

Physics of superheavy elements

Periodic table of chemical elements

Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	
↓ Period																			
1	1 H																		2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F		10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl		18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br		36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I		54 Xe
6	55 Cs	56 Ba	57 La *	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At		86 Rn
7	87 Fr	88 Ra	89 Ac *	104 Rf *	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts		118 Og
				* 58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu		
				* 90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr		

What is the heaviest element?

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				* 90 Th	* 91 Pa	* 92 U	* 93 Np	* 94 Pu	* 95 Am	* 96 Cm	* 97 Bk	* 98 Cf	* 99 Es	* 100 Fm	* 101 Md	* 102 No	* 103 Lr	

What is the heaviest element?

natural elements: **Pu** (Z=94) → a tiny amount in nature
U (Z=92)

What determines these numbers??

Lanthanides	57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
Actinides	89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

What is the heaviest element?

natural elements:

Pu (Z=94) → a tiny amount in nature

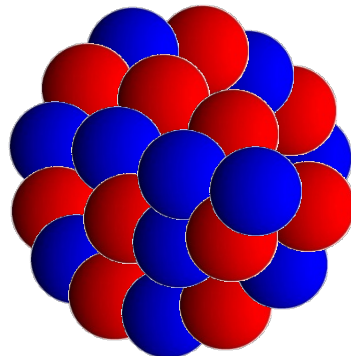
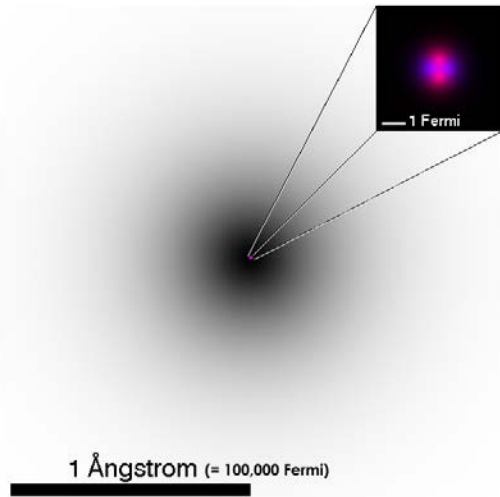
U (Z=92)

What determines these numbers??

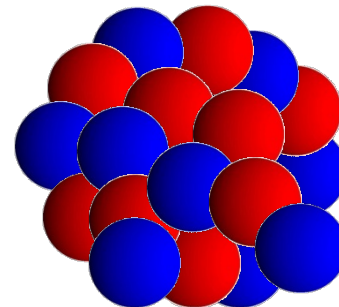
heavy nuclei → large Coulomb repulsion



unstable against α decay

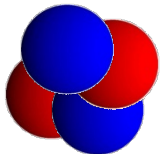


(Z,N)



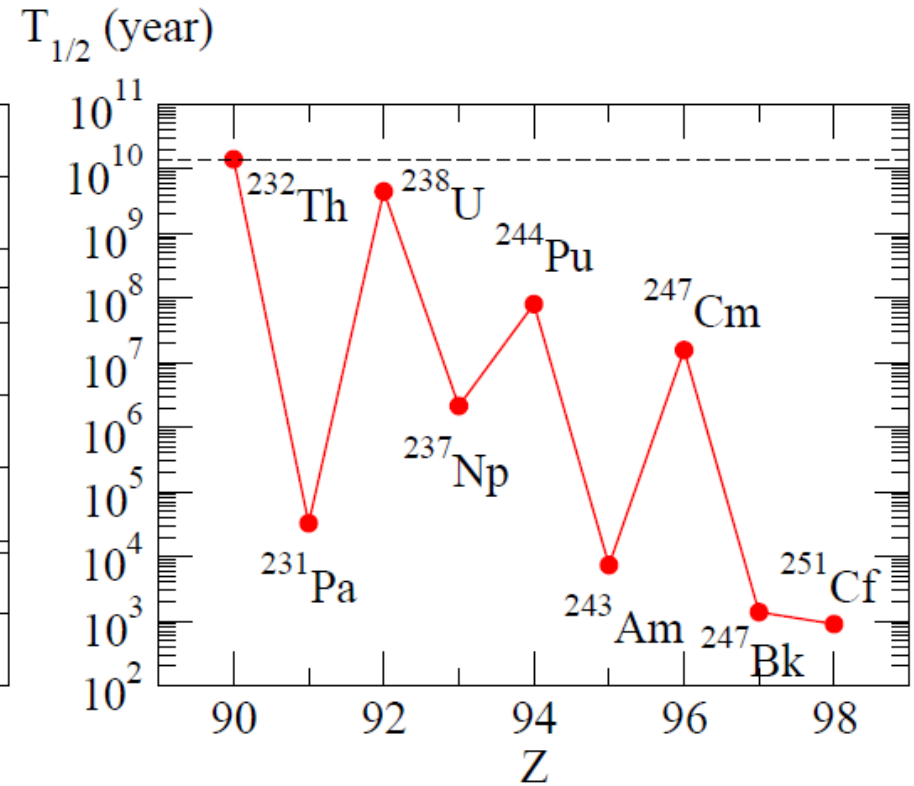
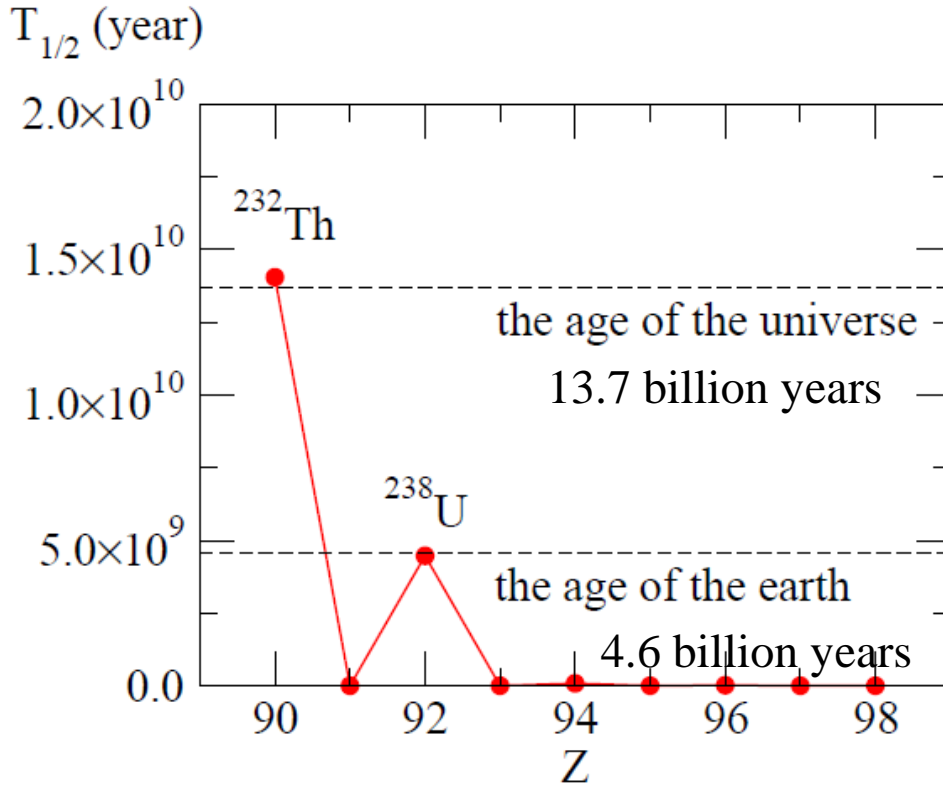
(Z-2,N-2)

+



(Z=2,N=2)

Decay half-lives of heavy nuclei



^{232}Th 1.405×10^{10} years

^{238}U 4.468×10^9 years

^{244}Pu 8.08×10^7 years

^{247}Cm 1.56×10^7 years

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artificially synthesized ('man-made')

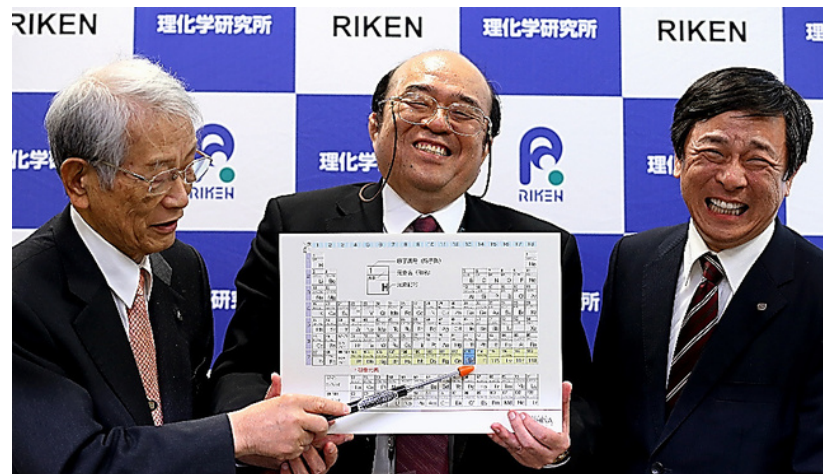
superheavy elements (SHE)

← nuclear reactions

Fusion reactions for SHE

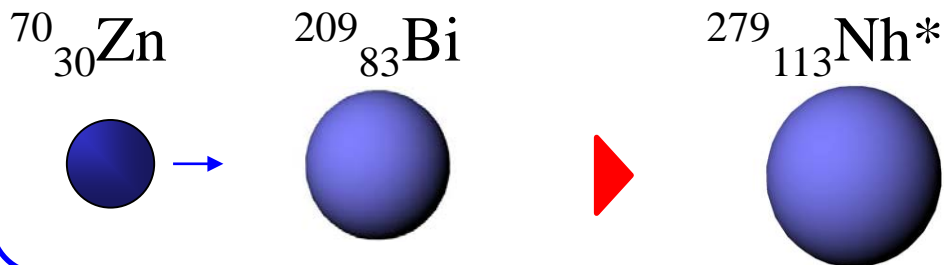
the element 113: Nh

113 Nh nihonium	115 Mc moscovium
117 Ts tennessine	118 Og oganesson



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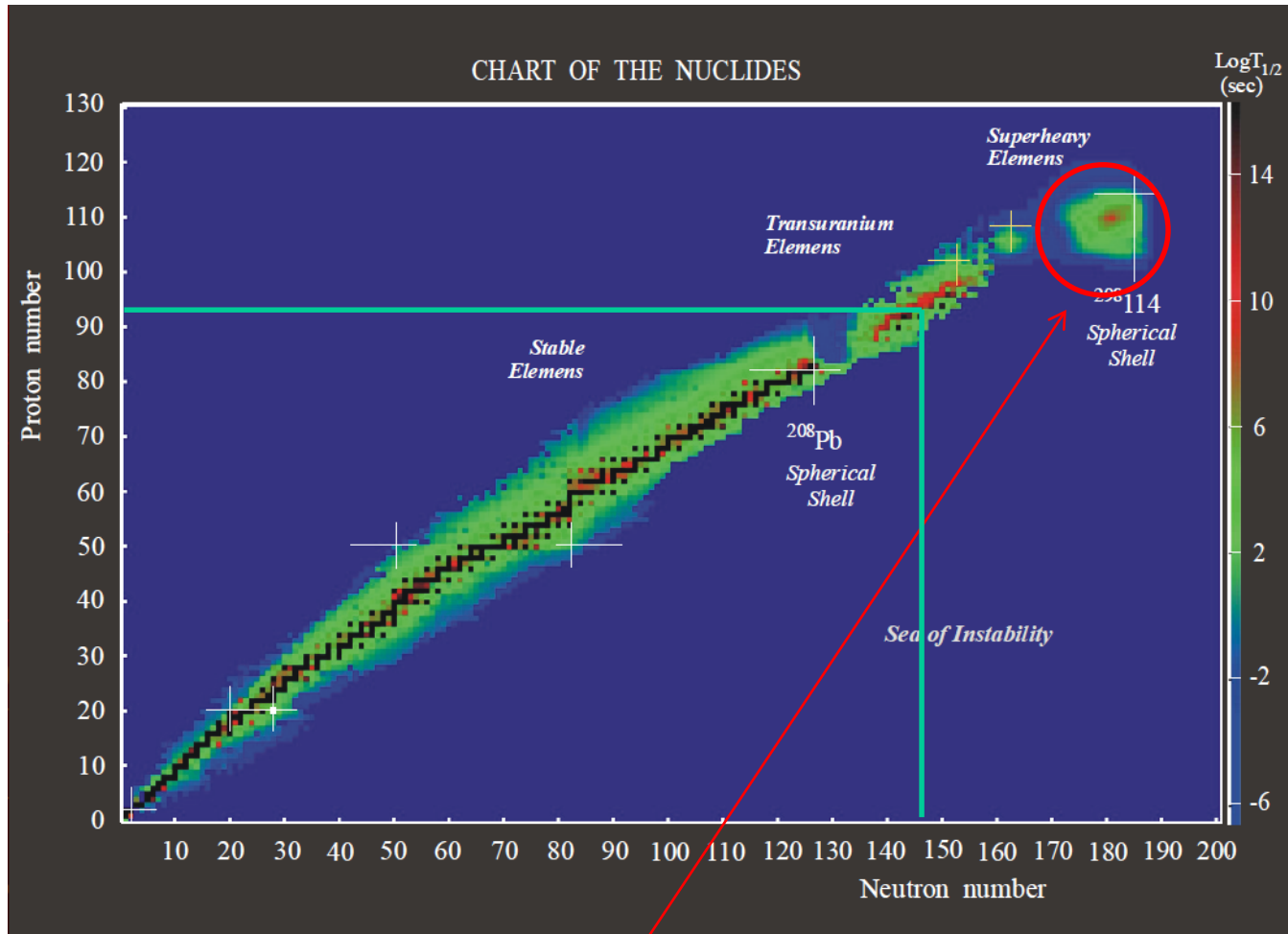
November, 2016



Heavy-ion fusion reaction

Wikipedia

Prediction of island of stability: an important motivation of SHE study

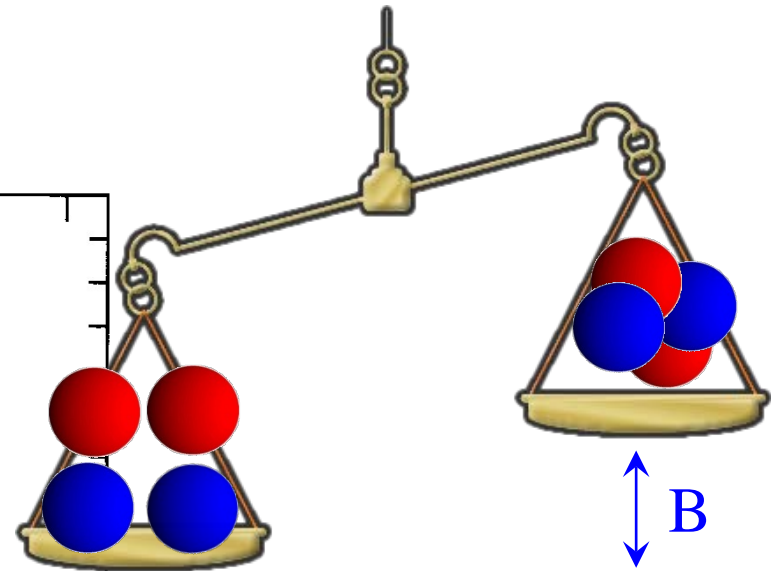
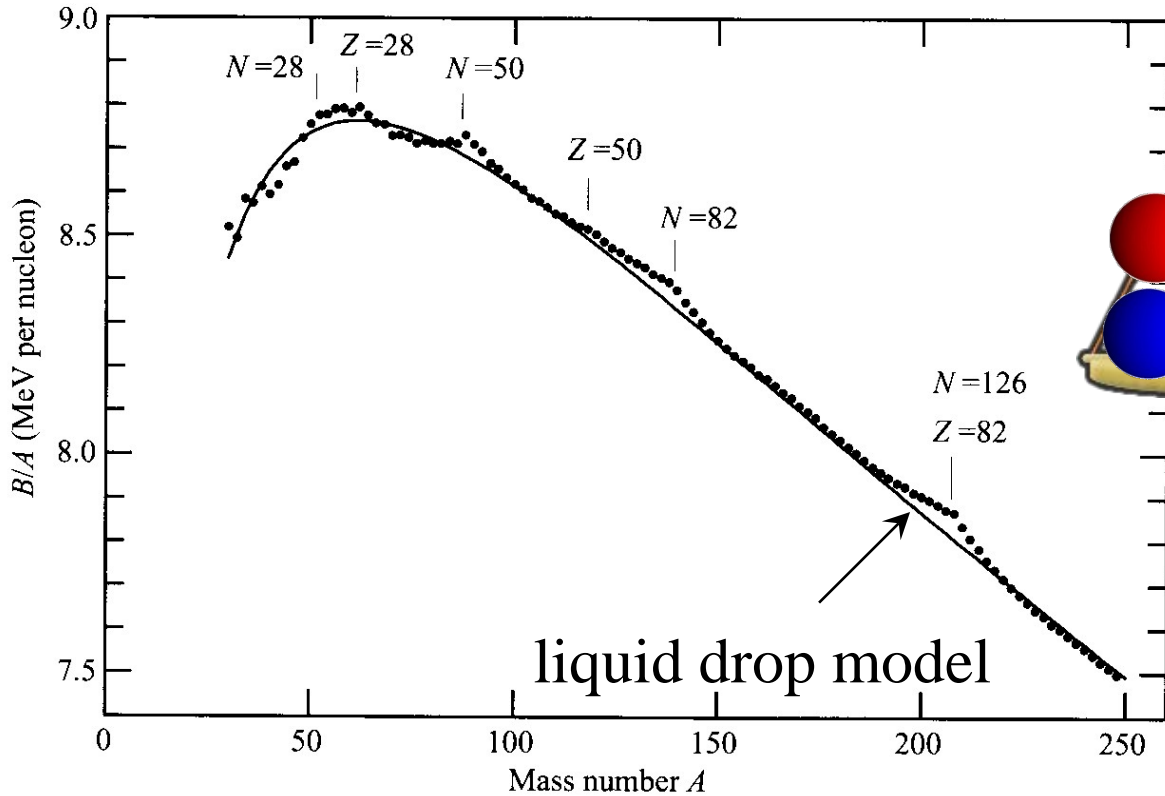


island of stability around $Z=114$, $N=184$

Yuri Oganessian

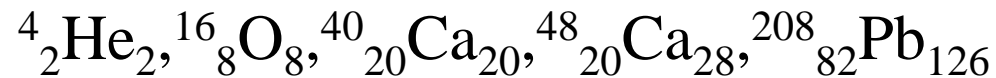
W.D. Myers and W.J. Swiatecki (1966), A. Sobiczewski et al. (1966)

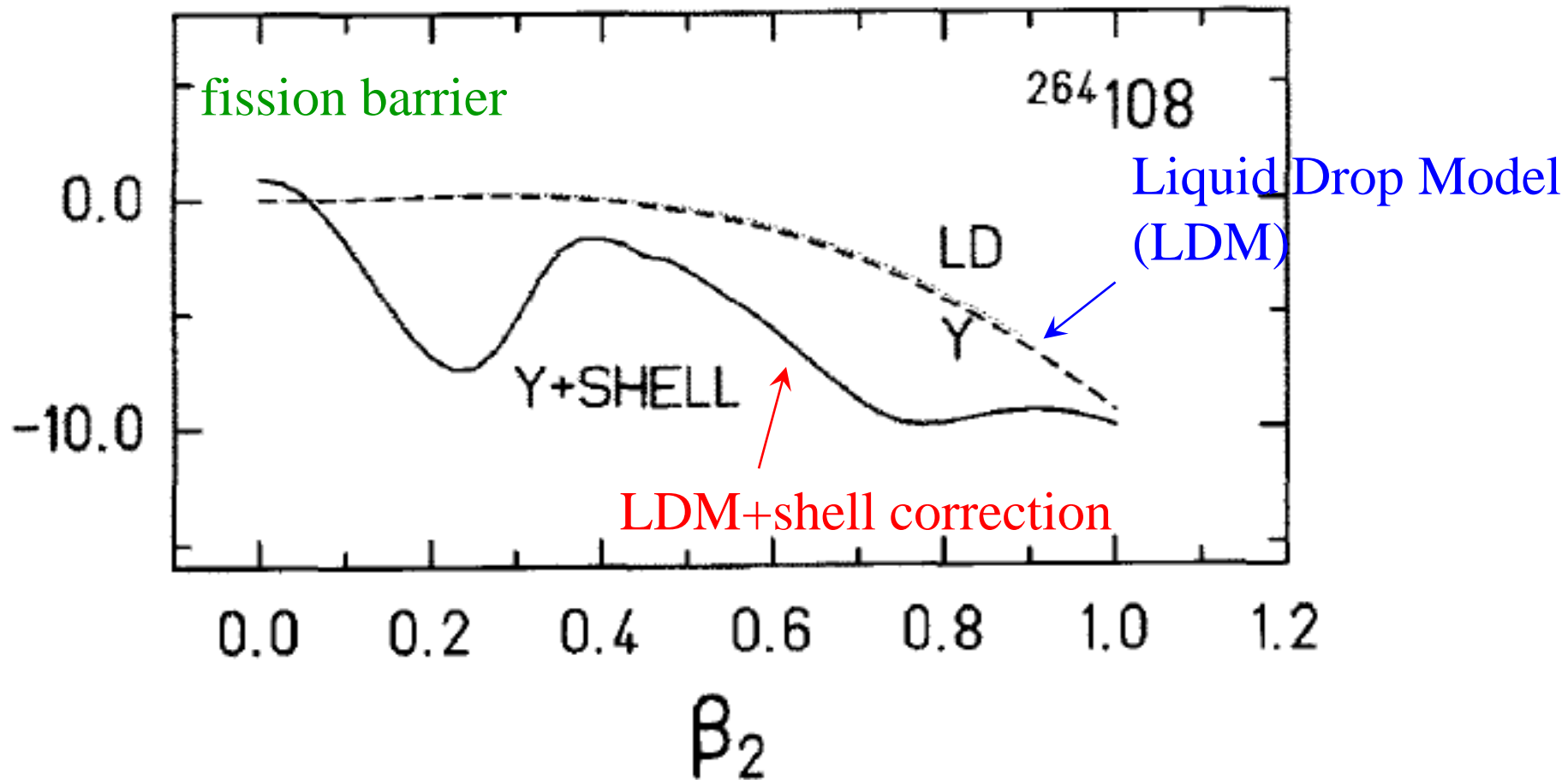
shell energy



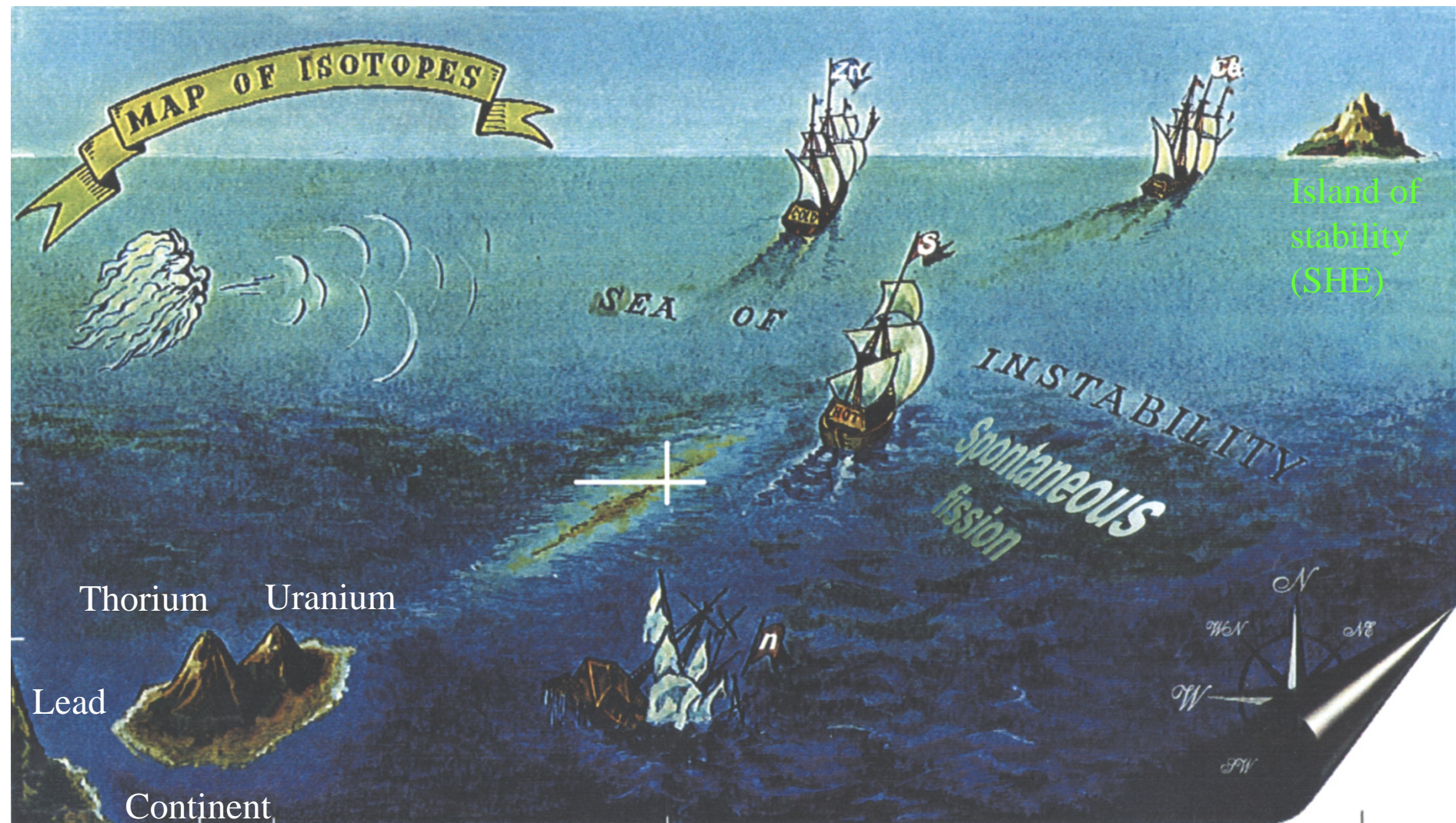
Extra binding for N or $Z = 2, 8, 20, 28, 50, 82, 126$ (magic numbers)

⇒ Very stable





Z. Patyk et al., NPA491('89) 267



who is she?

7

87	88	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118
Fr	Ra	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Uut	Fl	Uup	Lv	Uus	Uuo

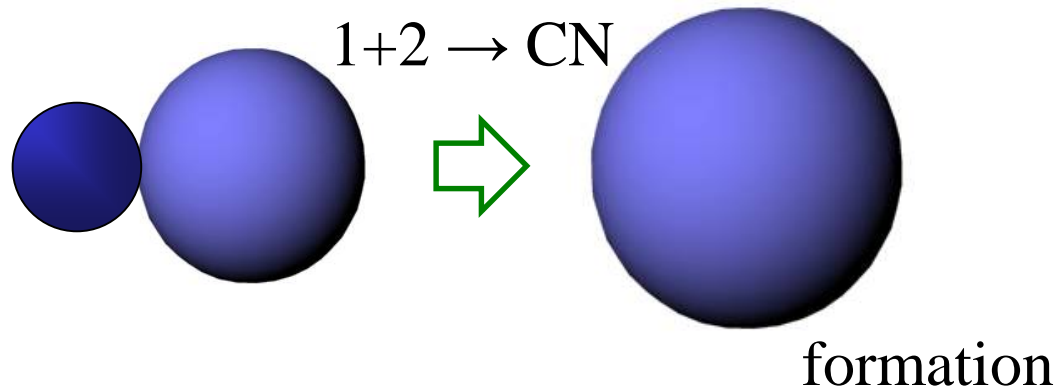
Z=110	Darmstadtium (Ds)	1994	Germany
Z=111	Roentgenium (Rg)	1994	Germany
Z=112	Copernicium (Cn)	1996	Germany
Z=113	Nihonium (Nh)	2003	Russia / 2004 Japan
Z=114	Flerovium (Fl)	1999	Russia
Z=115	Moscovium (Mc)	2003	Russia
Z=116	Livermorium (Lv)	2000	Russia
Z=117	Tennessine (Ts)	2010	Russia
Z=118	Oganesson (Og)	2002	Russia

113 Nh nihonium	115 Mc moscovium
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Germany, Japan: cold fusion reactions

Russia: hot fusion reactions

Germany, Japan: cold fusion reactions
 Russia: hot fusion reactions



	Hot Fusion	Cold Fusion
Example	$^{48}\text{Ca} + ^{243}\text{Am} \rightarrow ^{187}\text{Nh} + 4\text{n}$	$^{70}\text{Zn} + ^{209}\text{Bi} \rightarrow ^{278}\text{Nh} + 1\text{n}$
asymmetry	large	small

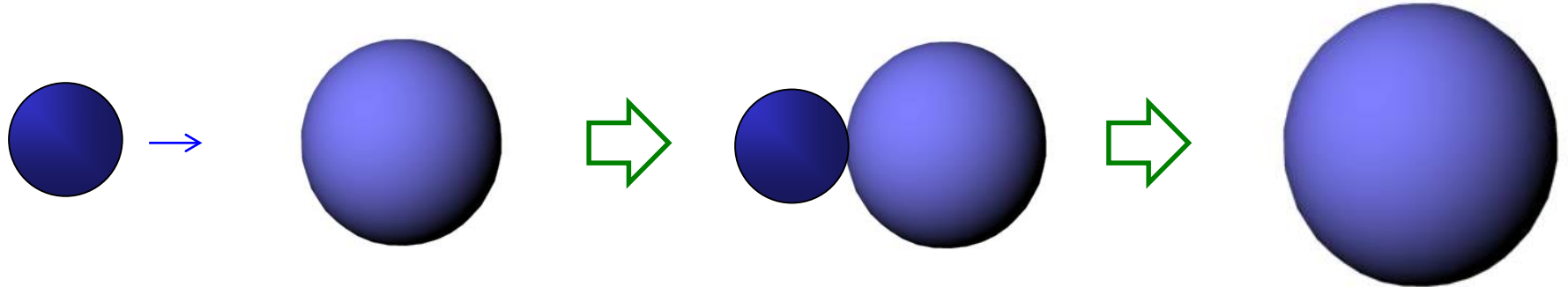
hot CN

cold CN

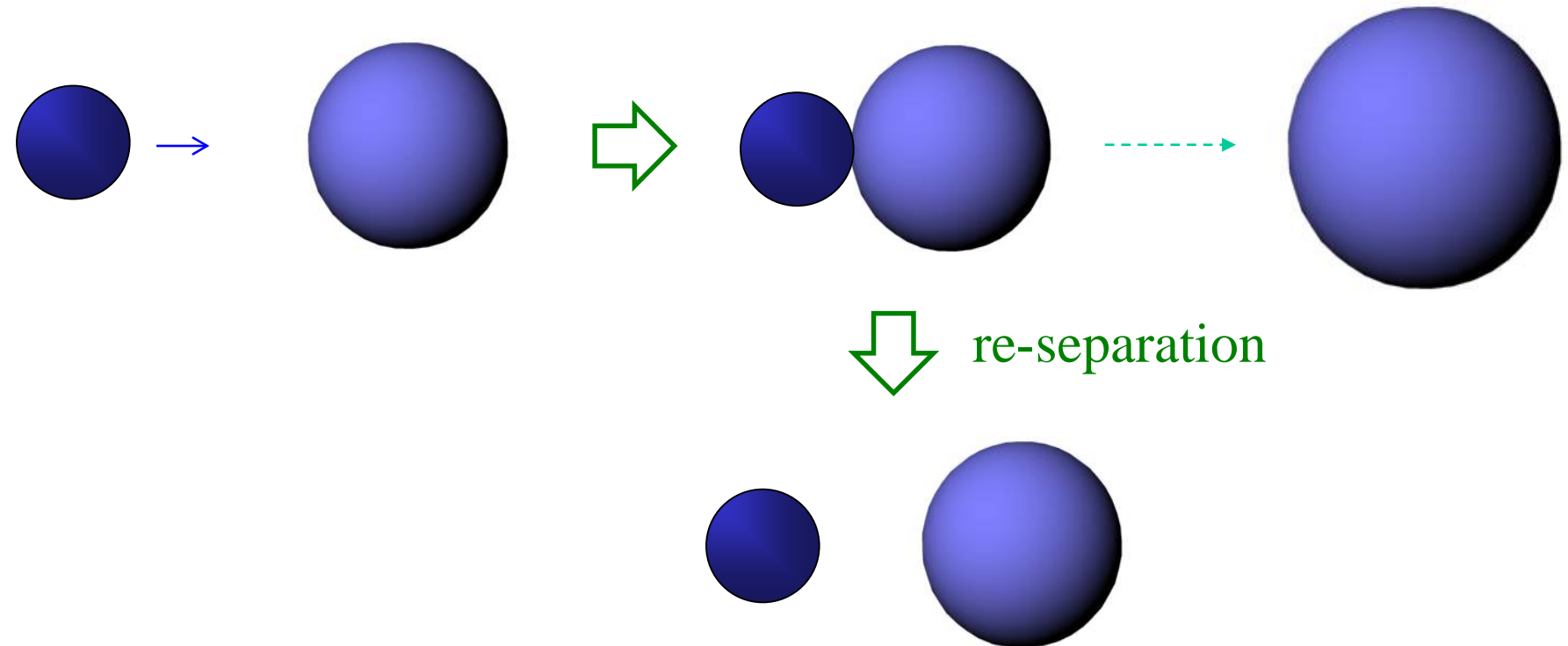
How to synthesize SHE?

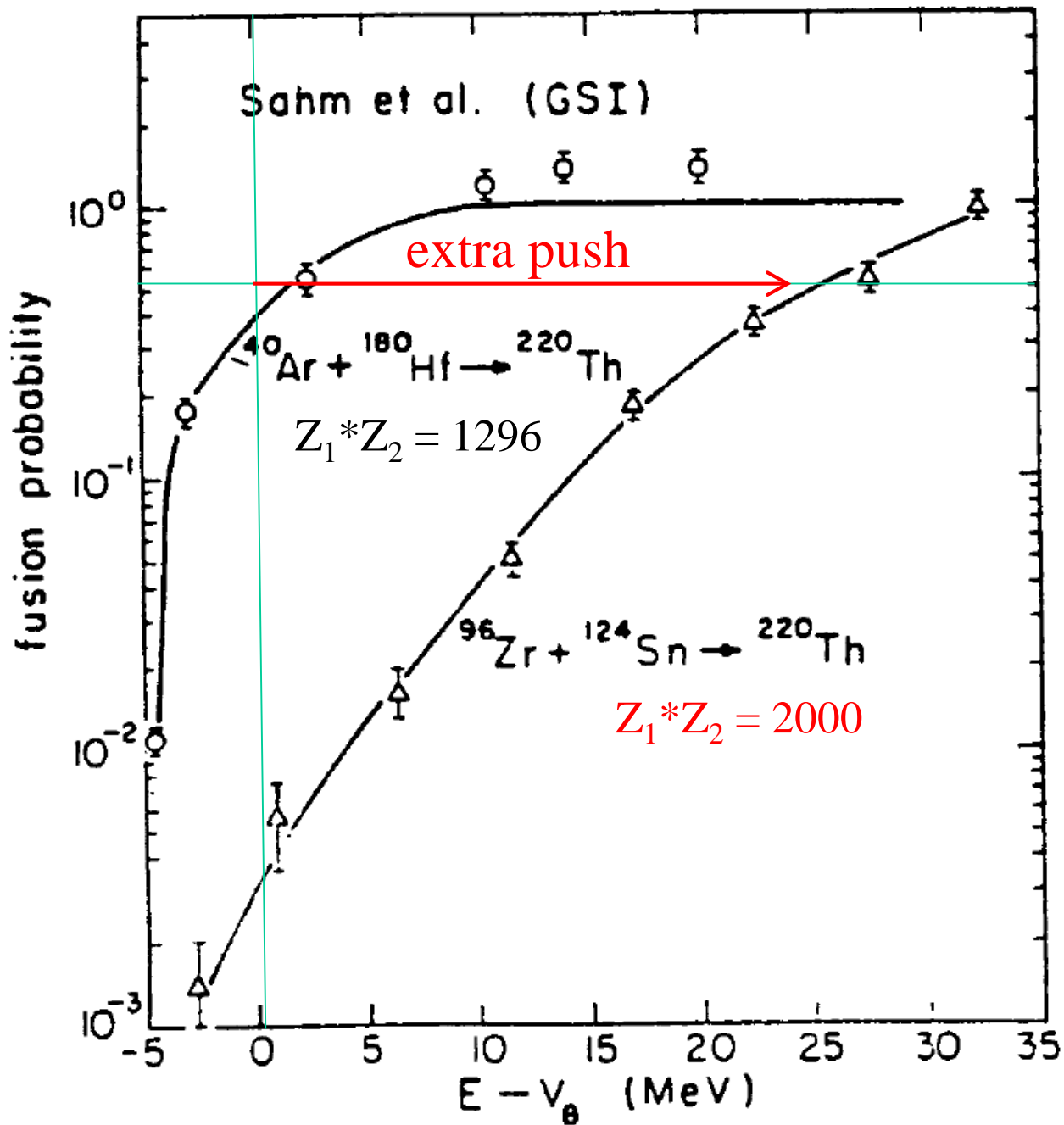
Nuclear fusion reactions

➤ Fusion of medium-heavy systems:

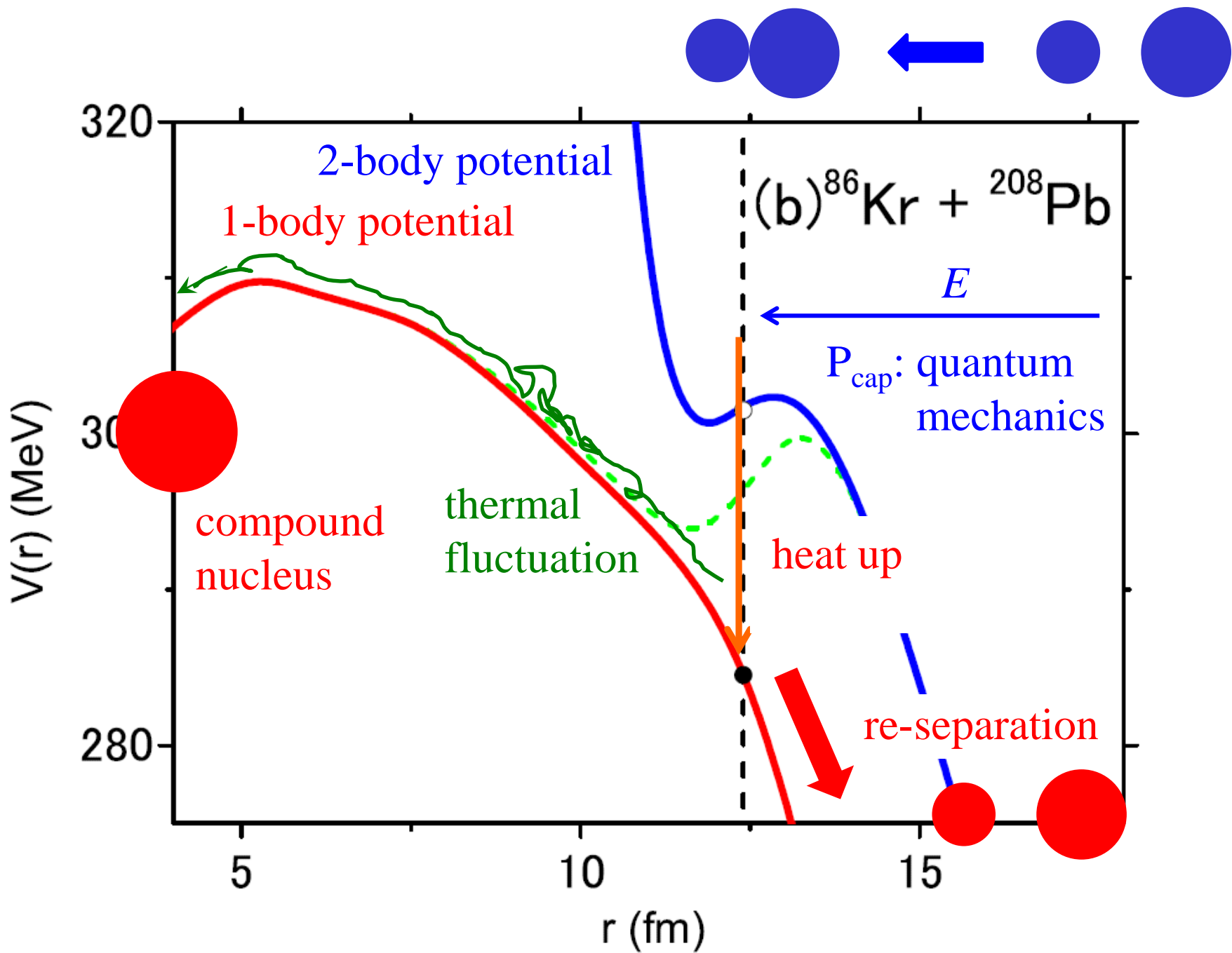


➤ Fusion of heavy and super-heavy systems:





C.-C. Sahm et al.,
 Z. Phys. A319('84)113

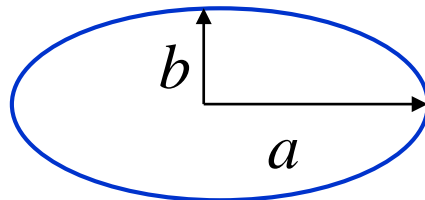


(復習)

$$B(N, Z) = a_v A - a_s A^{2/3} - a_C \frac{Z^2}{A^{1/3}} - a_{\text{sym}} \frac{(N - Z)^2}{A}$$

原子核を体積一定のまま変形してみる

例) 回転楕円体



$$a = R \cdot (1 + \epsilon)$$

$$b = R \cdot (1 + \epsilon)^{-1/2}$$

$$ab^2 = R^3 = \text{一定}$$

変形したときのエネルギー変化:

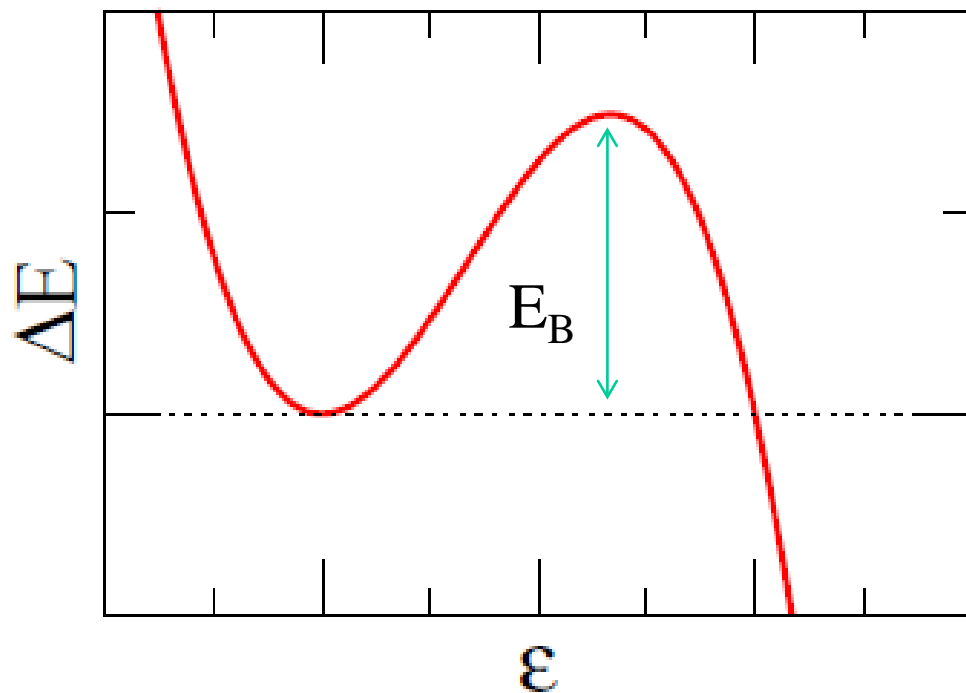
- 体積項、対称エネルギー項: 変化せず
 - クーロン項
 - 表面項
- } 変化

{ 表面項 → 球形になる傾向
クーロン項 → 変形になる傾向 } → 2つの力の競合

(復習)

$$\Delta E = E_S^{(0)} \left\{ \frac{2}{5}(1-x)\epsilon^2 - \frac{4}{105}(1+2x)\epsilon^3 + \dots \right\}$$

$$x \equiv \frac{E_C^{(0)}}{2E_S^{(0)}} = \frac{a_C}{2a_S} \cdot \frac{Z^2}{A} \sim \frac{1}{53.3} \cdot \frac{Z^2}{A}$$



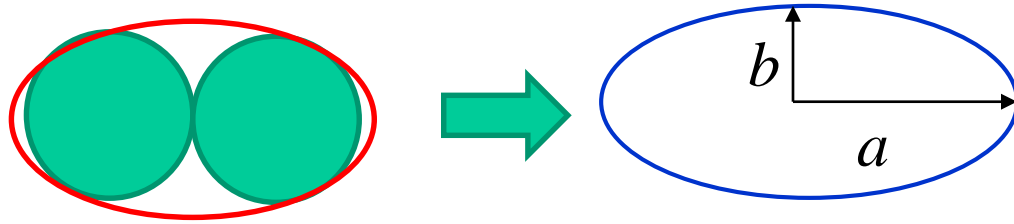
$$E_B = \frac{98}{15} \cdot \frac{(1-x)^3}{(1+2x)^2} \cdot E_S^{(0)}$$

重い核ほど障壁は低くなる

$$\epsilon_B = 7 \cdot \frac{(1-x)}{(1+2x)}$$

重い核ほど障壁での変形度は小さくなる

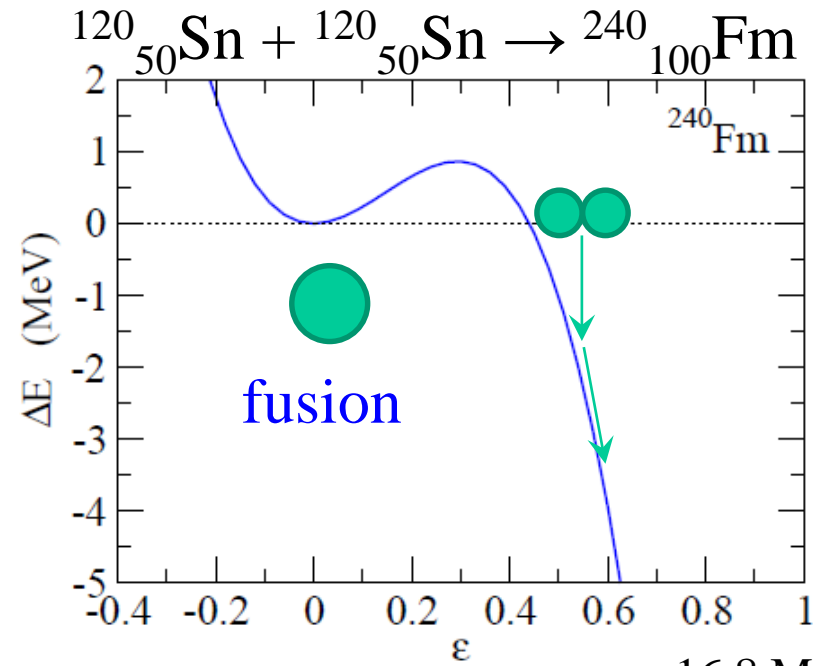
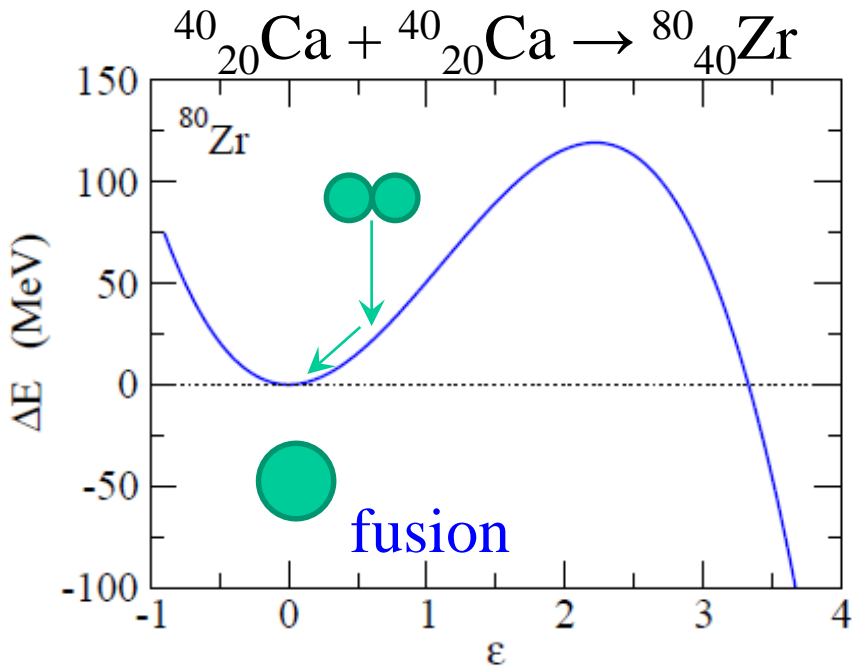
if two identical nuclei contact:



$$a = R_0 \cdot (1 + \epsilon)$$

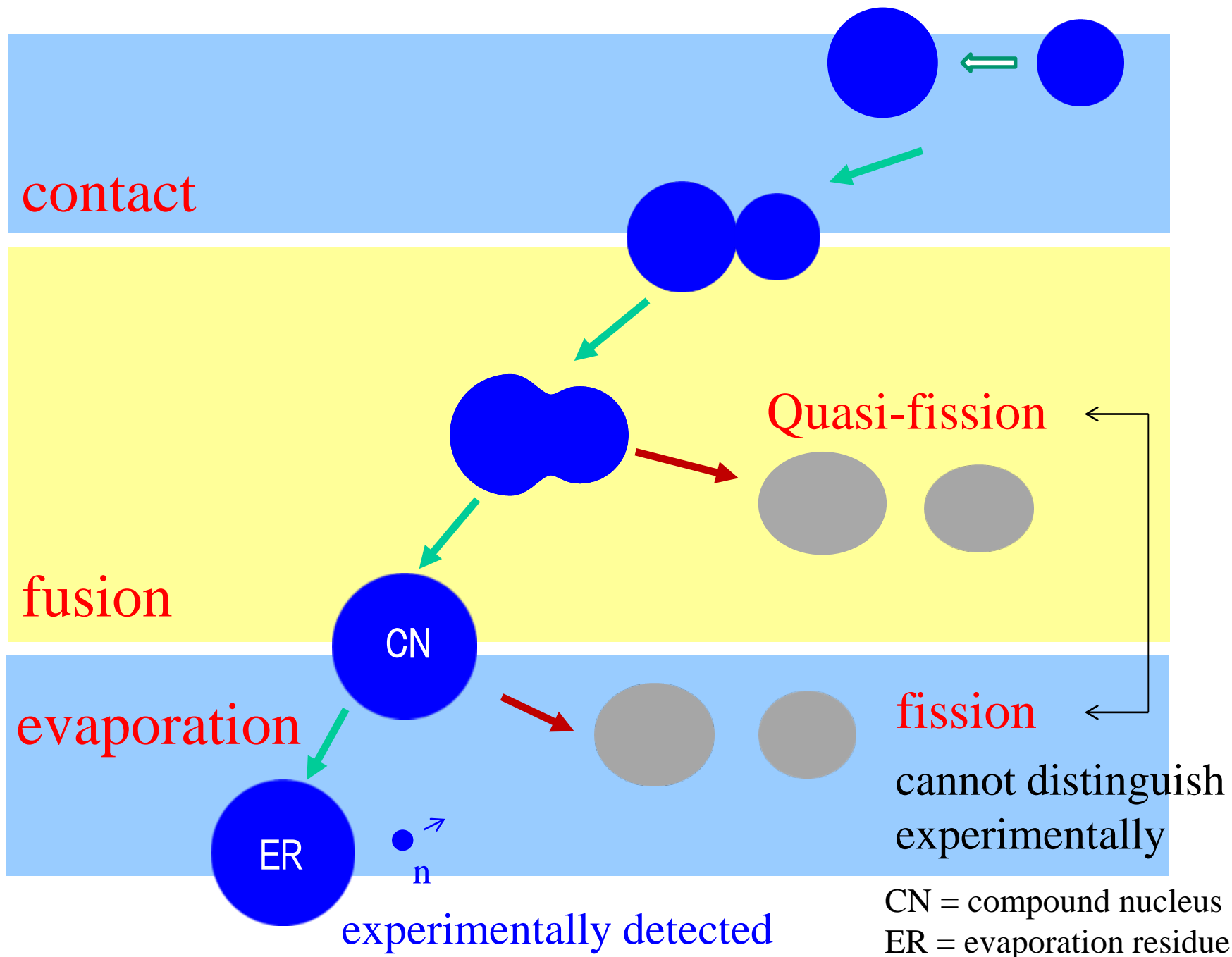
$$b = R_0 \cdot (1 + \epsilon)^{-1/2}$$

$$\frac{a}{b} \sim \frac{2R}{R} = 2 \rightarrow \epsilon \sim 0.587$$



threshold: $Z_1 \cdot Z_2 = 1600 \sim 1800$

$a_s = 16.8 \text{ MeV}$
 $a_c = 0.72 \text{ MeV}$

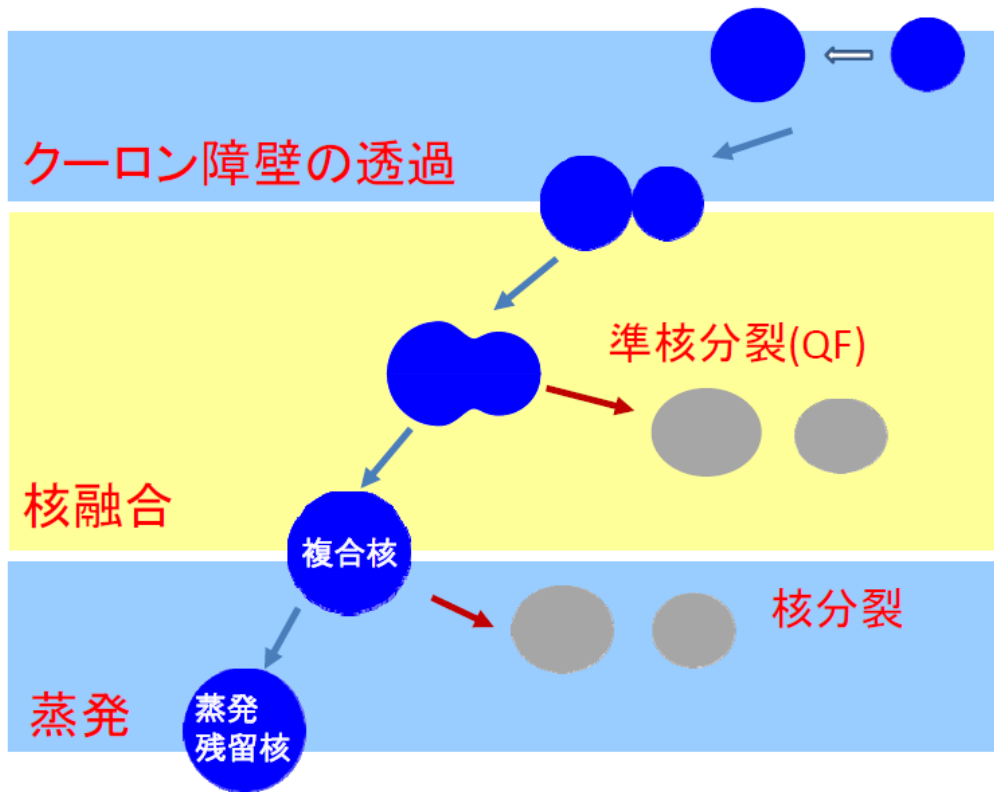


* どのように核融合反応断面積を測定するのか?

➤ 中重核領域の場合:

✓ 核融合生成物の直接測定 (蒸発残留核 + 核分裂)

➤ 重核・超重核領域の場合:



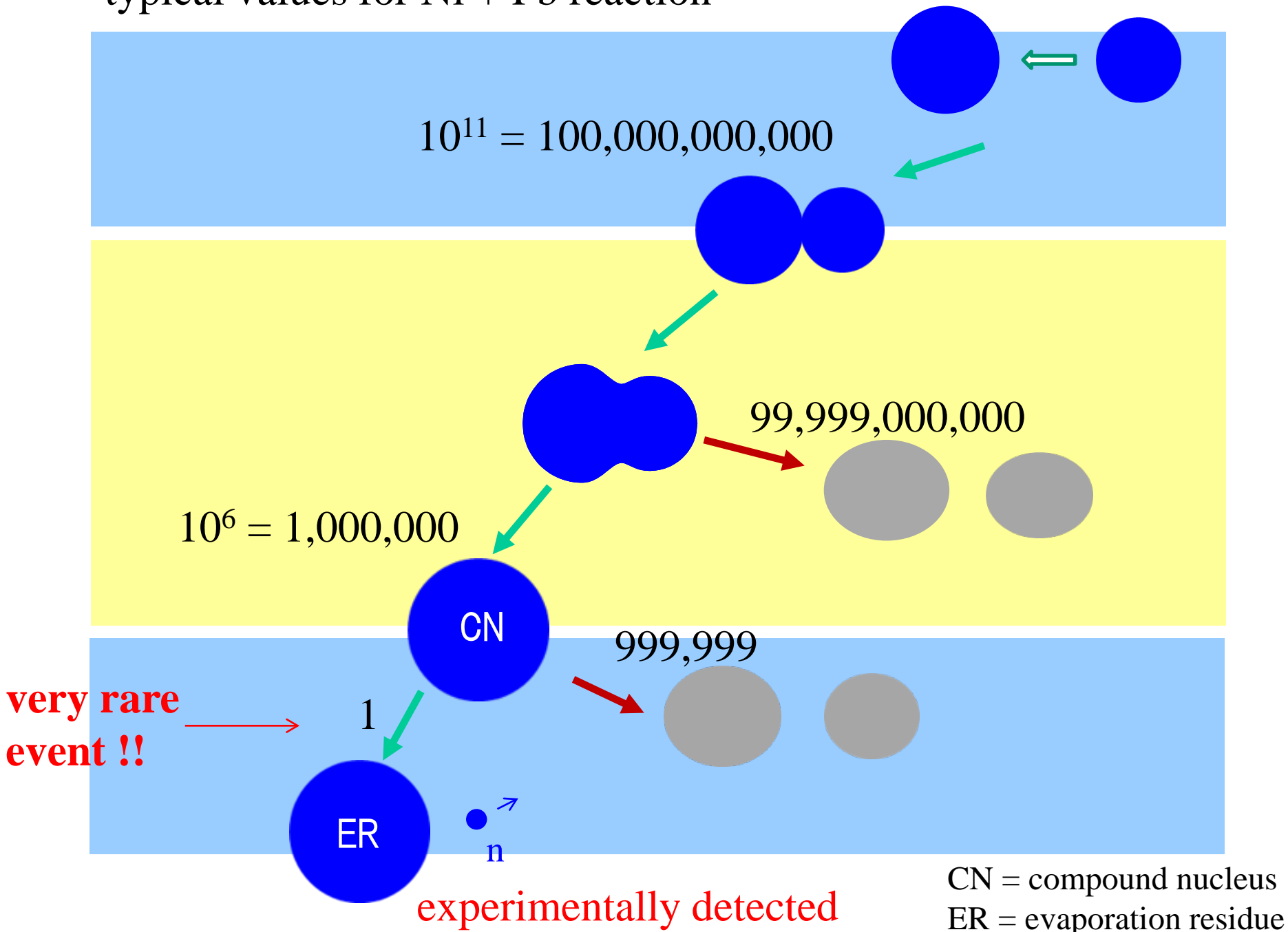
準核分裂 + 生き残りの2重苦

大きな準核分裂の確率のため、核分裂片の測定は複合核形成を意味しない (QFとFFの区別は実験的に困難)

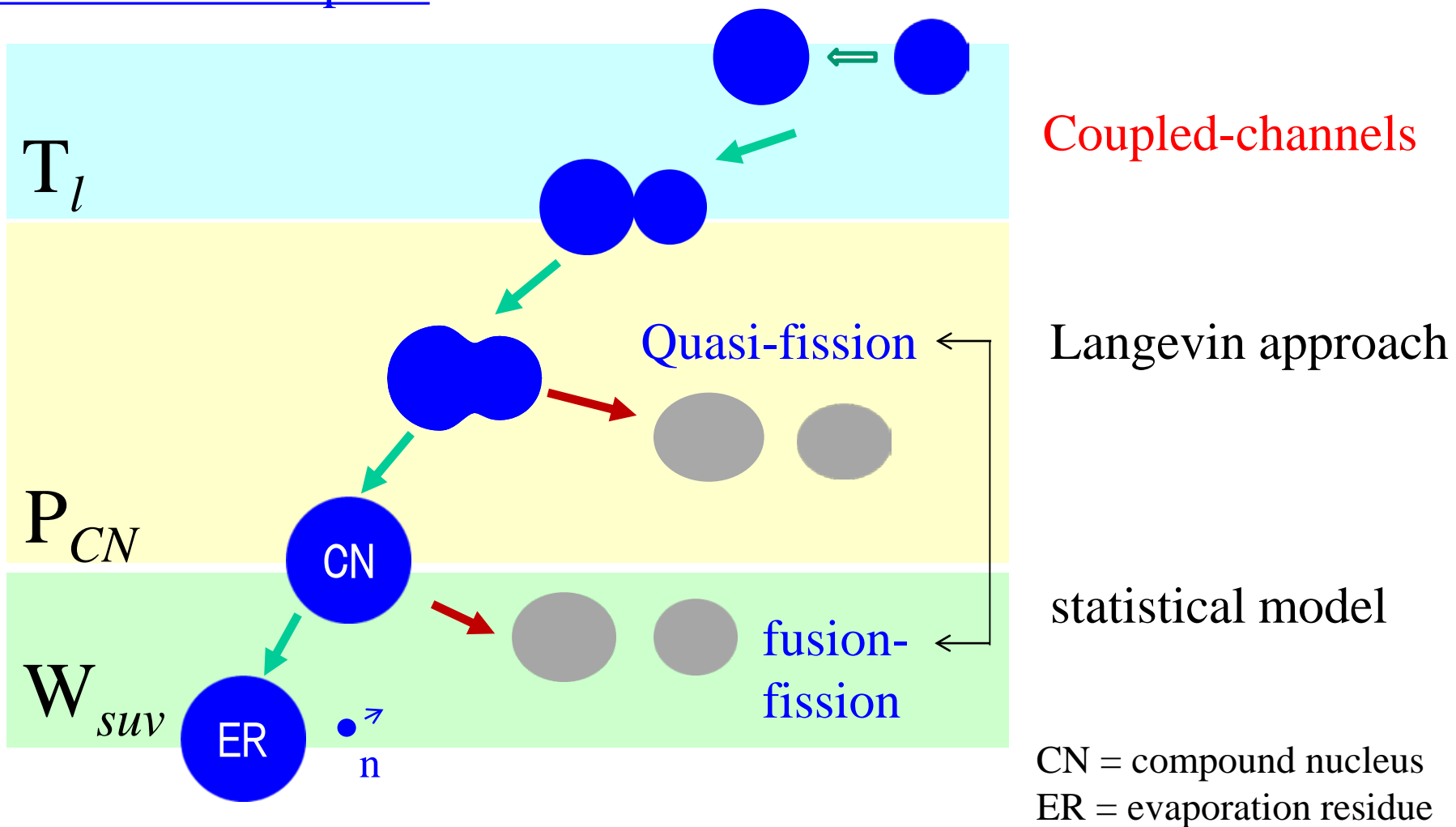
蒸発残留核の測定をもって複合核形成とみなす

重い複合核:
圧倒的な確率で核分裂
(例: $^{58}\text{Fe} + ^{208}\text{Pb}$ 反応では
核分裂しない確率は
 $P_{\text{suv}} \sim 10^{-6}$ 程度)

typical values for Ni + Pb reaction

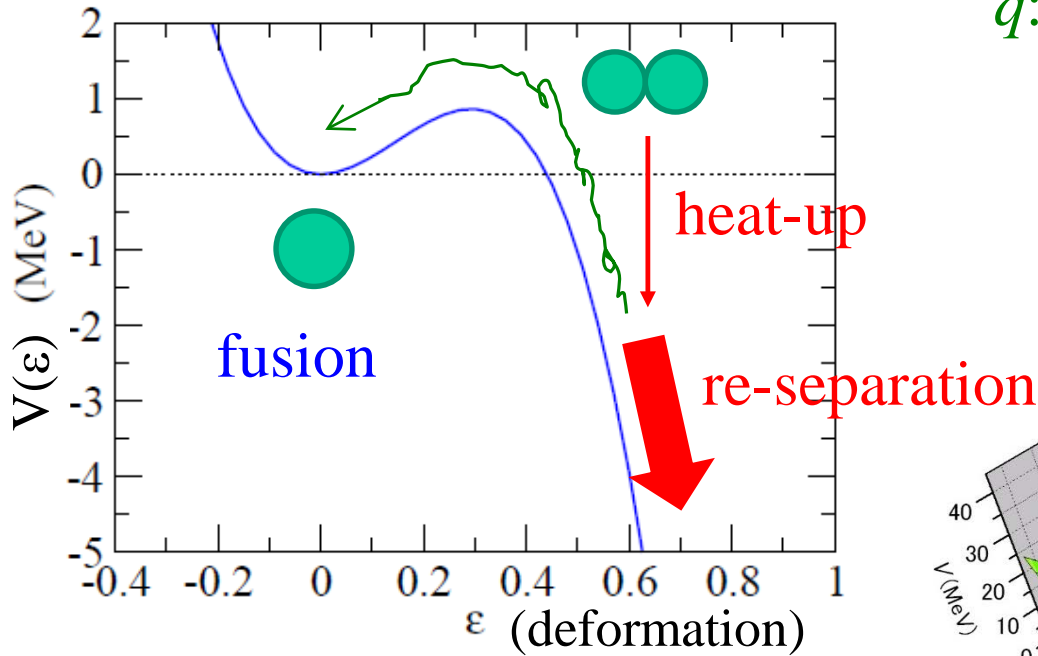


Theoretical description



$$\sigma_{ER}(E) = \frac{\pi}{k^2} \sum_l (2l + 1) T_l(E) P_{CN}(E, l) W_{suv}(E^*, l)$$

Langevin approach



thermal fluctuation

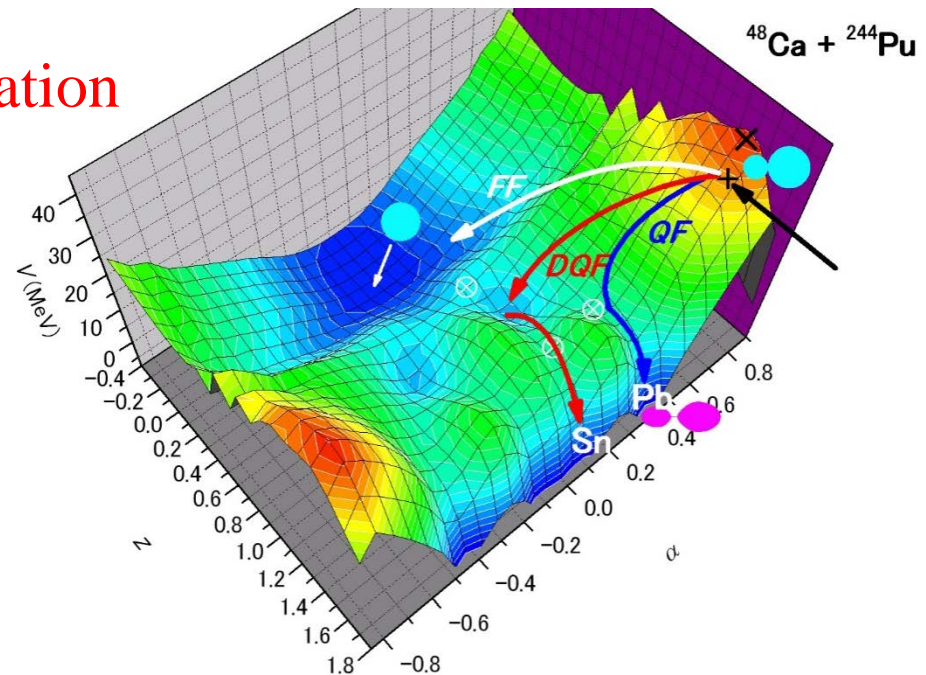
→ Langevin method
(Brownian method)

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

γ : friction coefficient
 $R(t)$: random force

multi-dimensional extention

- internuclear separation,
- deformation,
- asymmetry of the two fragments



Theory: Lagenvin approach

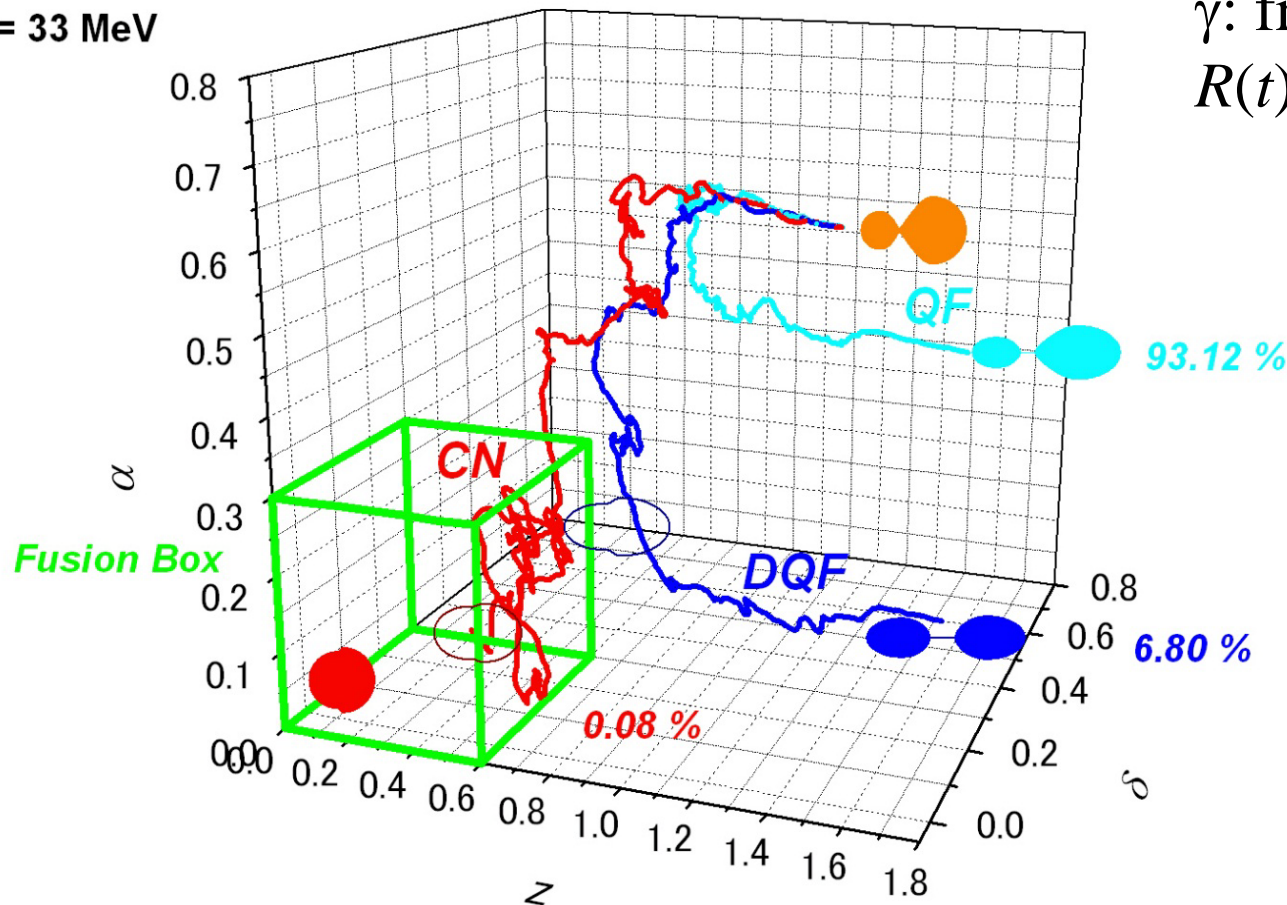
multi-dimensional extension of:

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

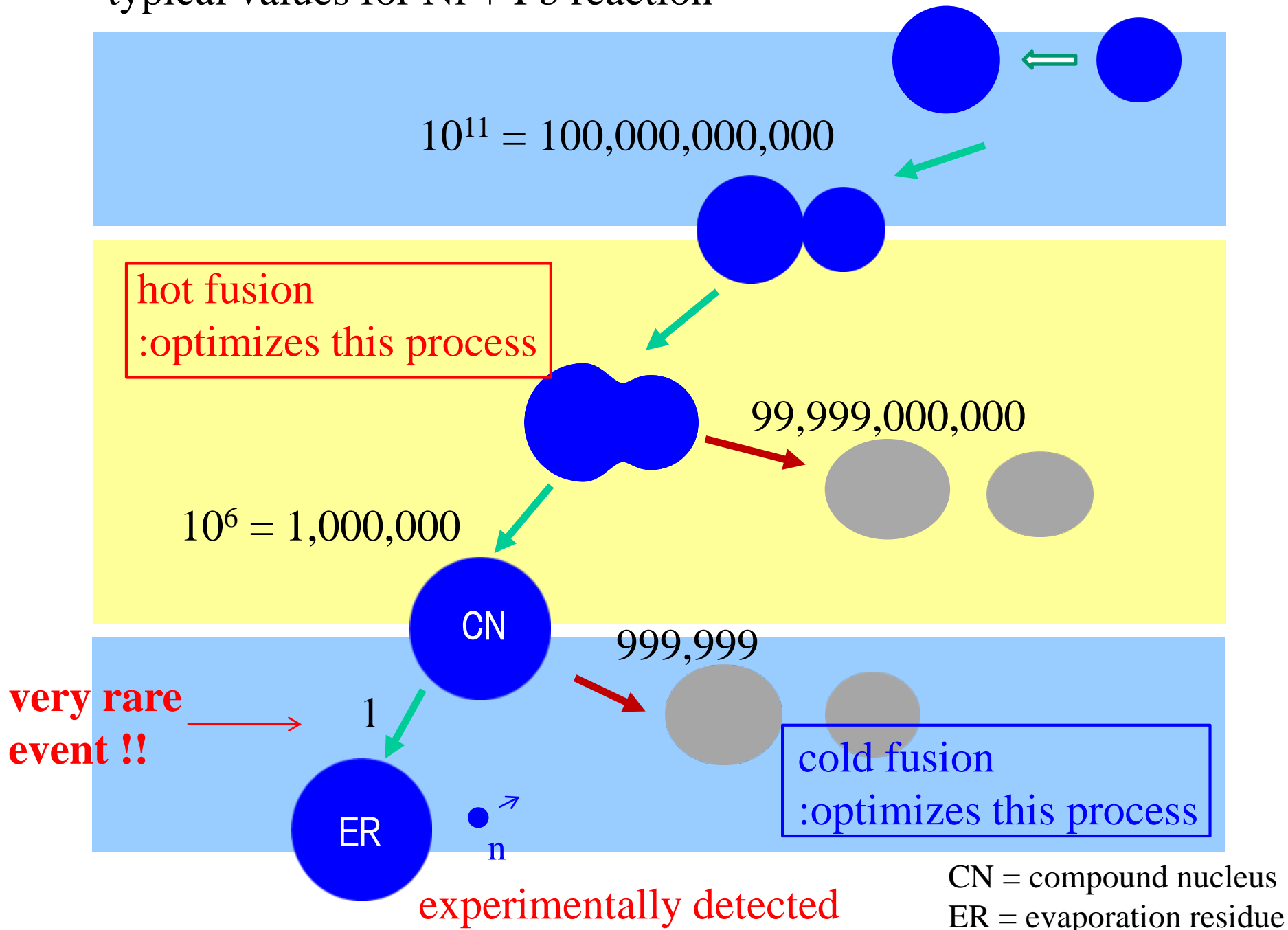
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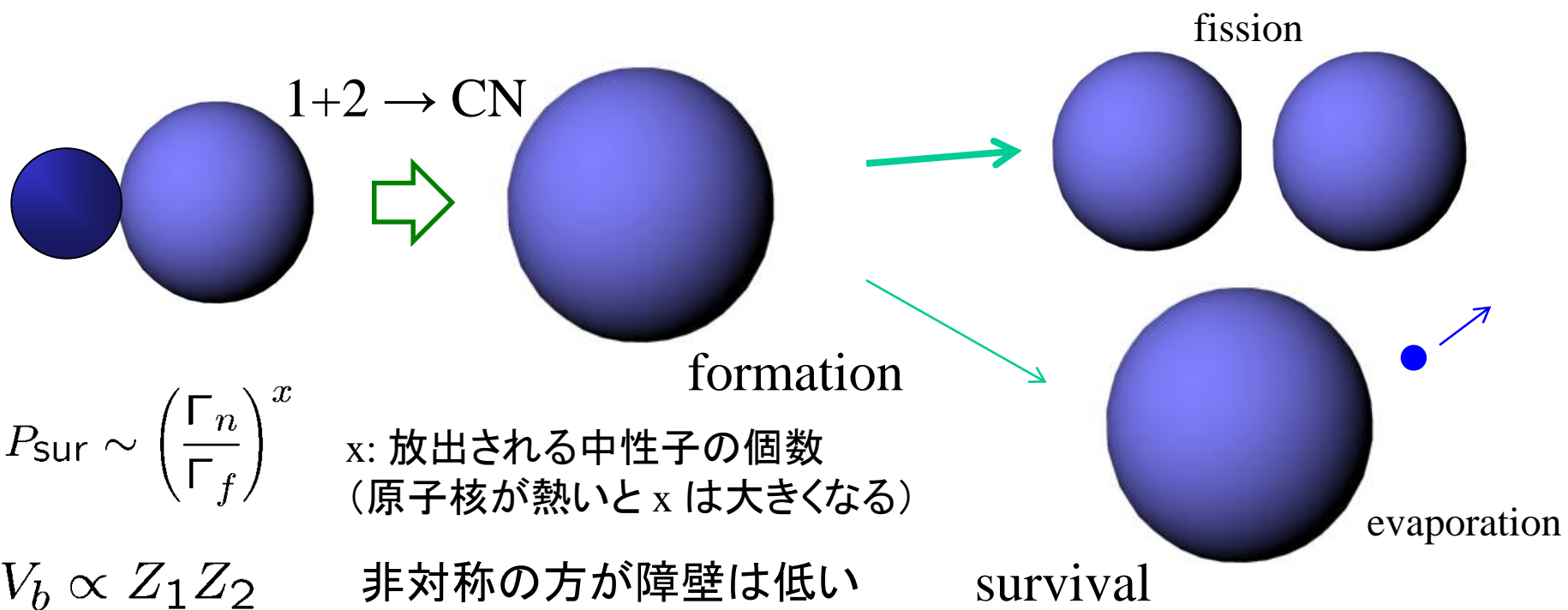


$E^* = 33 \text{ MeV}$



typical values for Ni + Pb reaction





	Hot Fusion	Cold Fusion
Example	$^{48}\text{Ca} + ^{243}\text{Am} \rightarrow ^{187}\text{Nh} + 4n$	$^{70}\text{Zn} + ^{209}\text{Bi} \rightarrow ^{278}\text{Nh} + 1n$
asymmetry	large	small
Capture	large	small
Survival	small	large

$$\sigma \sim \text{fb} = 10^{-39} \text{ cm}^2$$

RIKEN

(Cold fusion)



3rd event Aug. 12 2012

113

112

known nuclides

111

110

109

108

107

106

105

104

103

102

101

100

99

98

118

117

116

115

113

113

α

α

α

α

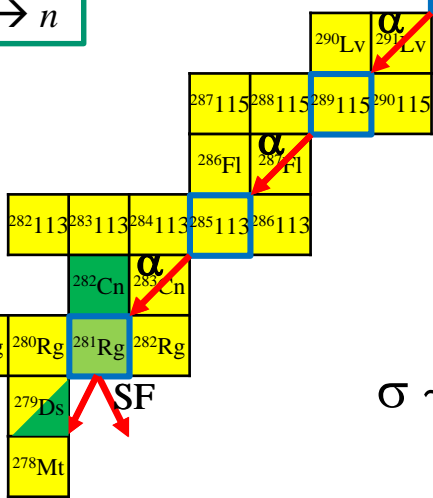
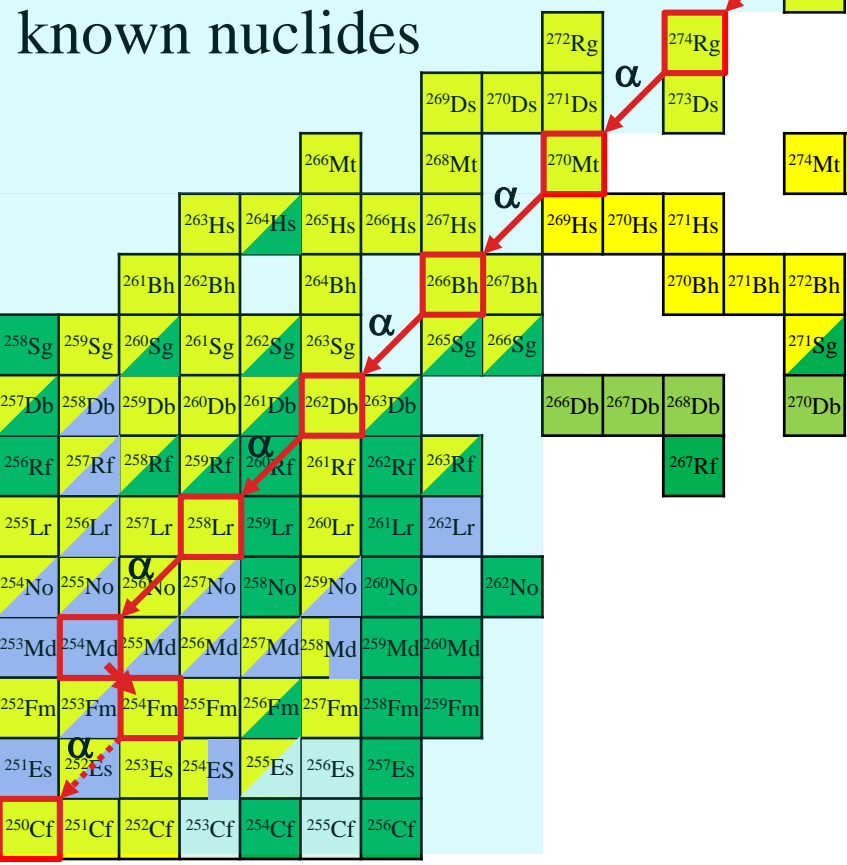
α

α

α

α

α



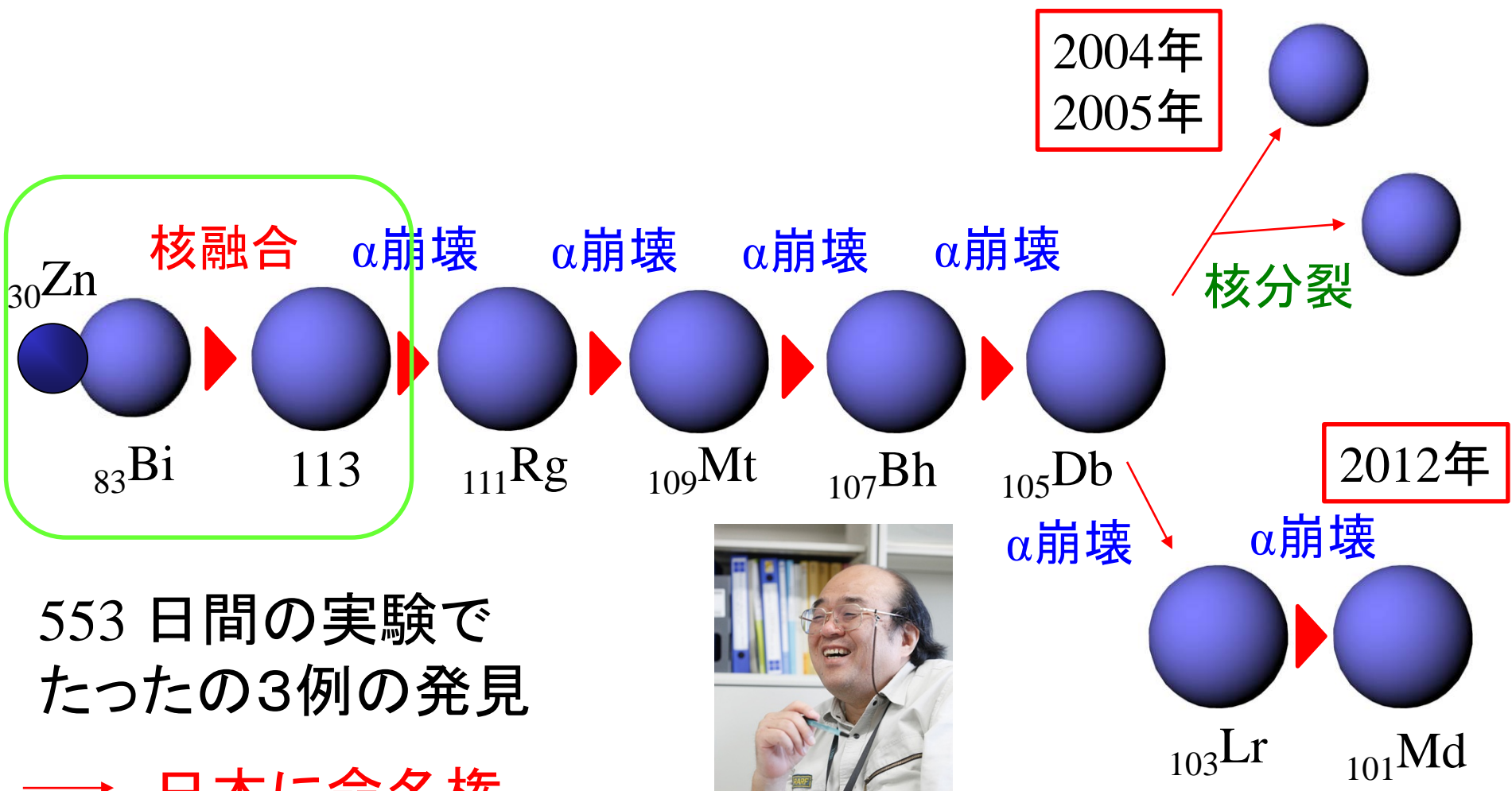
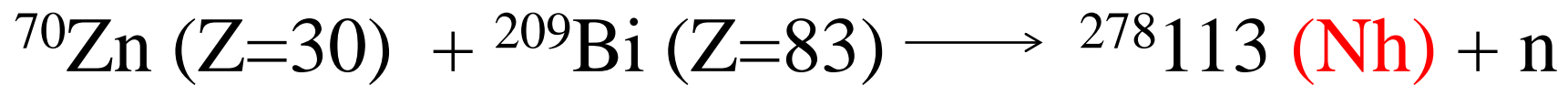
Dubna
(Hot fusion)

$$\sigma \sim \text{pb} = 10^{-36} \text{ cm}^2$$

cf. Cold Fusion:
既知核とつながる
(不定性がより少ない)

Hot Fusion:
より中性子過剰な複合核
が作れる。

新元素113番 ニホニウム (Nh)



553 日間の実験で
たったの3例の発見

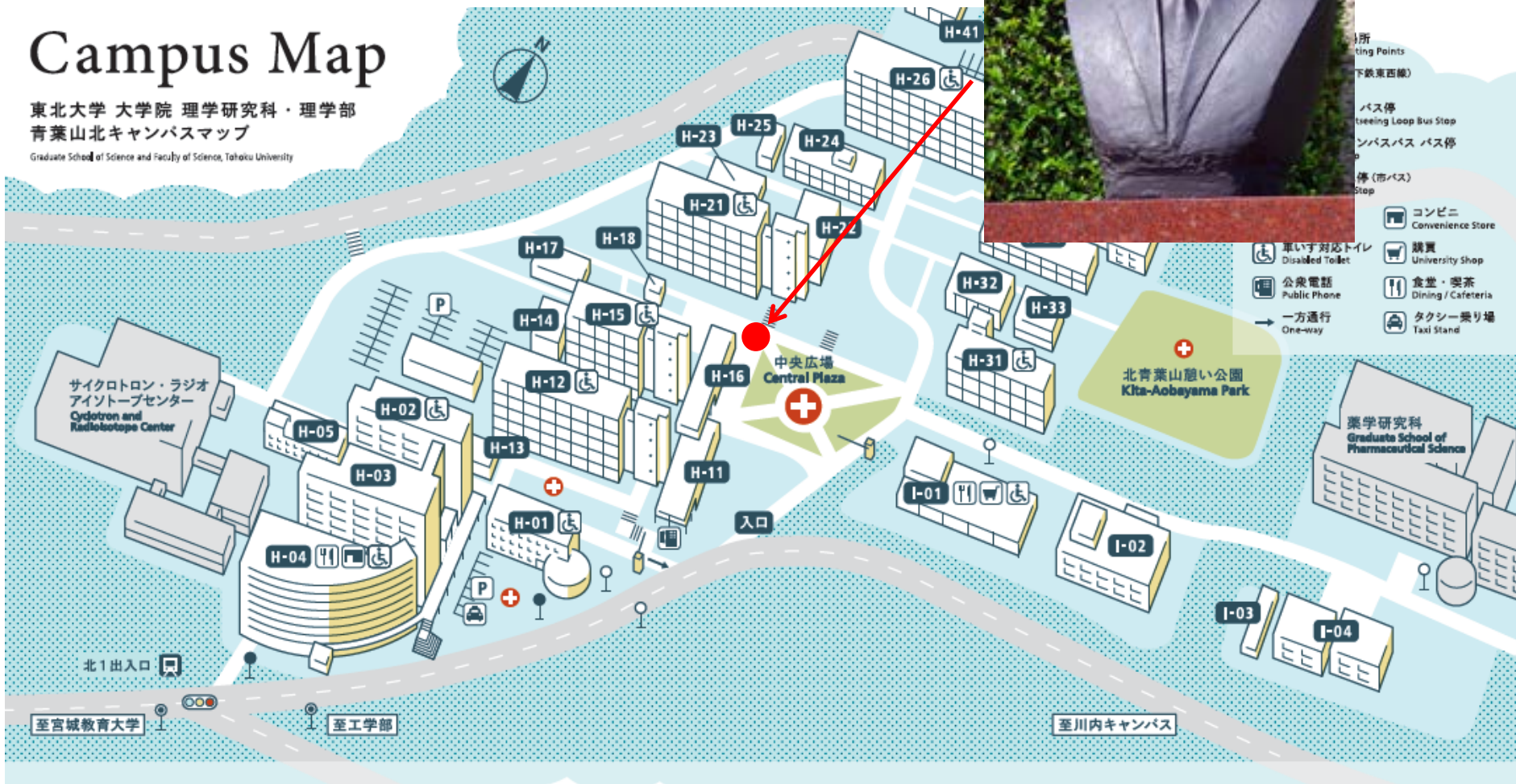
→ 日本に命名権
ニホニウム Nh



Campus Map

東北大学 大学院 理学研究科・理学部
青葉山北キャンスマップ

Graduate School of Science and Faculty of Science, Tohoku University



- 所 (Building)
- 停留点 (Waiting Points)
- 地下鉄東西線 (Subway Toei Line)
- バス停 (Bus Stop)
- 循環バス (Circulating Loop Bus Stop)
- キャンパスバス (Campus Bus Stop)
- 市バス (Municipal Bus Stop)
- コンビニ (Convenience Store)
- 購買 (University Shop)
- 食堂・喫茶 (Dining / Cafeteria)
- タクシー乗り場 (Taxi Stand)
- 車いす対応トイレ (Disabled Toilet)
- 公共電話 (Public Phone)
- 一方通行 (One-way)

理学研究科
Graduate School of
Pharmaceutical Science

北青葉山憩い公園
Kita-Aobayama Park

中央広場
Central Plaza

サイクロトロン・ラジオ
アイソトープセンター
Cyclotron and
Radiotope Center

至宮城教育大学

至工学部

至川内キャンパス

幻の元素、ニッポニウム (Np)

1908年:「43番目の元素」として新元素を発見し
ニッポニウム (Np) と命名したと発表。

→ その後疑問視され、周期表からは落とされる
(実は75番元素レニウム(当時未発見)だった)



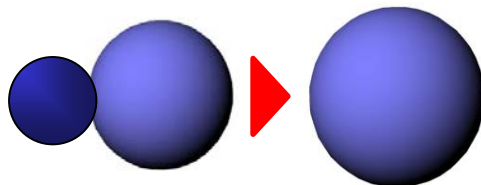
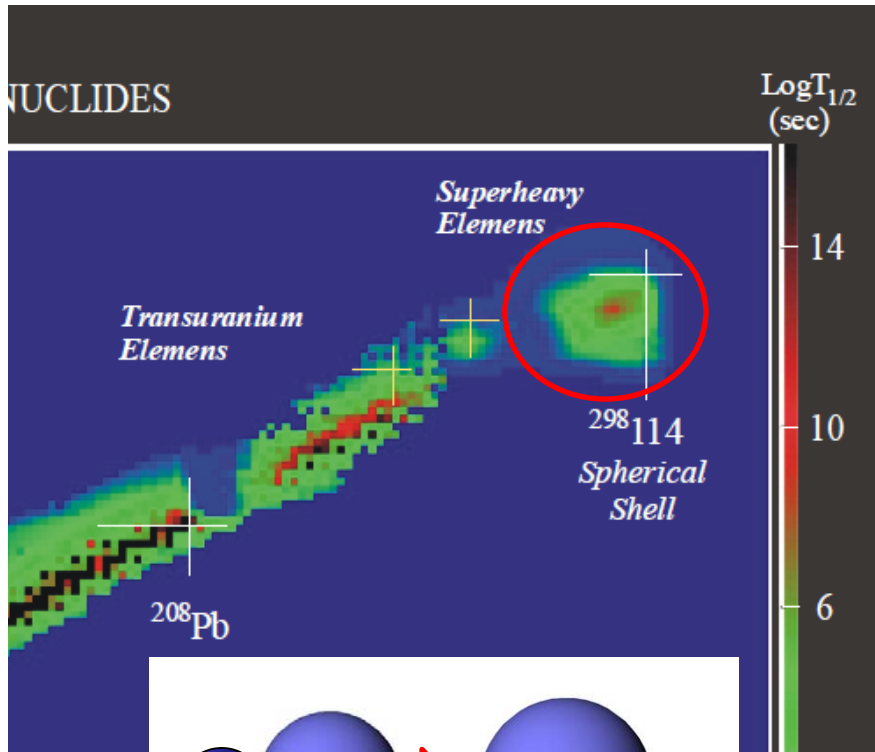
小川正孝
(1865－1930)



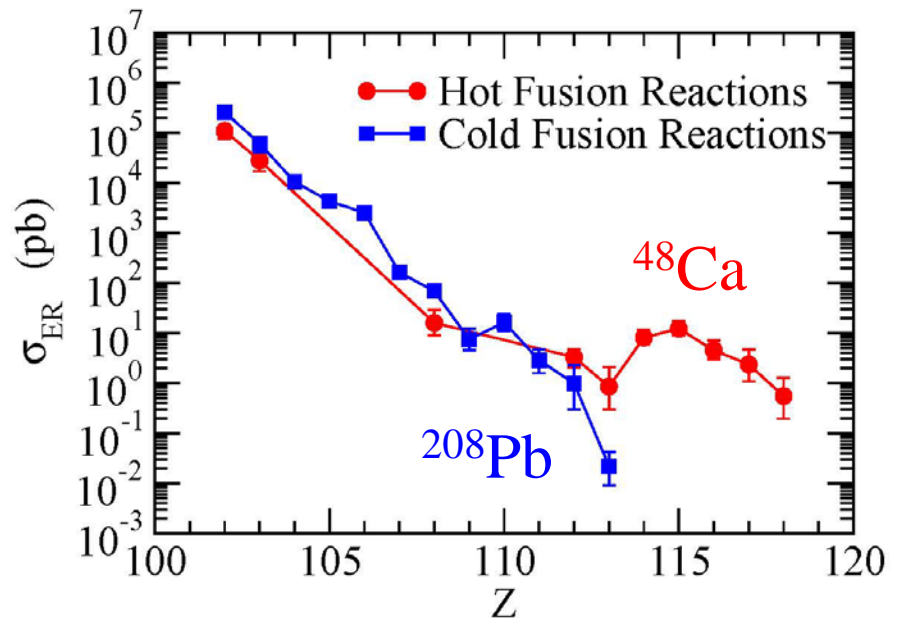
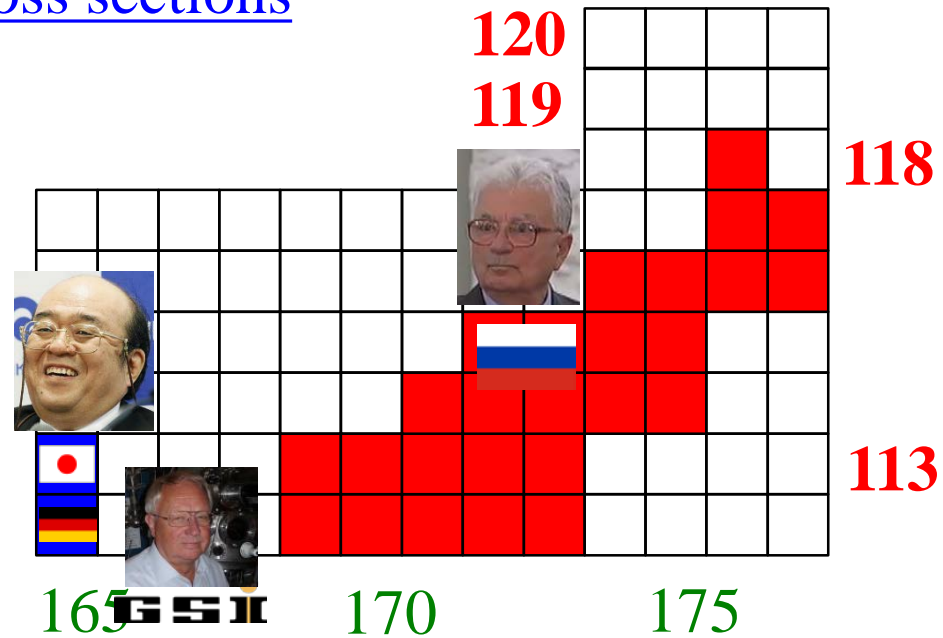
東北大学第4代総長
(1919－1928)

ニホニウム Nh は
この時以来の悲願
達成！

hot/cold fusion: a comparison of cross sections

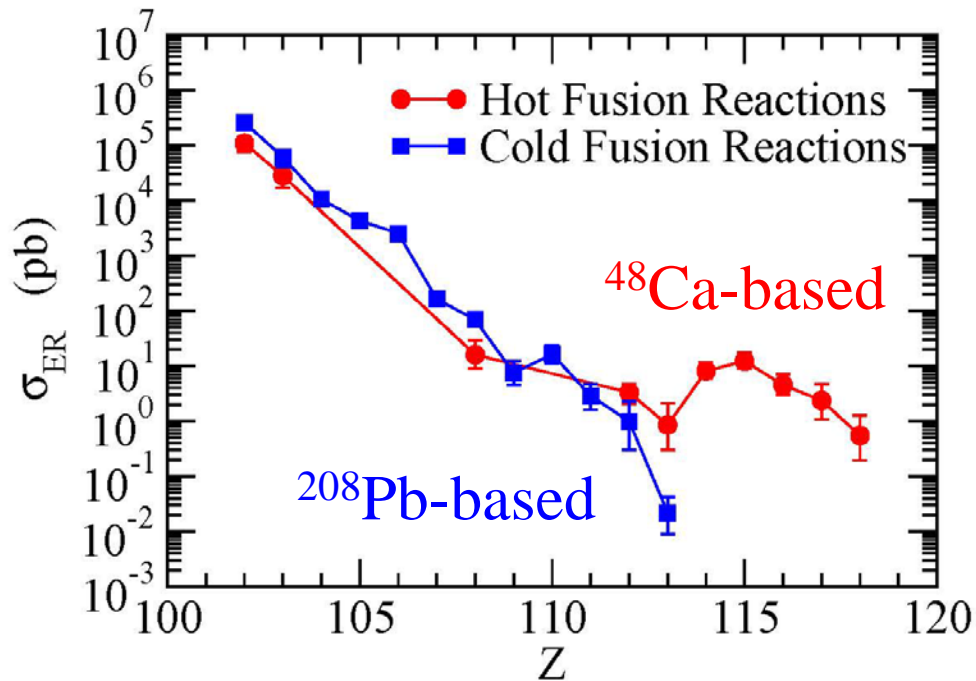
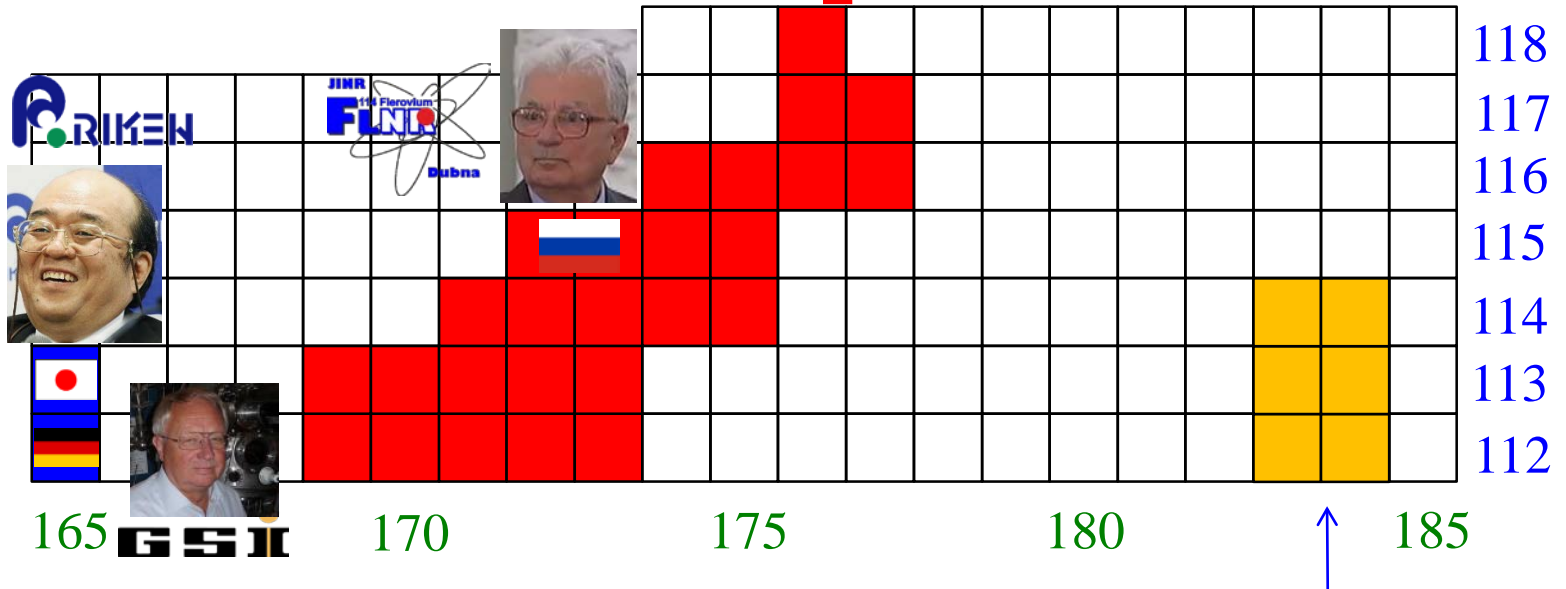


fusion reaction



Hot fusion reactions: ^{48}Ca +actinides

$Z = 119$ and 120



the island of stability?

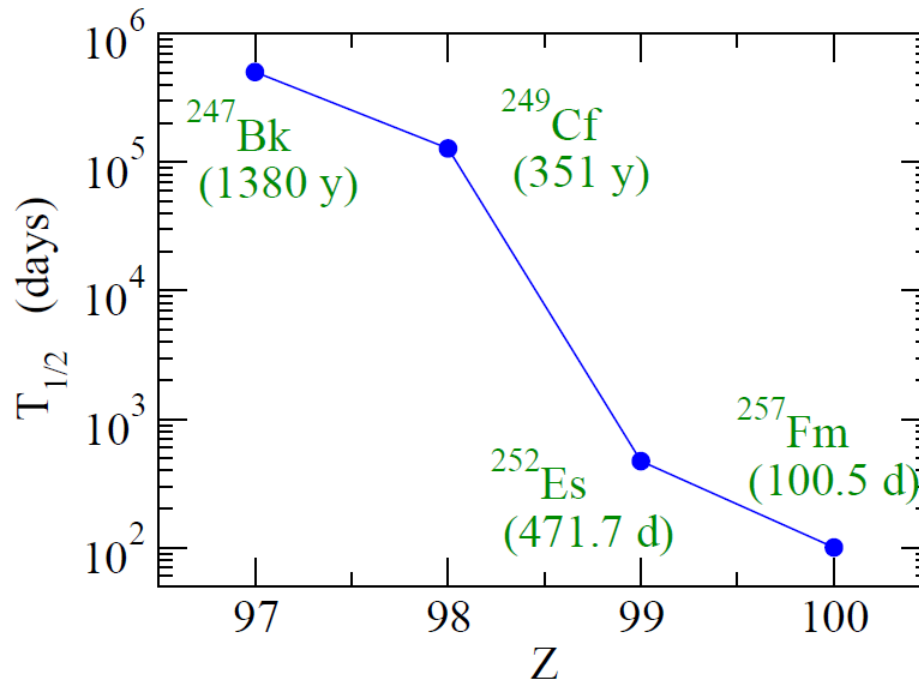
Hot fusion for $Z = 119$ and 120

Towards Z=119 and 120 nuclei

hot fusion reactions with ^{48}Ca :



short lived \rightarrow not available with
sufficient amounts

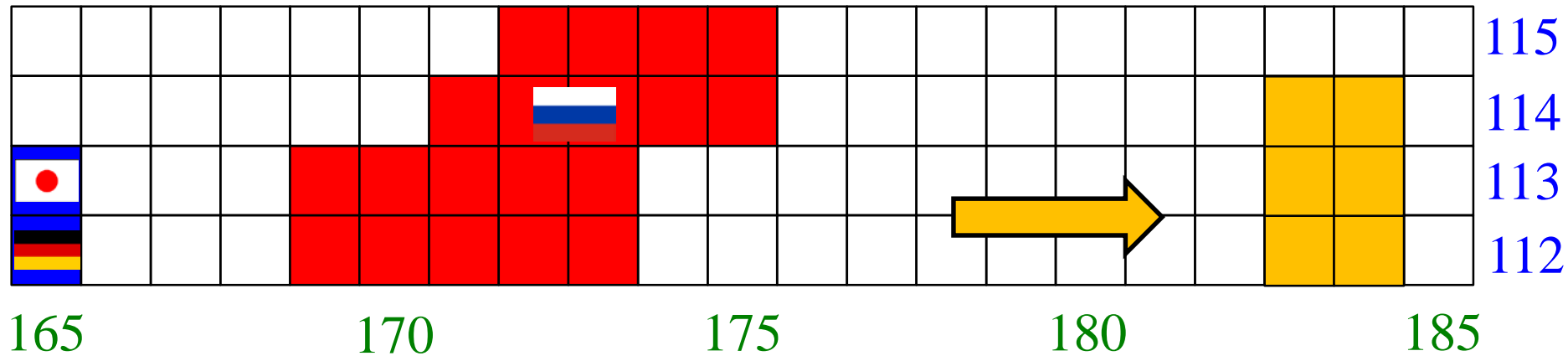


$^{48}\text{Ca} \rightarrow {}^{50}_{22}\text{Ti}, {}^{51}_{23}\text{V}, {}^{54}_{24}\text{Cr}$ projectiles

closed shell \rightarrow open shells

how much will
cross sections be affected?

Towards the island of stability



neutron-rich beams: indispensable

- how to deal with low beam intensity?
- reaction dynamics of neutron-rich beams?
 - ✓ capture: role of breakup and (multi-neutron) transfer?
 - ✓ diffusion: neutron emission during a shape evolution?
 - ✓ survival: validity of the statistical model?

structure of exotic nuclei

more studies are required

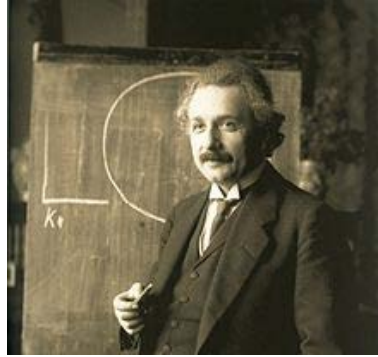
Chemistry of superheavy elements

Group →	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
↓ Period																		
1	1 H																	2 He
2	3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne
3	11 Na	12 Mg											13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
4	19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
5	37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
6	55 Cs	56 Ba	57 La	* 72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
7	87 Fr	88 Ra	89 Ac	* 104 Rf	* 105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
				* 58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	
				* 90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	

- Are they here in the periodic table?
- Does Nh show the same chemical properties as B, Al, Ga, In, and Tl?

relativistic effect : important for large Z

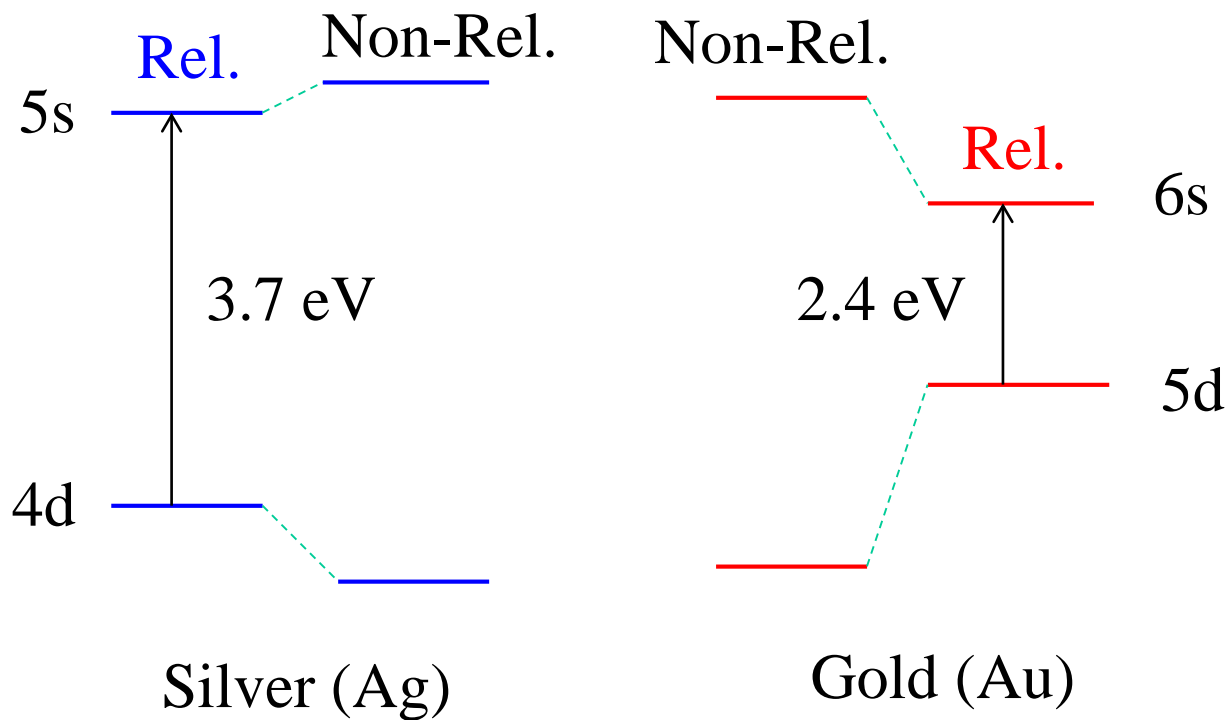
$$E = mc^2$$



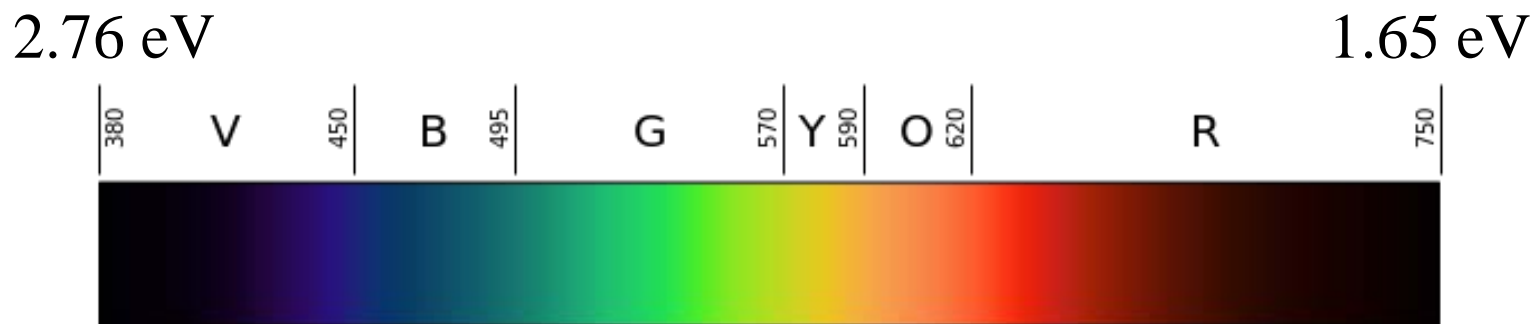
Solution of the Dirac equation (relativistic quantum mechanics)
for a hydrogen-like atom:

$$E_{1S} = mc^2 \sqrt{1 - (Z\alpha)^2} \sim mc^2 \left(1 - \frac{(Z\alpha)^2}{2} - \underbrace{\frac{(Z\alpha)^4}{8} + \dots}_{\text{relativistic effect}} \right)$$

relativistic effect

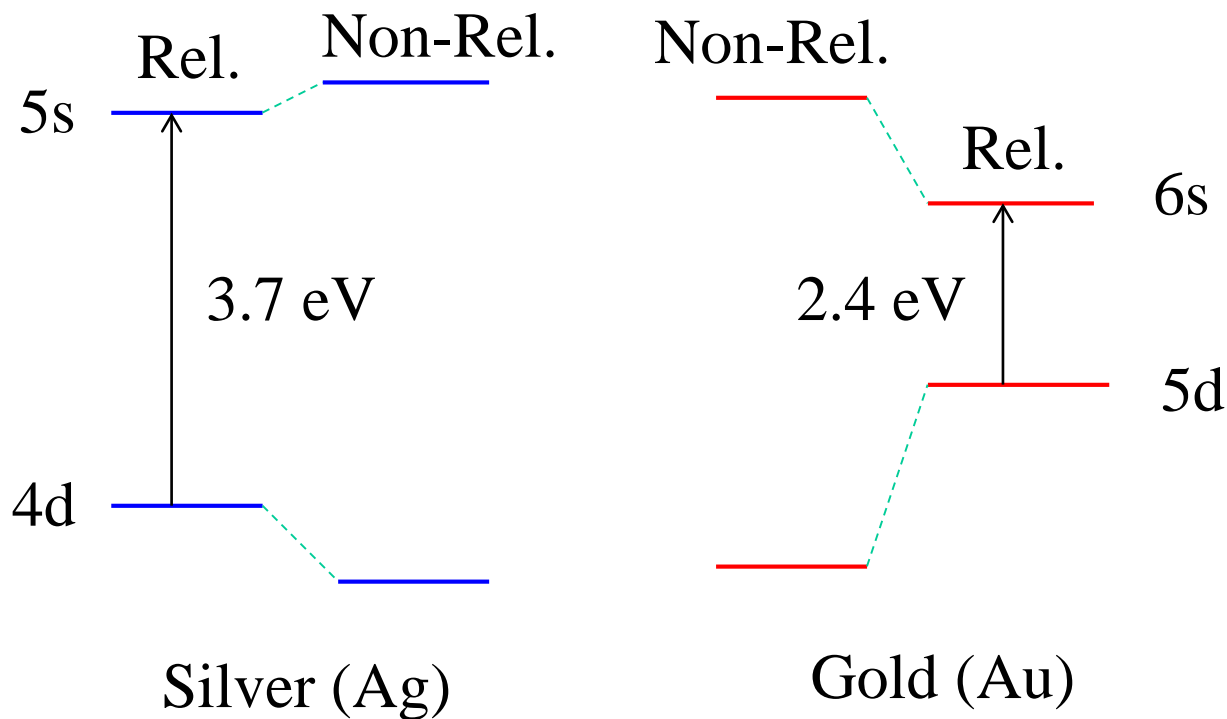


cf. visible spectrum



↑
3.7 eV

↑
2.4 eV



cf. visible spectrum

3.7 eV 2.76 eV 2.4 eV 1.65 eV



← absorbed (Au)

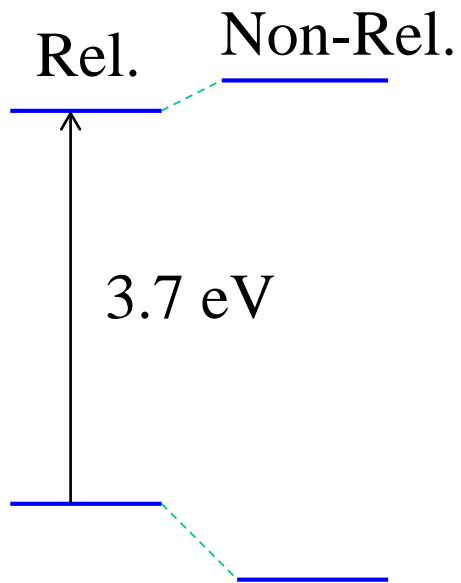
→ reflected (Au)

→ reflected (Ag)



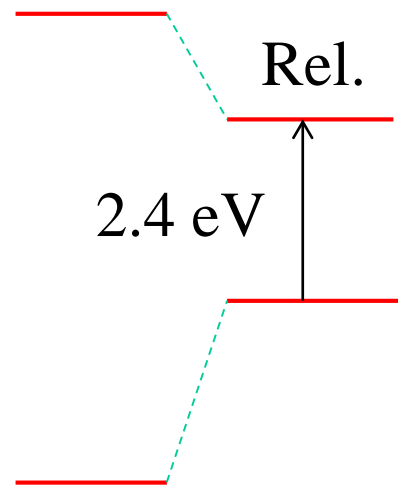


no color
absorbed

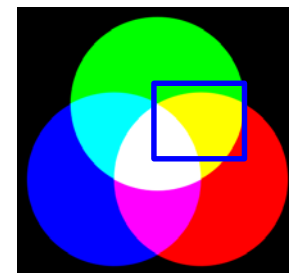


Silver (Ag)

Non-Rel.



Gold (Au)



blue: absorbed



Ag



Au

Chemistry of superheavy elements

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				* 90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	

How do the relativistic effects alter the periodic table for SHE?

→ a big open question