

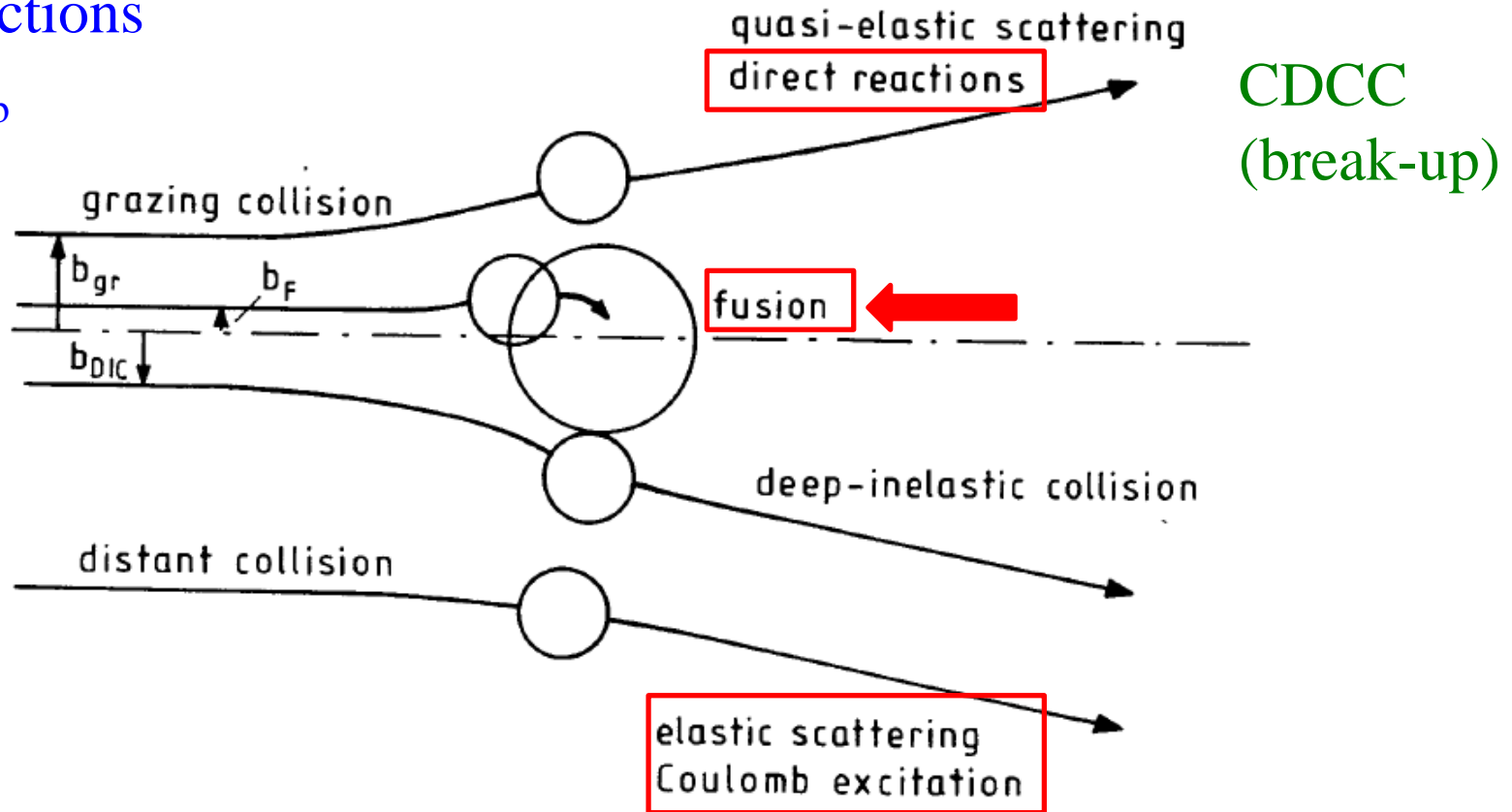
# Reactions with heavy nuclei



Kouichi Hagino

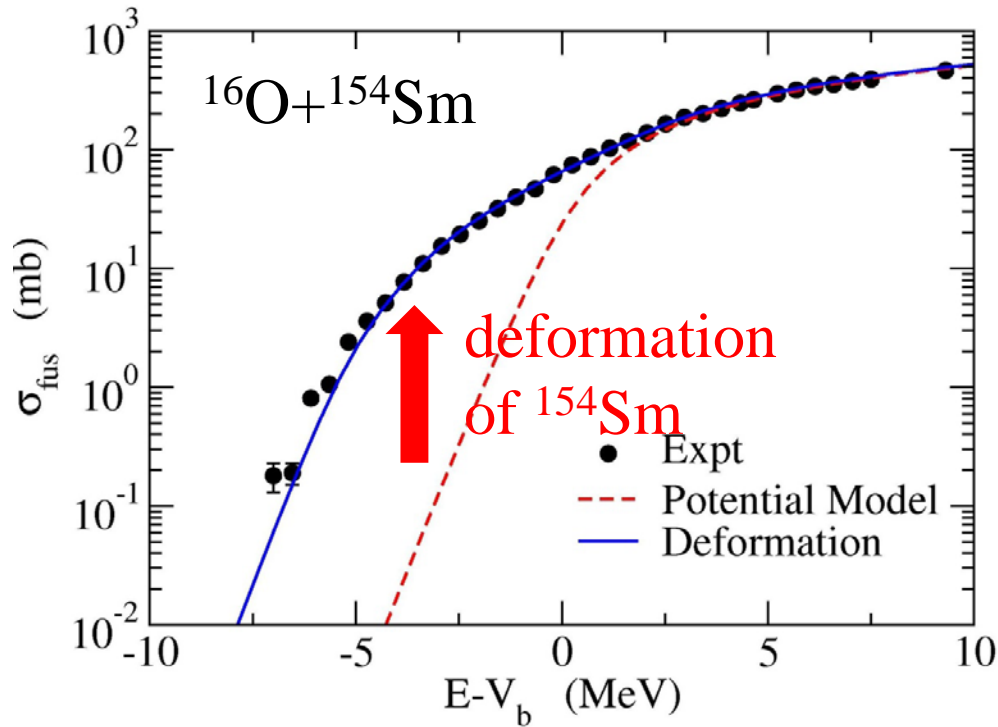
*Tohoku University, Sendai, Japan*

H.I. Reactions  
at  $E > V_b$



“Theory of Nuclear Reactions” Frobrich and Lipperheide

◆ H.I. Sub-barrier fusion reactions ( $Z_P * Z_T < 1600$ )



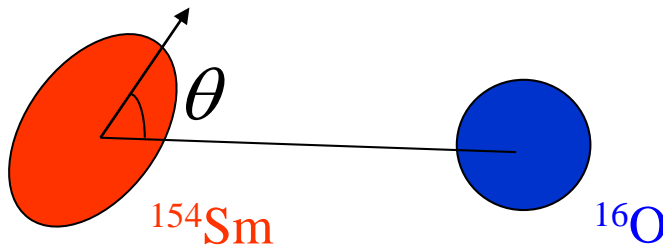
collective excitations  
during fusion



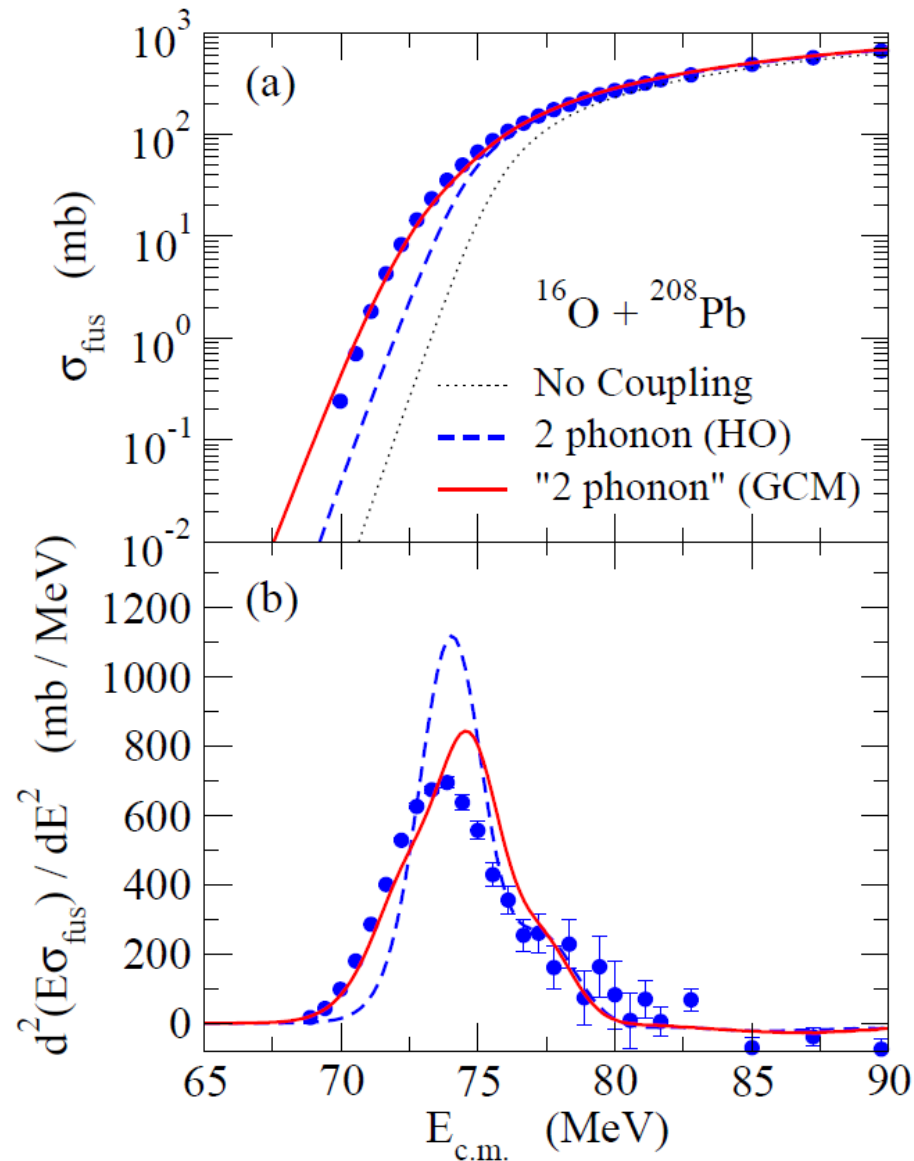
**coupled-channels method**

- ✓ excitation energies
- ✓ transition strengths
- ✓ multi-phonon excitations  
or g.s. rotational band

$$\sigma_{\text{fus}}(E) = \int_0^1 d(\cos \theta) \sigma_{\text{fus}}(E; \theta)$$

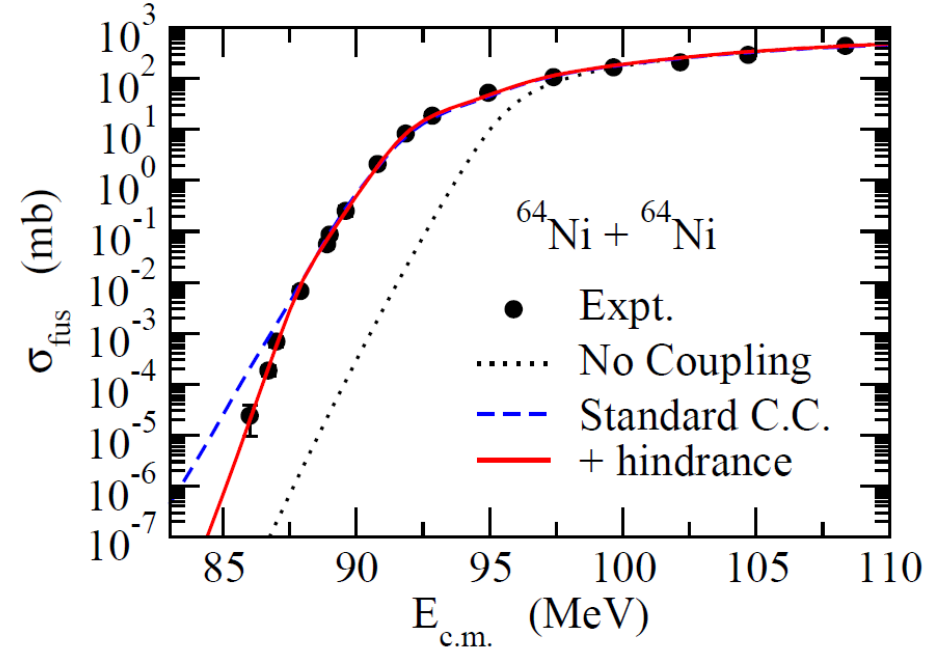
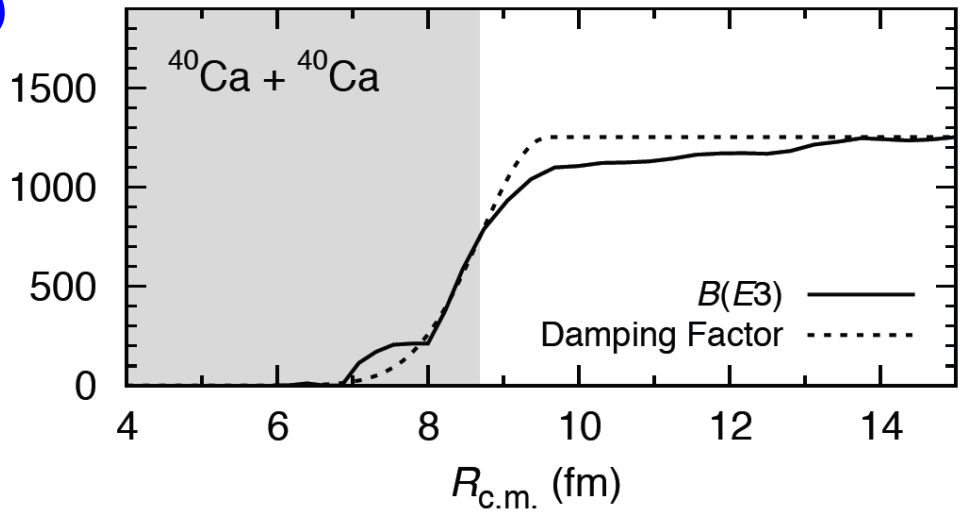


✓ C.C. with a state-of-the-art nuclear structure calculation (beyond-MF)



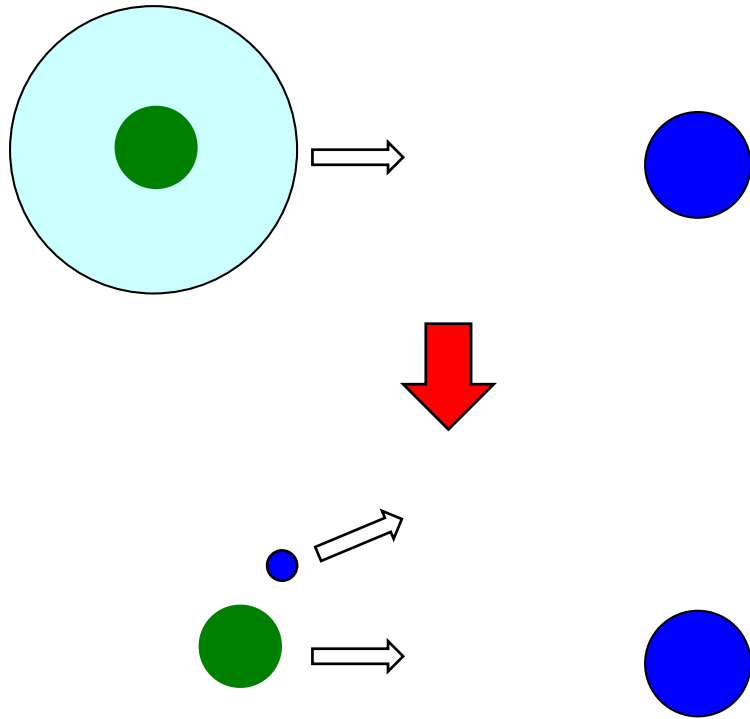
J.M. Yao and K.H. (2016)

✓ C.C. with RPA



T. Ichikawa and K. Matsuyanagi  
PRC88('13) 011602(R)

# Fusion of halo nuclei



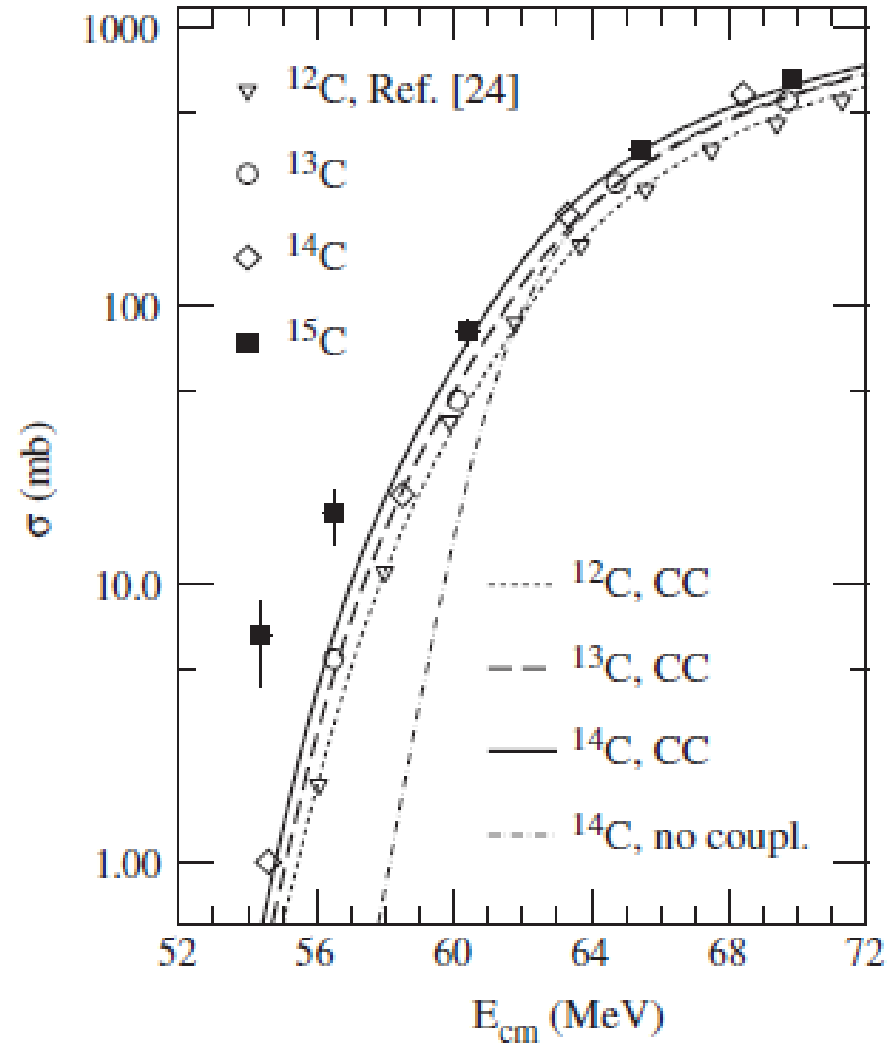
1. Lowering of potential barrier  
due to a halo structure

→ enhancement

2. effect of breakup

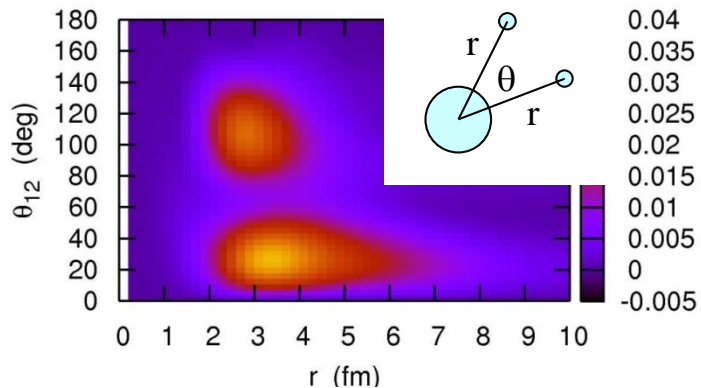
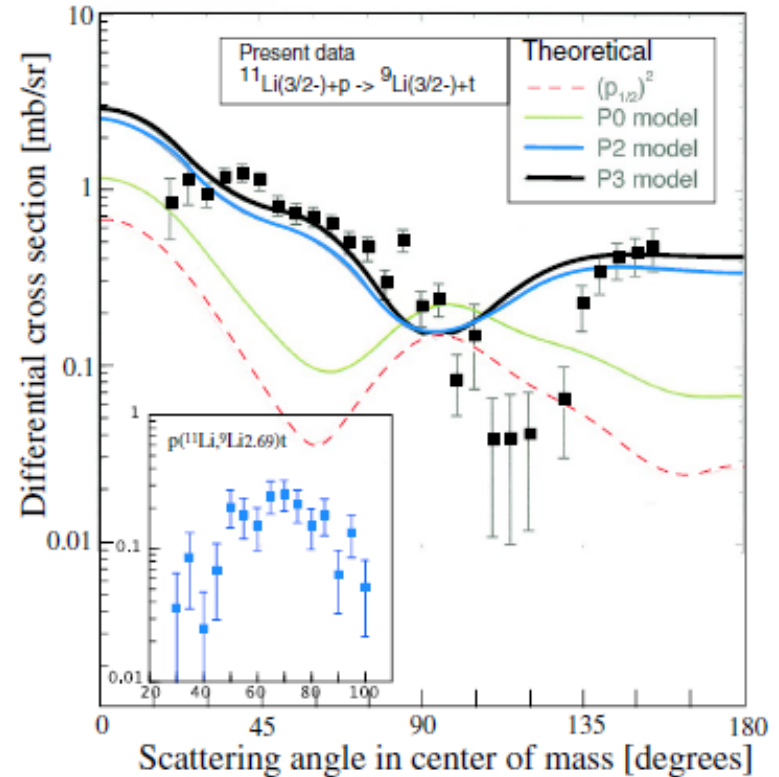
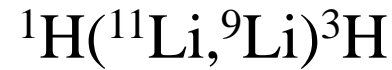
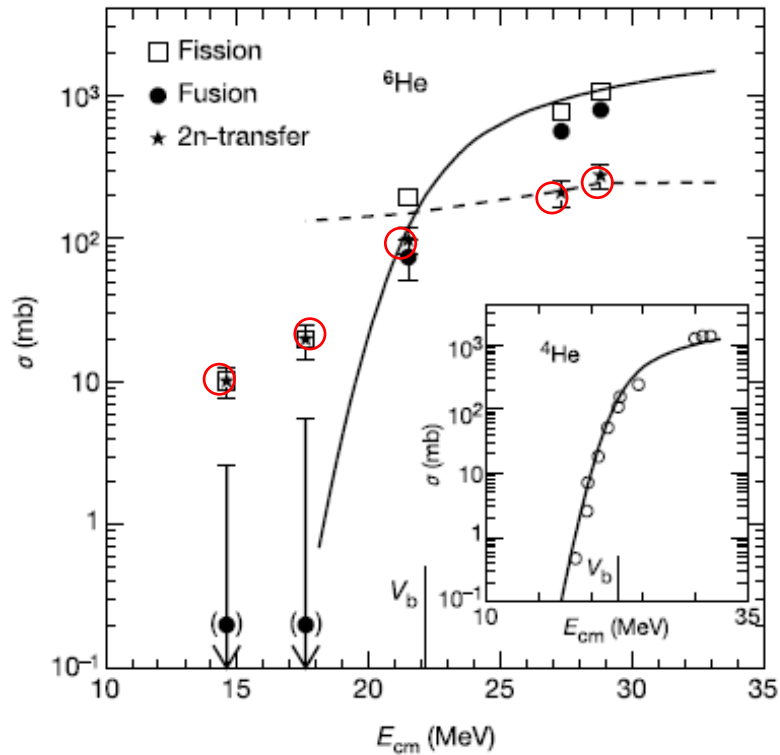
3. effect of transfer

$^{12,13,14,15}\text{C} + ^{232}\text{Th}$



M. Alcorta et al.,  
PRL106('11)172701

# Two-neutron transfer reactions: pairing correlations

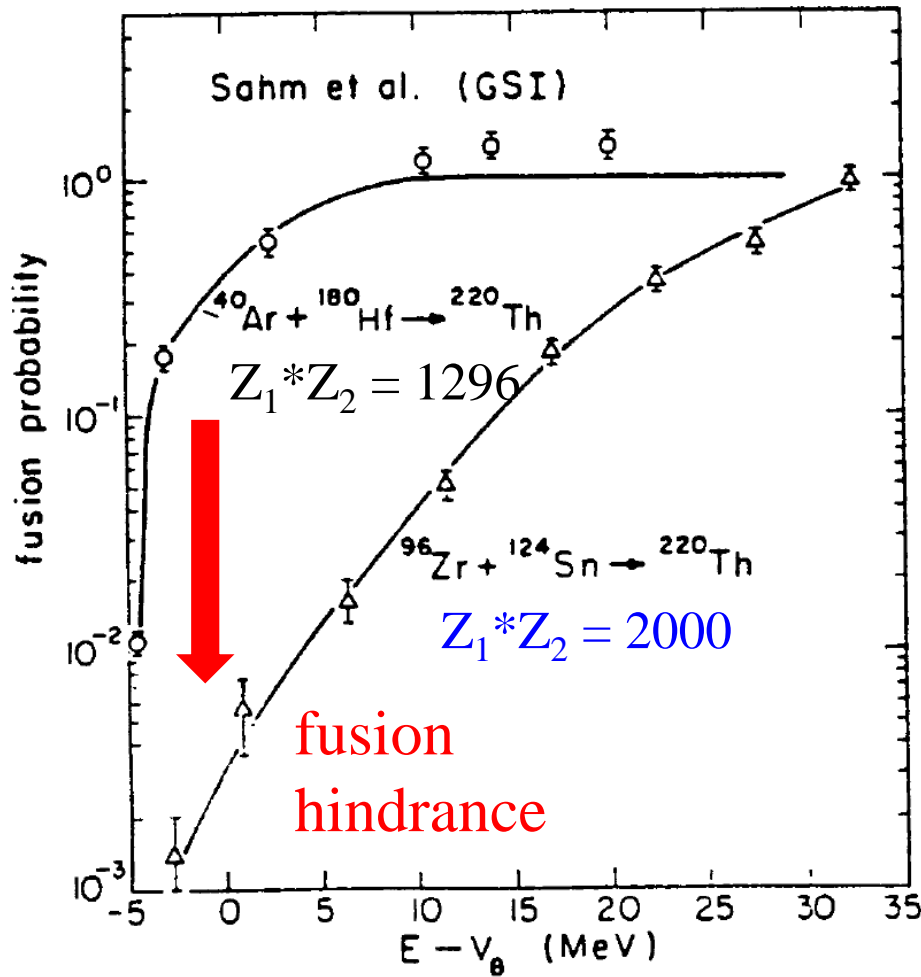


I. Tanihata et al., PRL100('08)192502

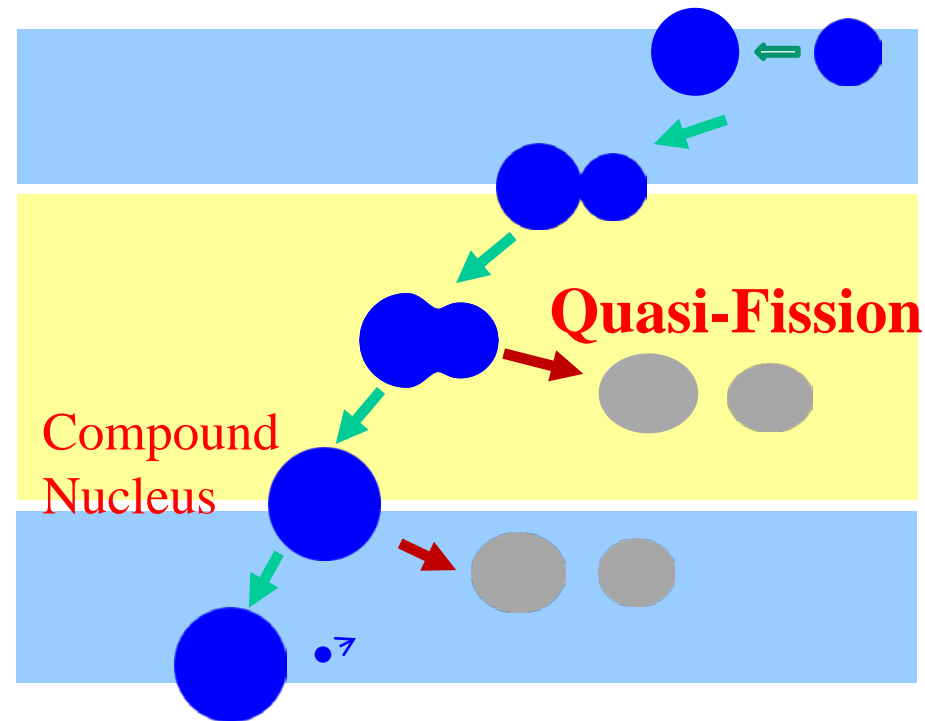
- ✓ reaction mechanics?
- ✓ role of unbound intermediate states?

◆ H.I. Sub-barrier fusion reactions ( $Z_P * Z_T > 1600 \sim 1800$ )

fusion hindrance



modern understanding



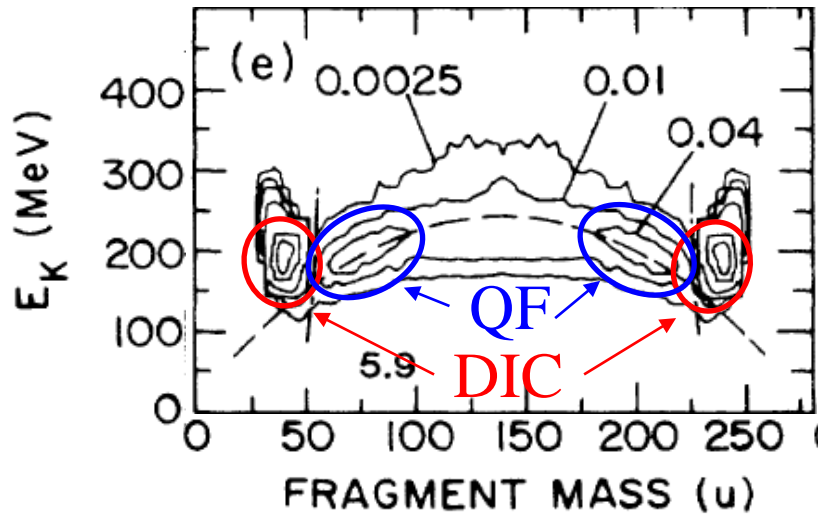
re-separation before CN  
 = Quasi-Fission

C.-C. Sahm et al.,  
 Z. Phys. A319('84)113

closely related phenomenon: deep inelastic collision (~ 70-80's)

$^{40}\text{Ca} + ^{238}\text{U}$  ( $E = 5.9 \text{ MeV/A}$ )

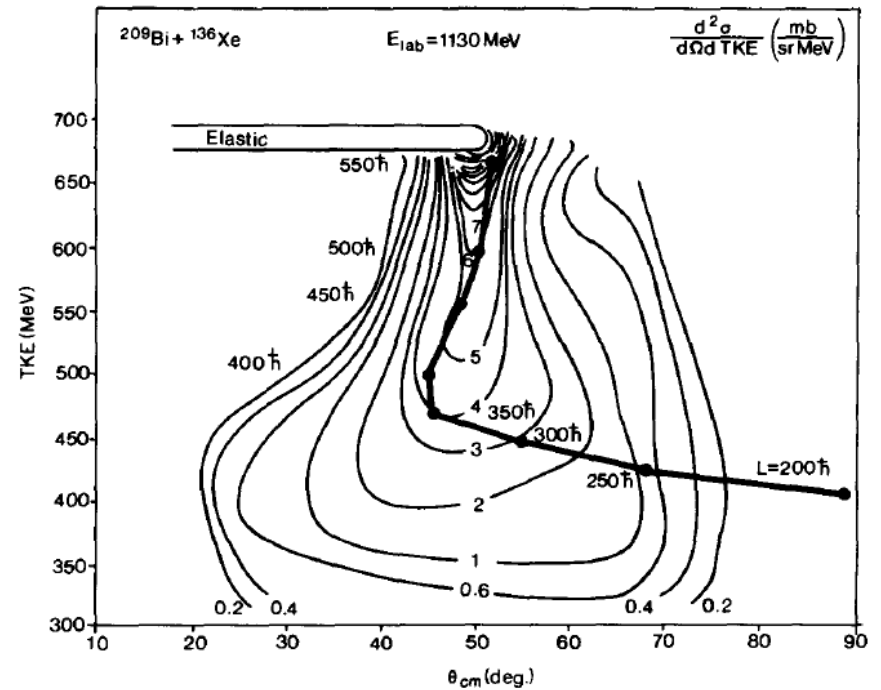
highly damped reaction



W.Q. Shen et al., PRC36('87)115

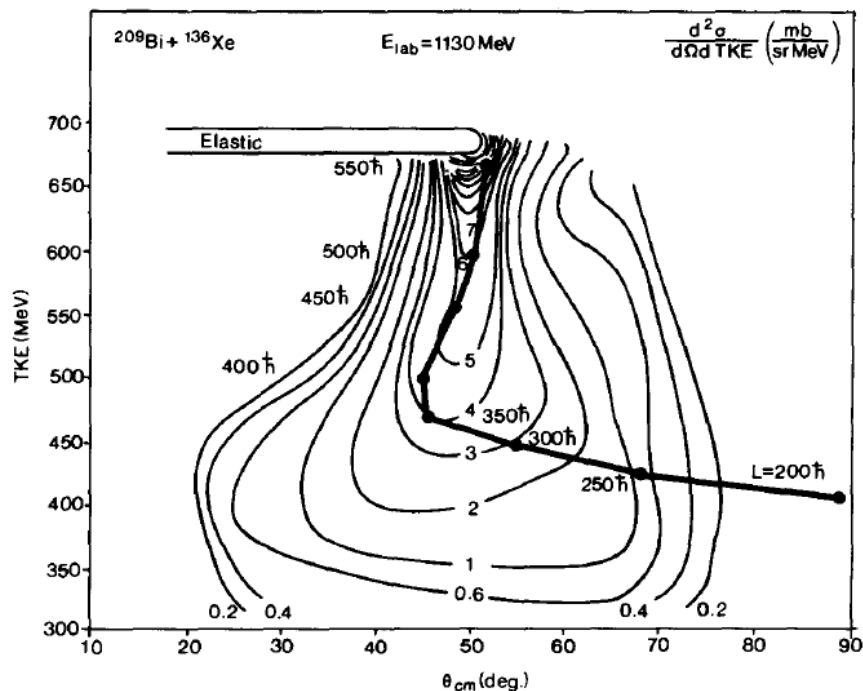
- ✓ many phenomenological models
- ✓ TDHF

a big success of TDHF:



A.K. Dhar, B.S. Nilsson,  
K.T.R. Davies and S.E. Koonin,  
NPA364 ('81)105

a big success of TDHF for DIC



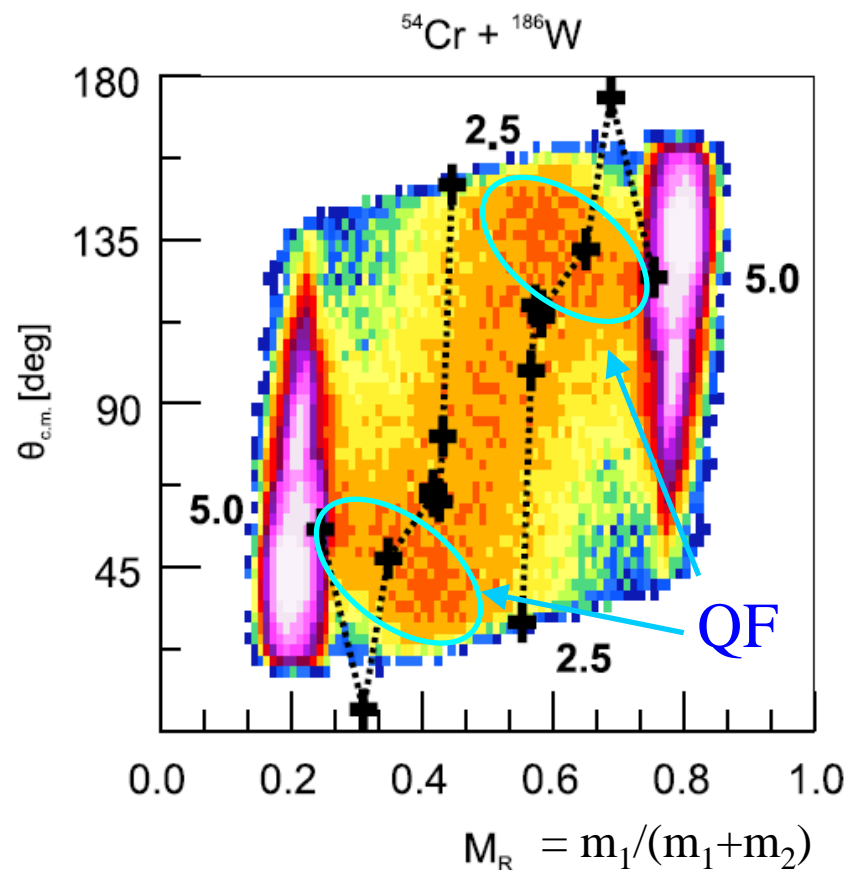
A.K. Dhar, B.S. Nilsson,  
K.T.R. Davies and S.E. Koonin,  
NPA364 ('81)105

➤ nuclear friction from TDHF

K. Washiyama, D. Lacroix, and  
S. Ayik, PRC79('09)024609

TDHF seems to work for  
QF as well

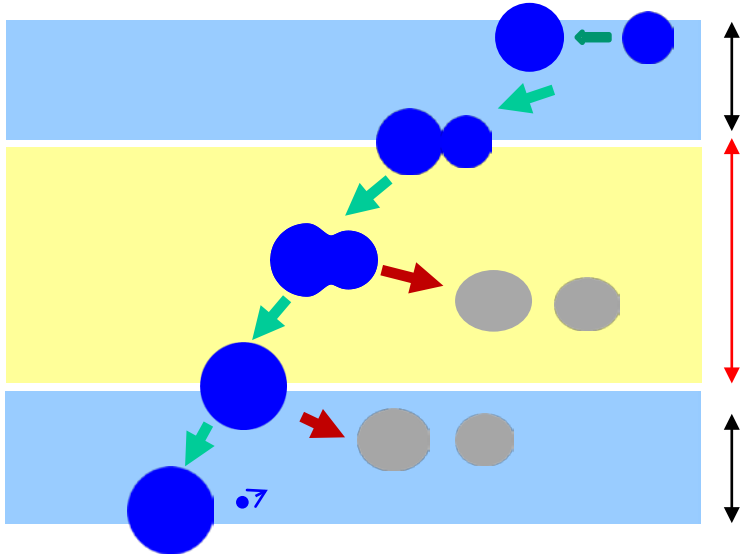
mass-angle distribution



A.S. Umar and V.E. Oberacker,  
NPA944('15)238  
c.f. expt.: ANU group (D.J. Hinde et al.)



# Super-heavy nuclei



coupled-channels method

Langevin approach

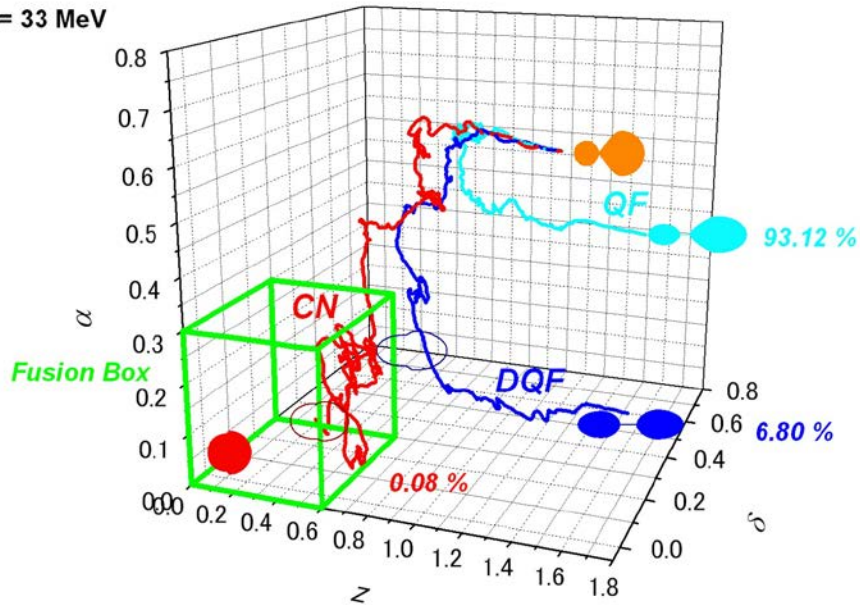
V.I. Zagrebaev and W. Greiner, NPA944('15)257

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

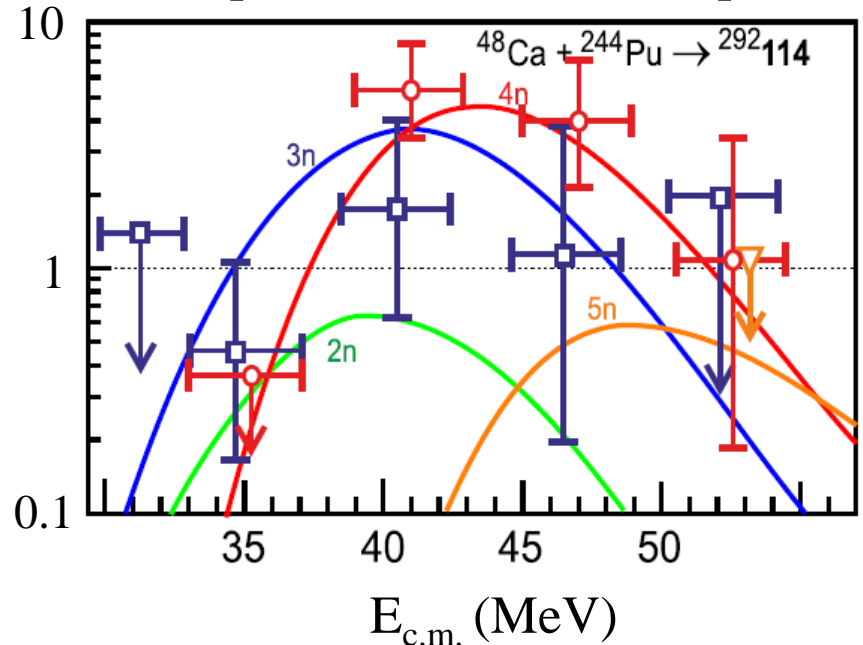
statistical model

$^{48}\text{Ca} + ^{244}\text{Pu} \rightarrow ^{292}\text{114}$

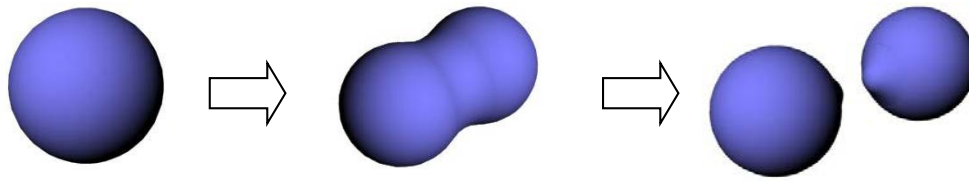
$E^* = 33 \text{ MeV}$



Evap. resid. cross section (pb)

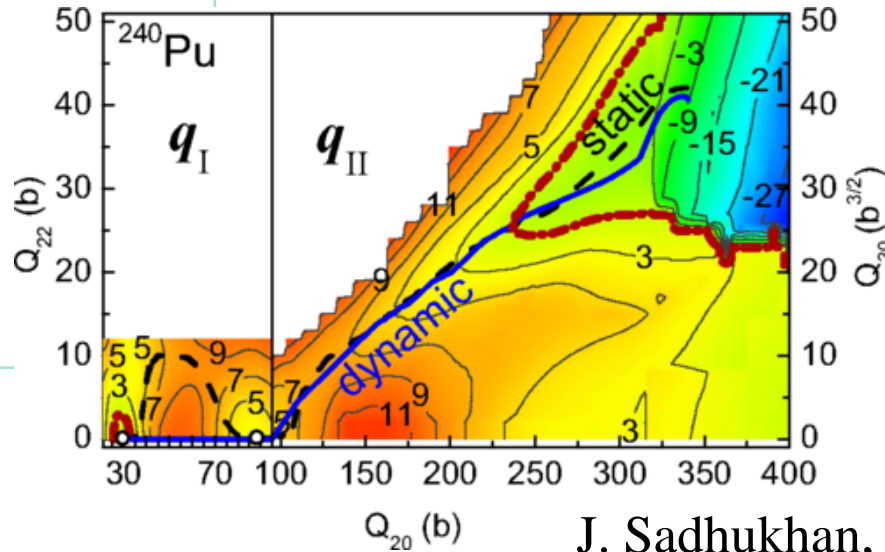


# Fission



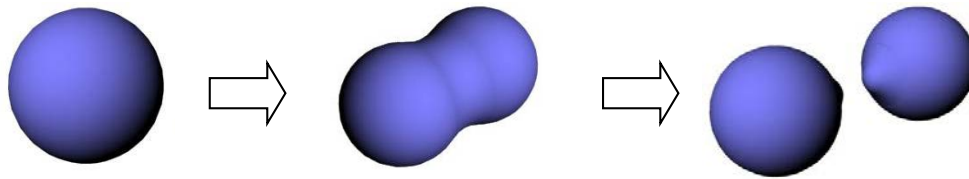
still a very challenging problem for nuclear theory

	<b>Time-indep. approach</b>	<b>Time-dep. approach</b>
Induced fission	✓ Bohr-Wheeler	✓ Langevin-type ✓ Discrete basis (Bertsch)
Spontaneous fission	✓ PES+Mass+WKB	✓ Im.-time TDHF (Negele) ✓ Time-dep. Hill-Wheeler (Goutte et al.) ✓ TDHF (after the barrier)



J. Sadhukhan, W. Nazarewicz, N. Schunck,  
PRC93('16)011304(R)

## Fission



still a very challenging problem for nuclear theory

	<b>Time-indep. approach</b>	<b>Time-dep. approach</b>
<b>Induced fission</b>	✓ Bohr-Wheeler	✓ Langevin-type ✓ Discrete basis (Bertsch)
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issues:

- which degrees of freedom? (time-indep. approaches)
- how to deal with many-body tunneling? (time-dep. approaches)

## Summary and discussions

### ➤ Heavy-ion reactions around the Coulomb barrier : strong interplay between structure and reaction

- sub-barrier fusion reactions (coupled-channels effects)
- fusion of massive nuclei (nuclear friction)
- spontaneous and induced fissions
- **two-neutron transfer (pairing correlations)**

### ➤ From phenomenological models to more microscopic models

- C.C. with microscopic inputs
- DFT for spontaneous fission
- TDHF approach ←

### ➤ “Beyond mean-field” approximations

Full time-dependent GCM?  $|\Psi(t)\rangle = \int dq f(q, t) |\Phi_q(t)\rangle$   
→ many-body tunneling

cf. “Quantum tunneling using entangled classical trajectories”

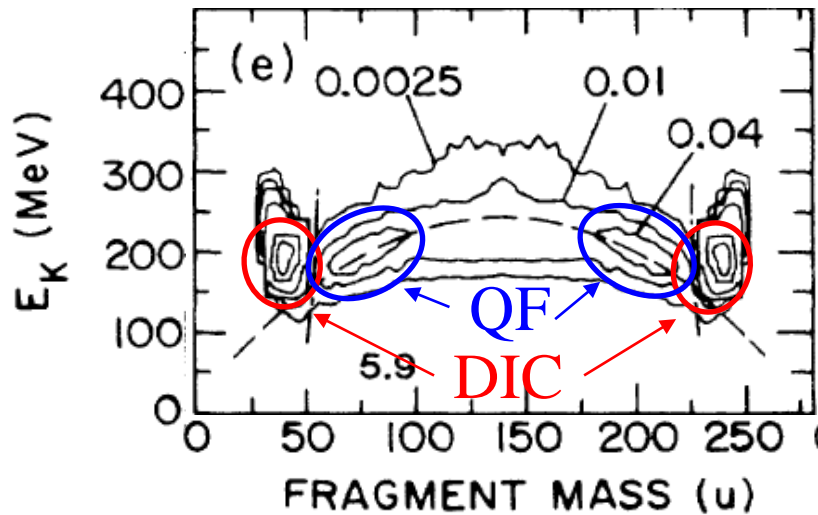
A. Donoso and C.C. Martens, PRL87 ('01) 223202



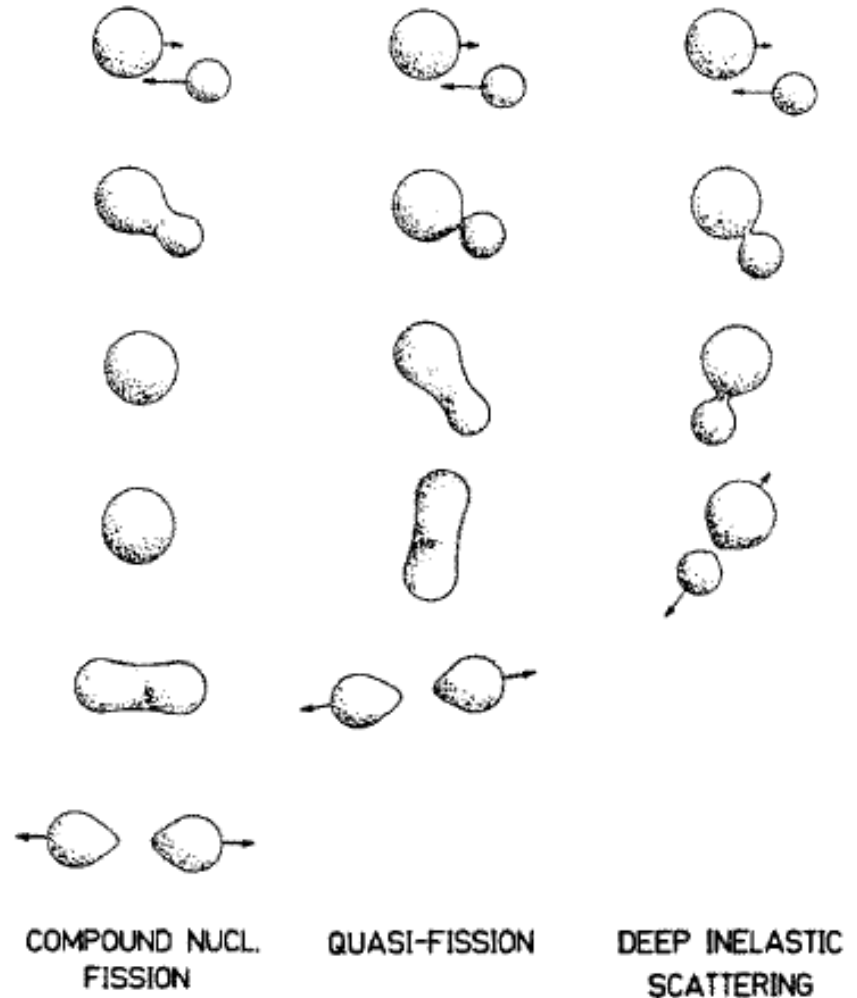
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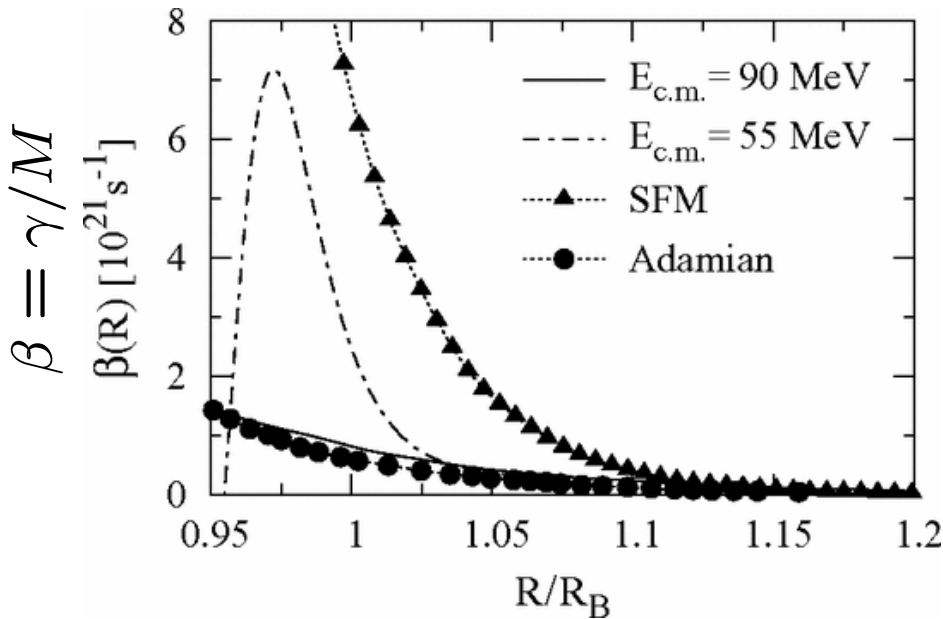
W.Q. Shen et al., PRC36('87)115



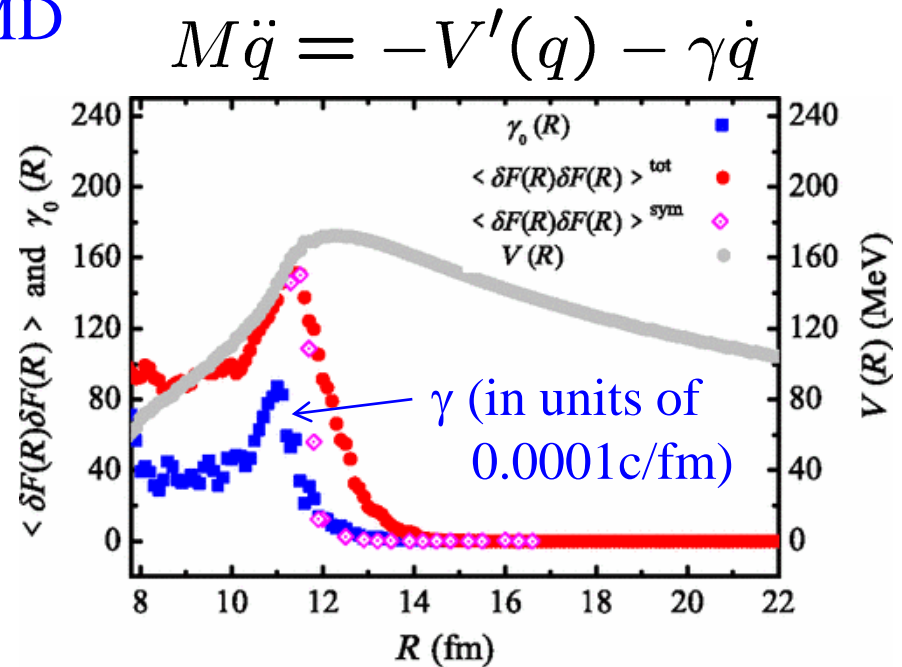
J. Toke et al., NPA440('85)327

## nuclear friction

- damping of giant resonances
- neutron induced fission (Kramers factor)
- deep-inelastic collisions and quasi-fission
  - ✓ wall-and-window formula
  - ✓ linear response theory
  - ✓ attempts with TDHF and QMD



K. Washiyama, D. Lacroix, and  
S. Ayik, PRC79('09)024609



K. Wen et al., PRL111('13)012501