$$

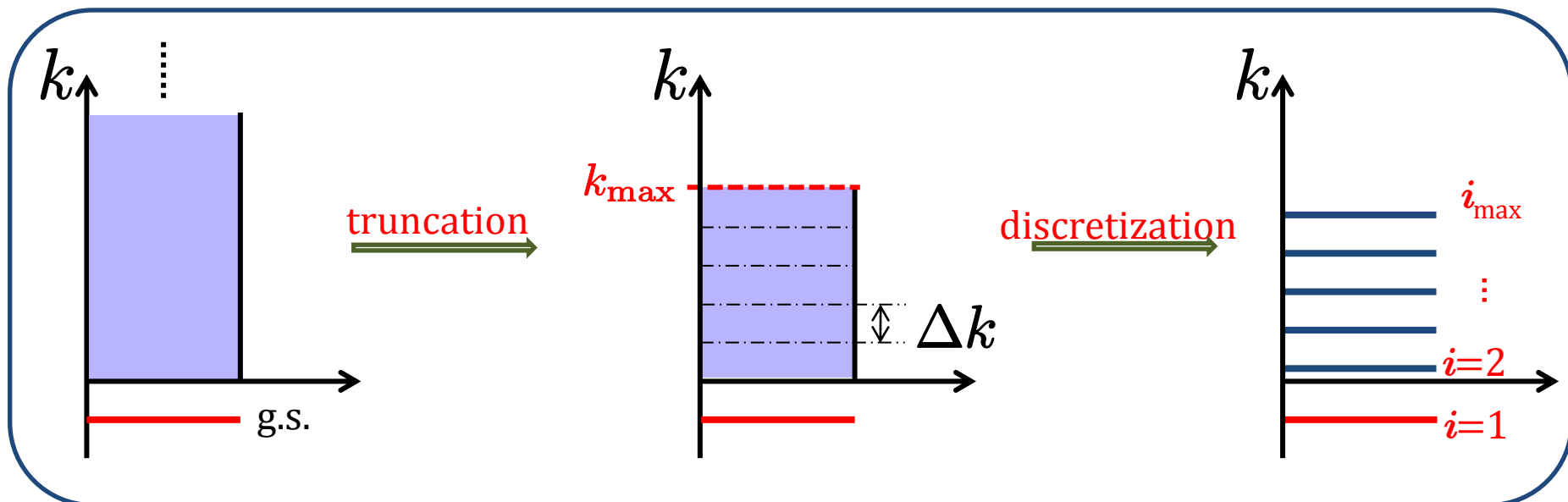


CDCC wave function

$$\Psi(\mathbf{r}, \mathbf{R}) = \phi_0\chi_0 + \int_0^\infty \phi_k\chi_k dk$$

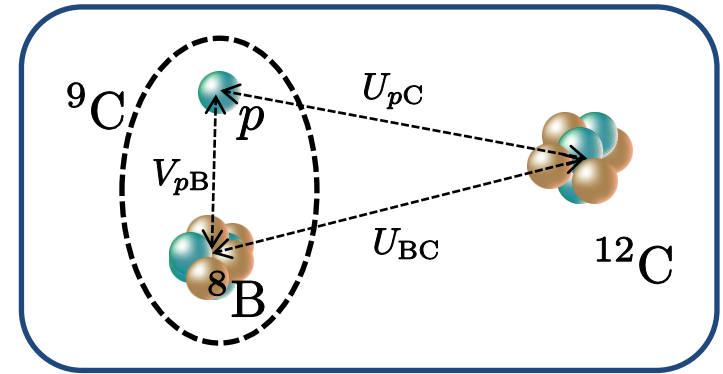


$$\Psi^{\text{CDCC}}(\mathbf{r}, \mathbf{R}) = \sum_i^{i_{\max}} \hat{\phi}_i \hat{\chi}_i$$



${}^9\text{C}$

- $s, p, d, f$  - waves
- $k_{\text{max}} = 0.6 \text{ [fm}^{-1}\text{]} (E_{\text{rel-max}} \sim 7.7 \text{ [MeV]})$
- $\Delta k = 0.05 \text{ [fm}^{-1}\text{]}$
- $V_{pB}$  : Woods-Saxon pot. reproducing B.E. (-1.3 MeV) & resonance



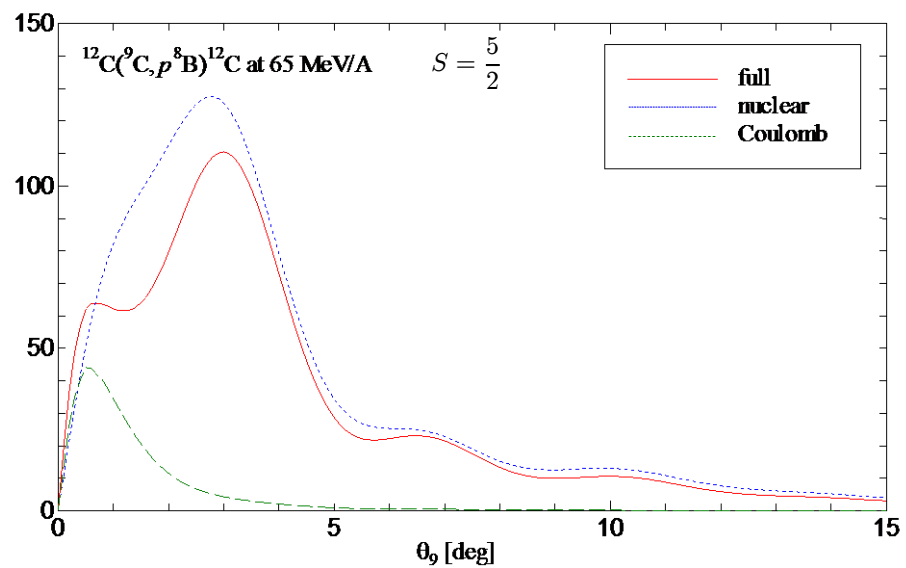
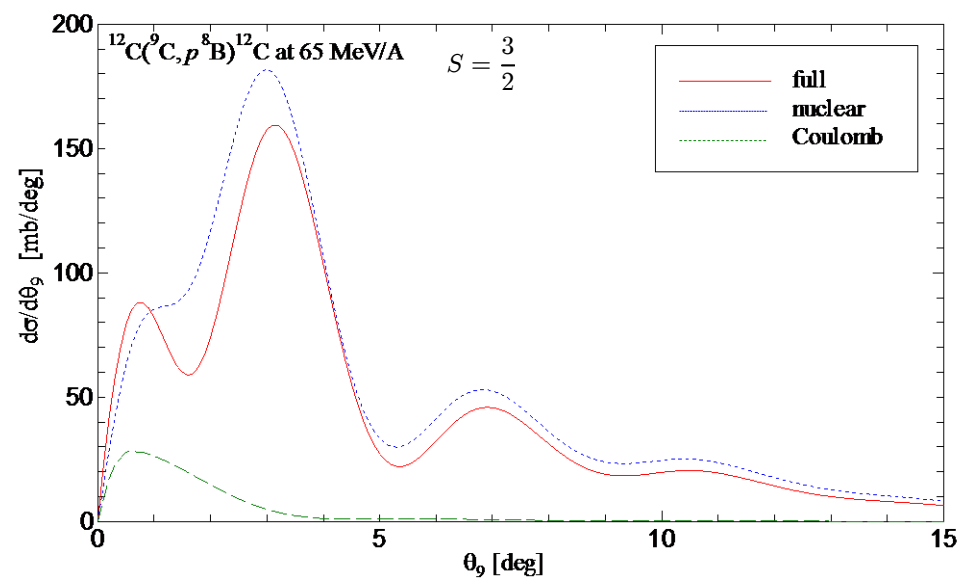
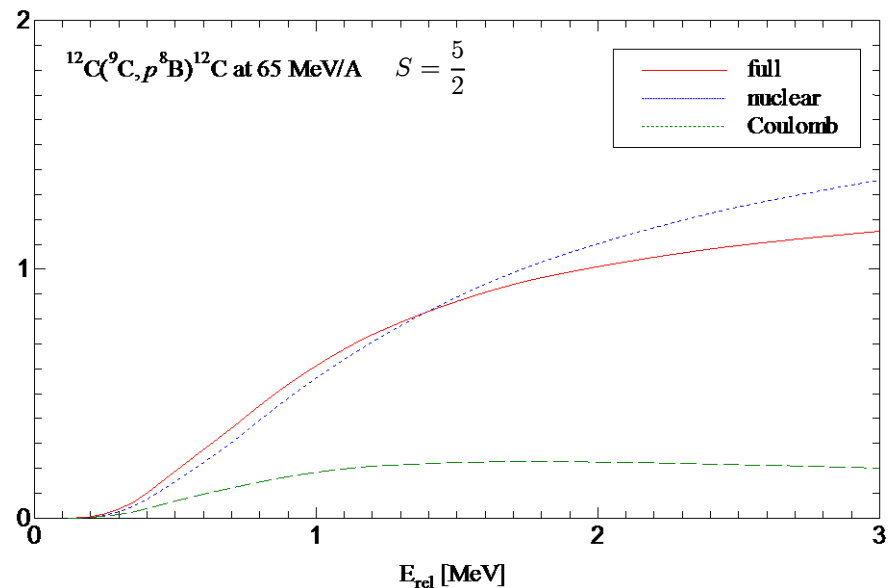
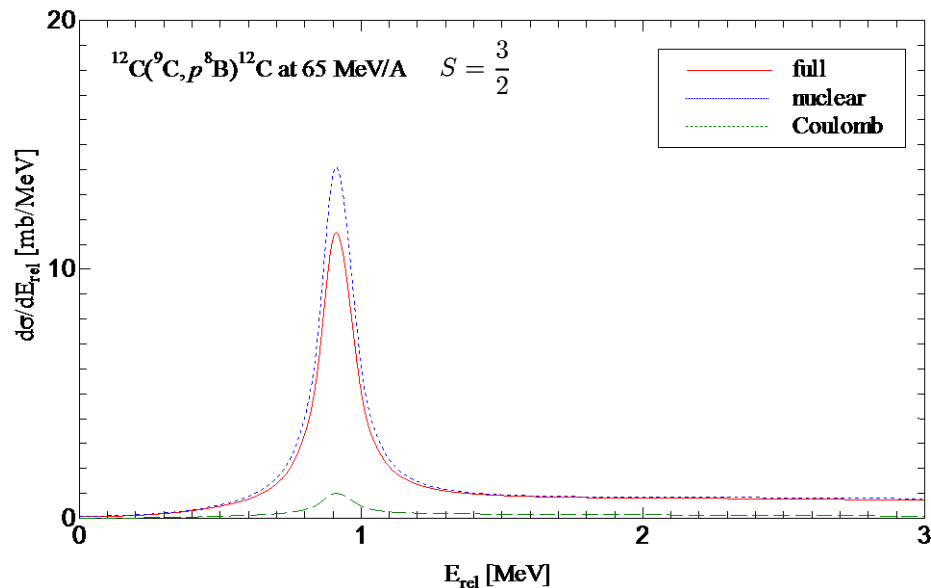
Distorting pot. : full microscopic folding model

- $$U_{pC} = \int \rho_C(\mathbf{r}_2) \sum_{i \in C} g_i d\mathbf{r}_2$$
- $$U_{BC} = \int \rho_B(\mathbf{r}_1) \rho_C(\mathbf{r}_2) \sum_{i \in B, j \in C} g_{ij} d\mathbf{r}_1 d\mathbf{r}_2$$

(  $NN$  interaction  $g_{ij}$  : Melbourne  $g$ -matrix  
 $\rho_B, \rho_C$  : Hartree-Fock calc. with Gogny D1S )

# Result

# Nuclear/Coulomb BU Effects



# Summary

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$^{12}\text{C}(^9\text{C},p^8\text{B})^{12}\text{C}$  at 65 MeV/A  
is analyzed by CDCC.

👉 Our CDCC calculation reproduces well the shape of breakup energy spectrum.

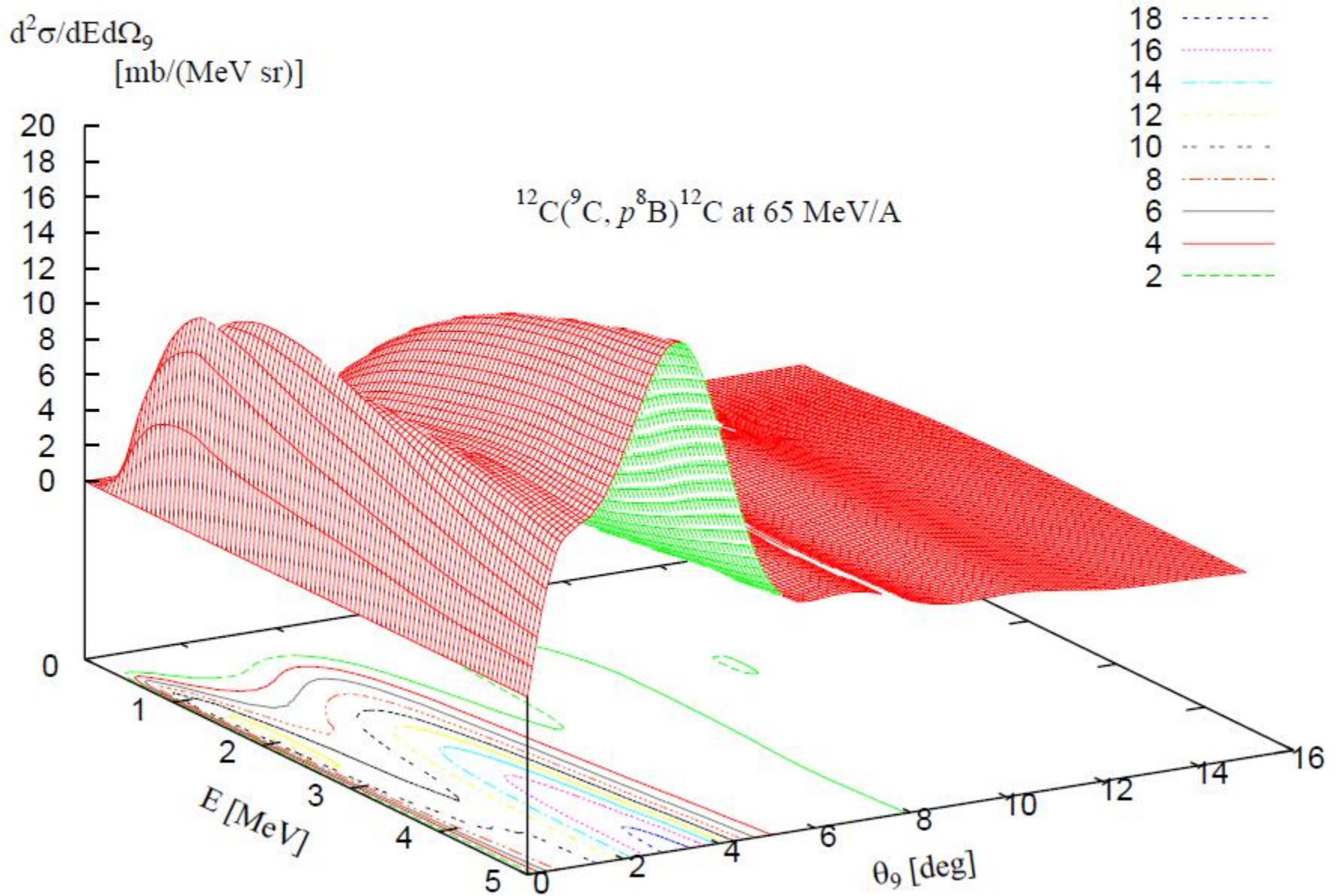
👉 ANC:  $(C_{3/2})^2 = 0.115$  [fm<sup>-1</sup>],  $(C_{5/2})^2 = 0.247$  [fm<sup>-1</sup>],  
 $S_{18} = 12 \pm 1$  [eV-b].

👉 There is strong interference between Nuclear & Coulomb breakup.



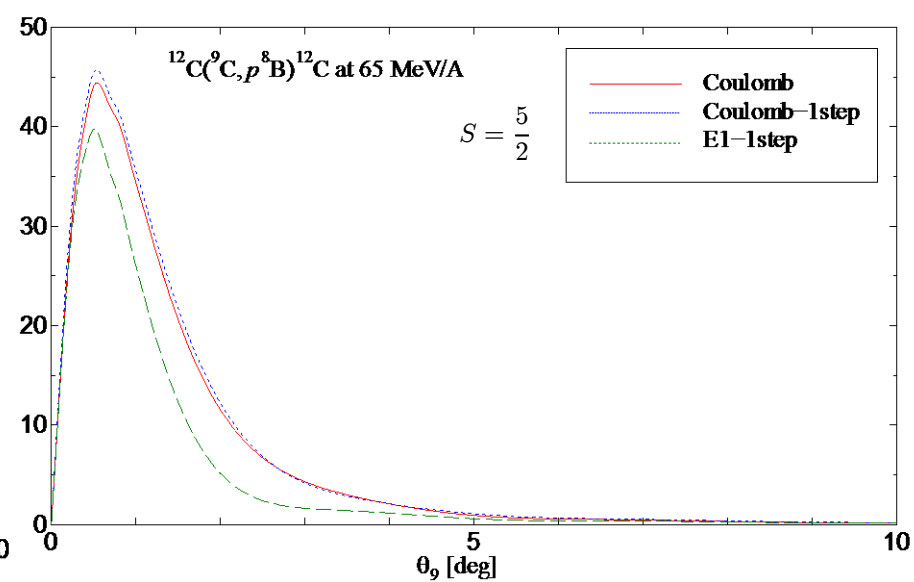
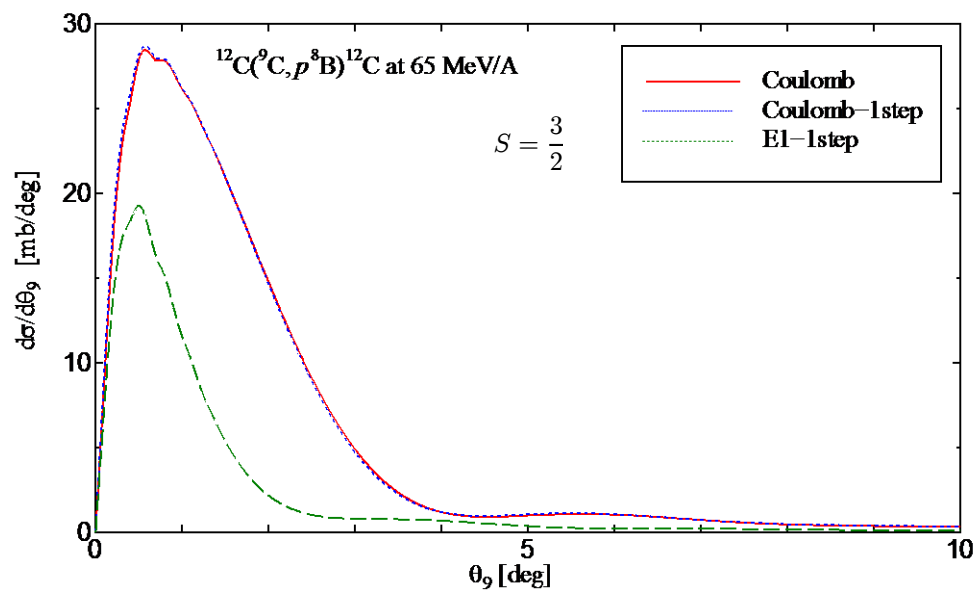
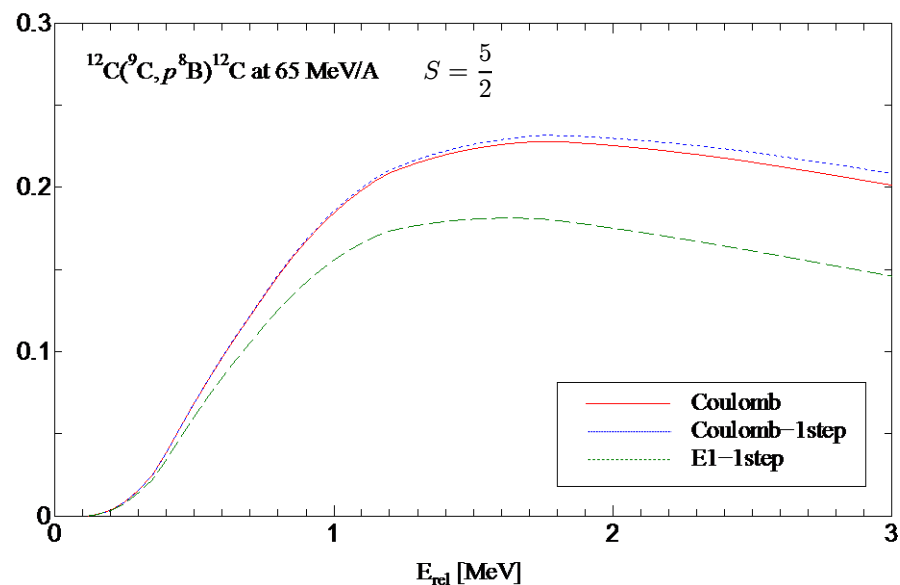
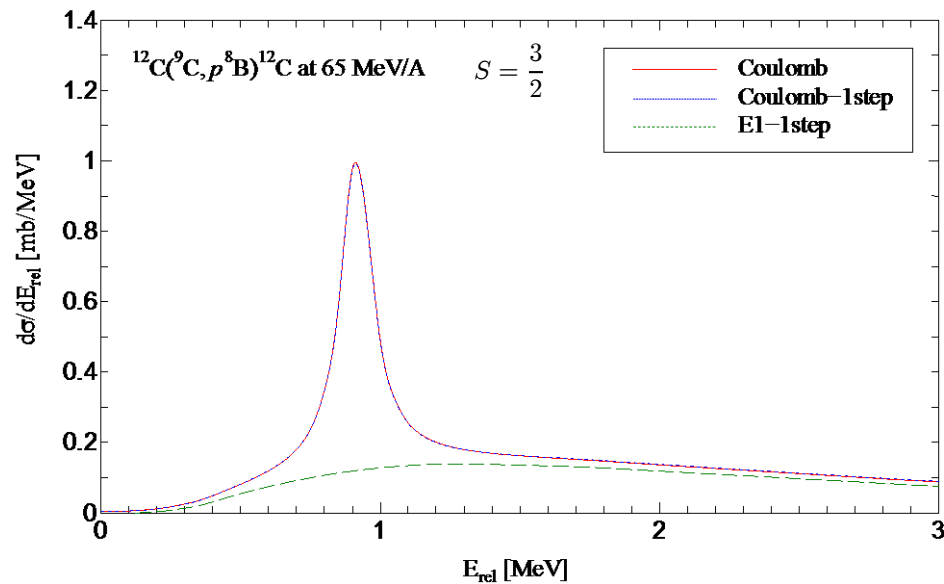
# Result

# Double Differential Cross Section



# Result

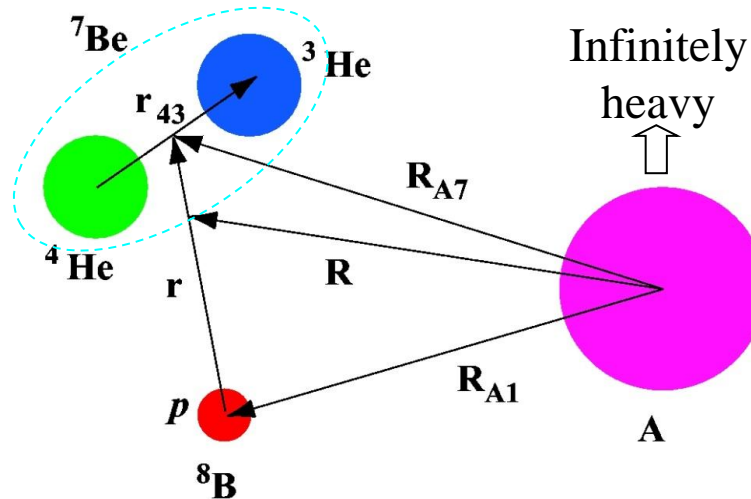
# Coulomb BU Multistep Effects



# Three “new” aspects of our $S_{17}$ paper

— KO, Hashimoto, Iseri, Kamimura, and Yahiro, *PRC73*, 024605 (2006).

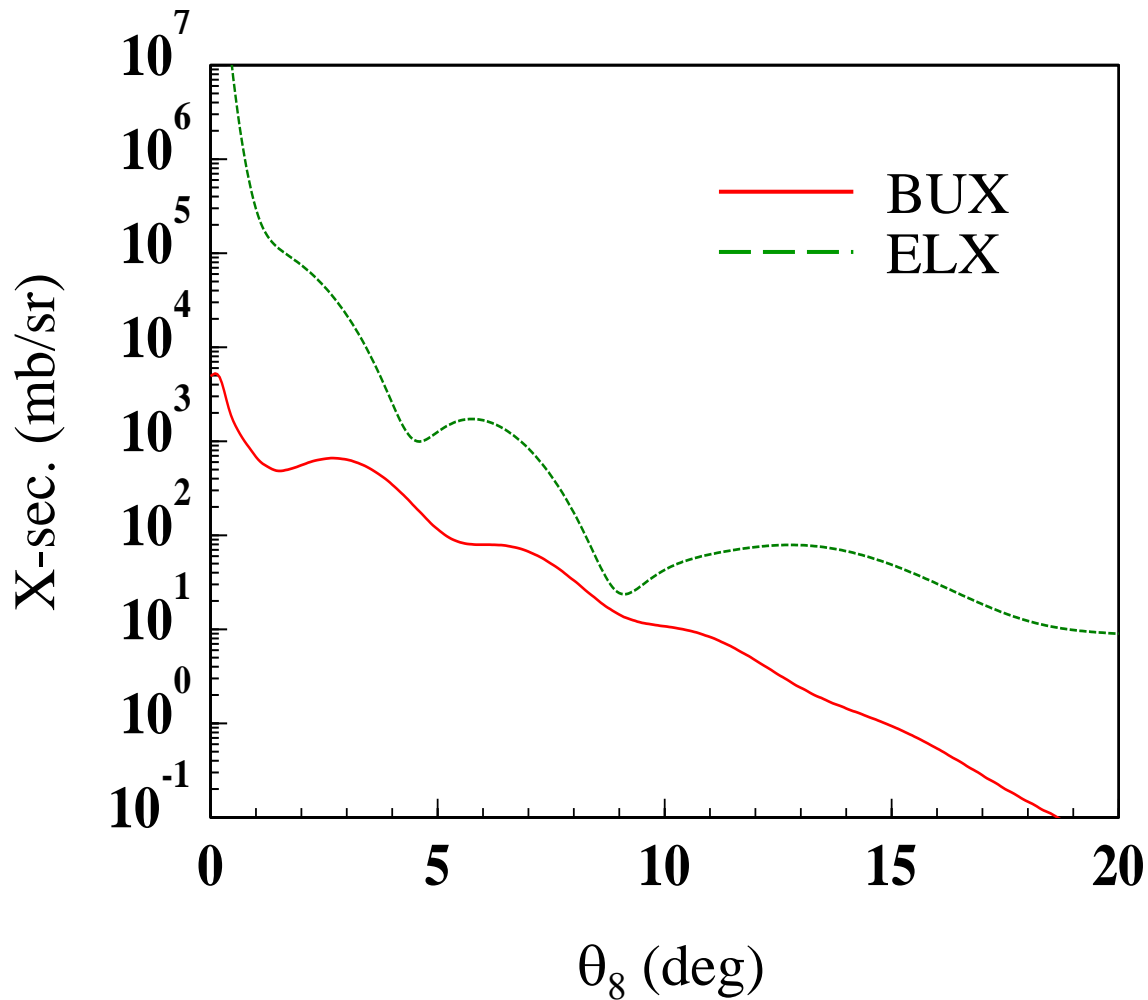
## 2) Reduction from 4-body breakup to 3-body breakup



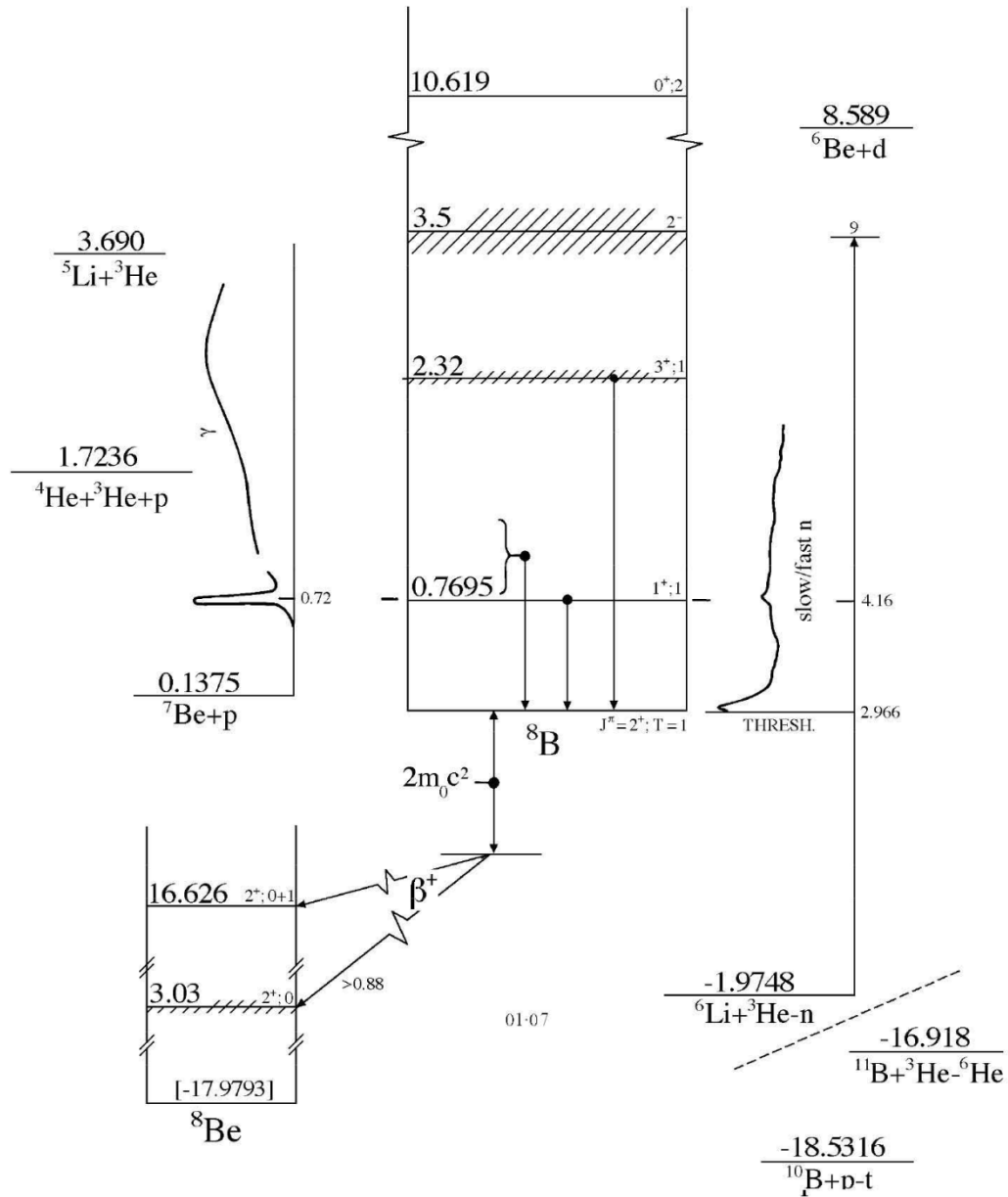
□ The triple-differential cross section for  $(^8\text{B}, ^7\text{Be}+p)$  is obtained by  $C \rho |T|^2$  with  $\mathfrak{T} = \langle \chi_1 \chi_7 \phi_7^{(0)} | U_{A3} + U_{A4} + U_{A1} + V_{13} + V_{14} | \Psi_{4\text{-body}} \rangle$

□  $^7\text{Be}$  breakup cross section by  $^{208}\text{Pb}$  turned out to be negligibly small for forward-scattering.  $\Rightarrow \begin{cases} U_{A3} + U_{A4} \approx \langle \phi_7^{(0)} | U_{A3} + U_{A4} | \phi_7^{(0)} \rangle \\ V_{13} + V_{14} \approx \langle \phi_7^{(0)} | V_{13} + V_{14} | \phi_7^{(0)} \rangle \end{cases}$

# $^8\text{B}$ scattering from $^9\text{Be}$ at 100 A MeV



# $^8\text{B}$ Energy levels



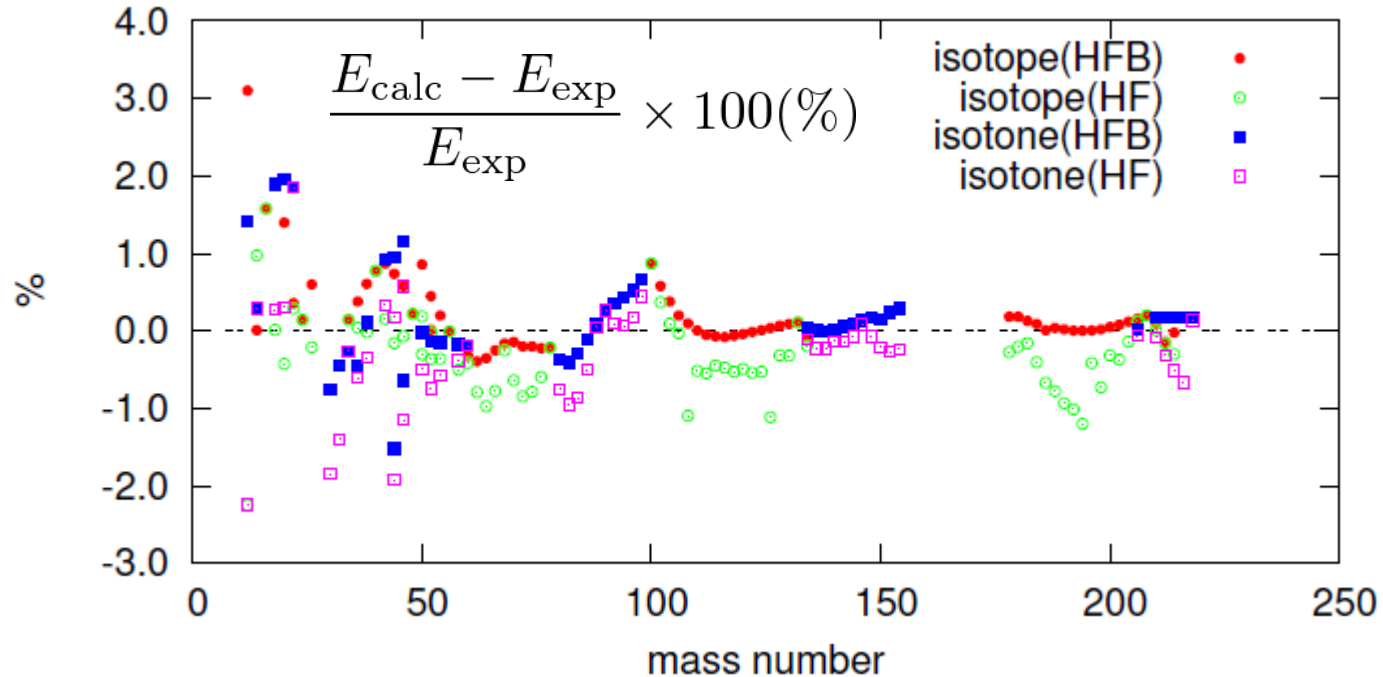
# Structure model

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## ✓ Hartree-Fock method with finite-range Gogny force

It is applicable to obtain the ground-state wave function of all nuclei.

The properties of many stable nuclei such as the binding energy are well reproduced.



We find that this method is reliable.

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# 核半径 ( ${}^6\text{He}$ , ${}^8\text{He}$ )

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