

Particle-rotation/vibration couplings in hypernuclei



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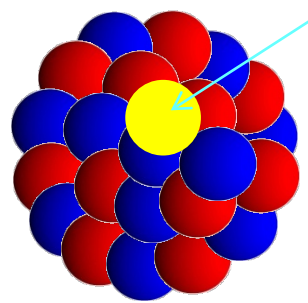


- 1. Introduction: hypernuclei*
- 2. Microscopic particle-core coupling schemes for hypernuclei*
- 3. Spectrum of Λ hypernuclei*
- 4. Summary*

Introduction

Λ hypernucleus

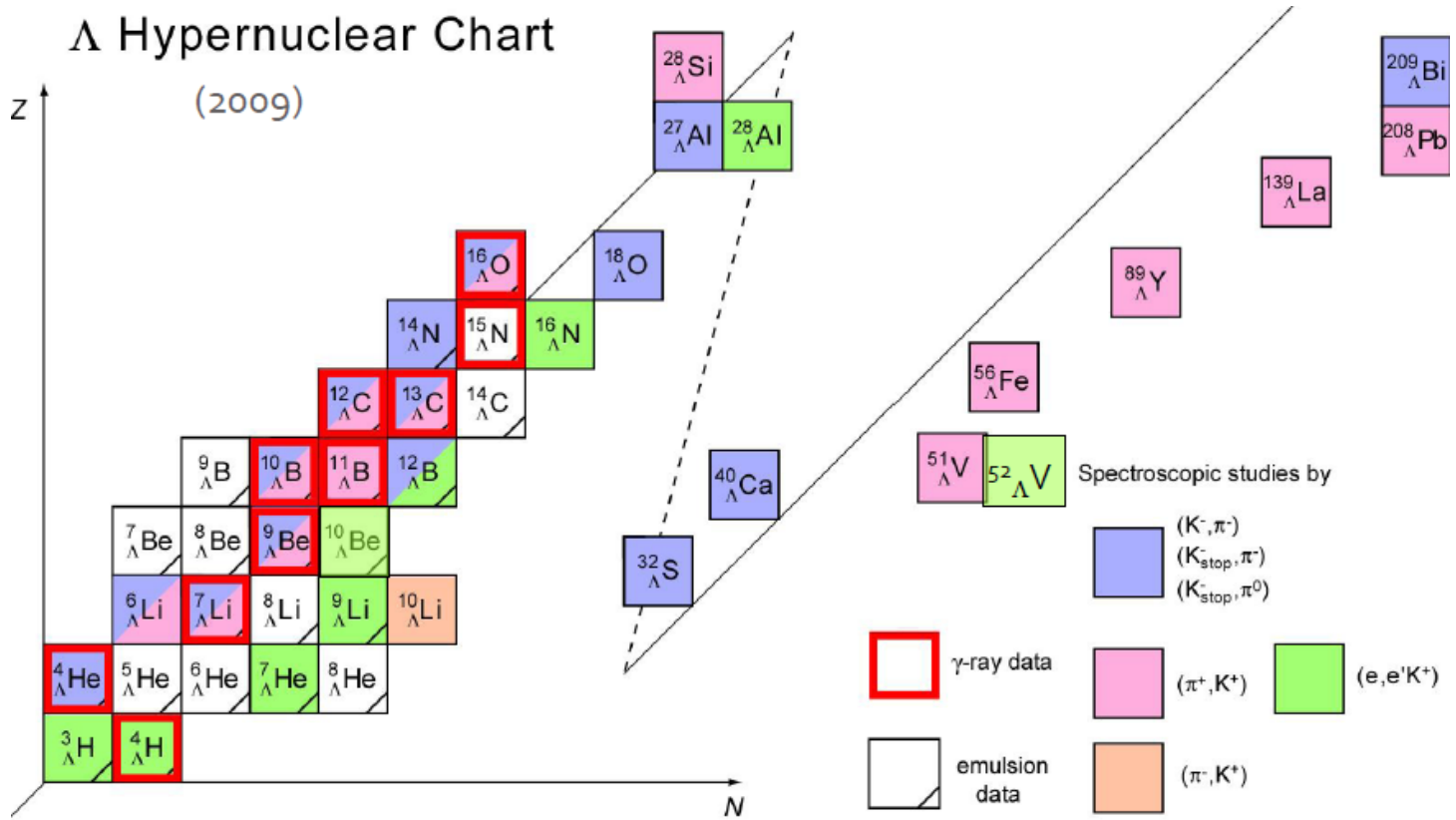
Λ particle: the lightest hyperon
(no charge, no isospin)

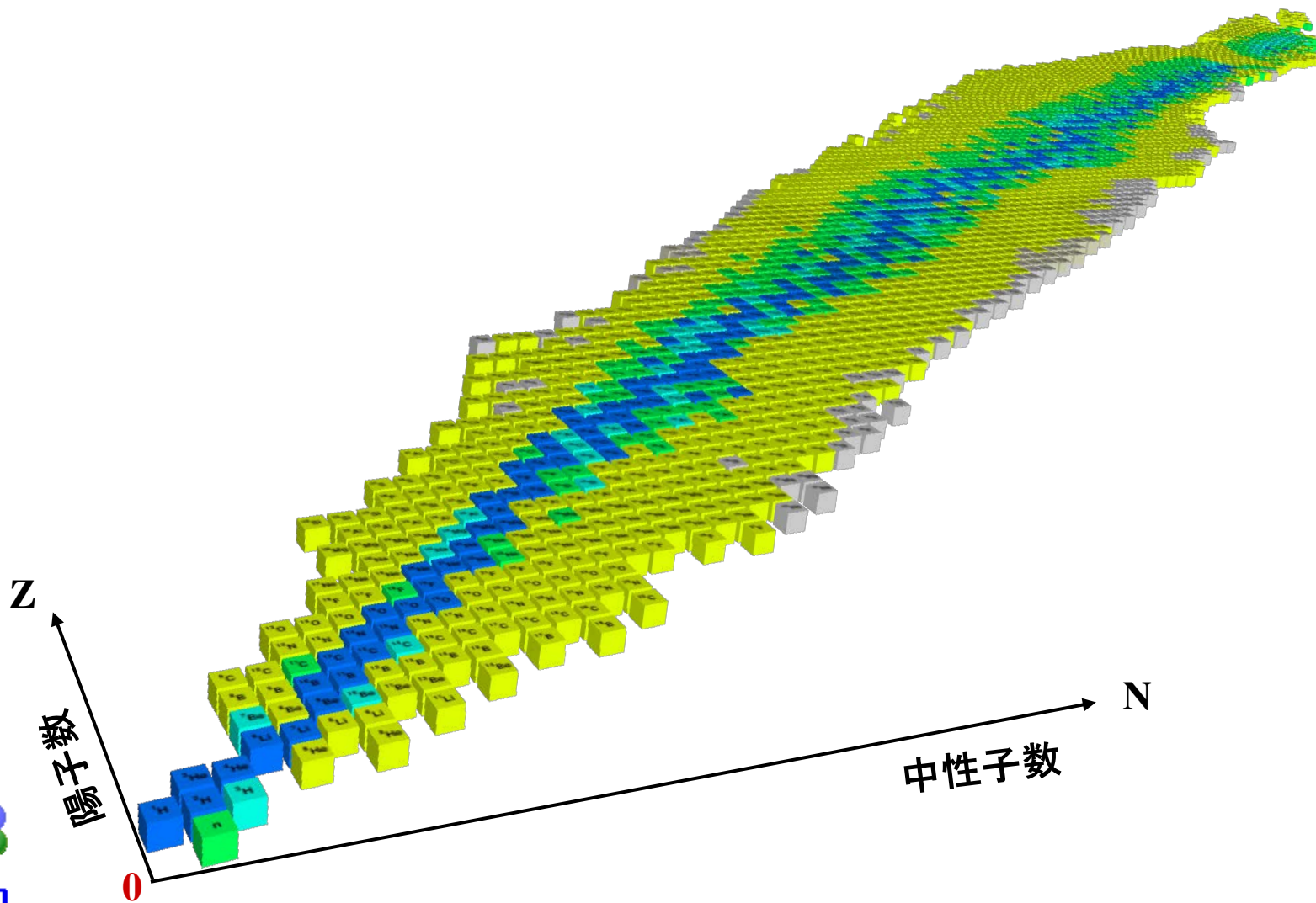


proton

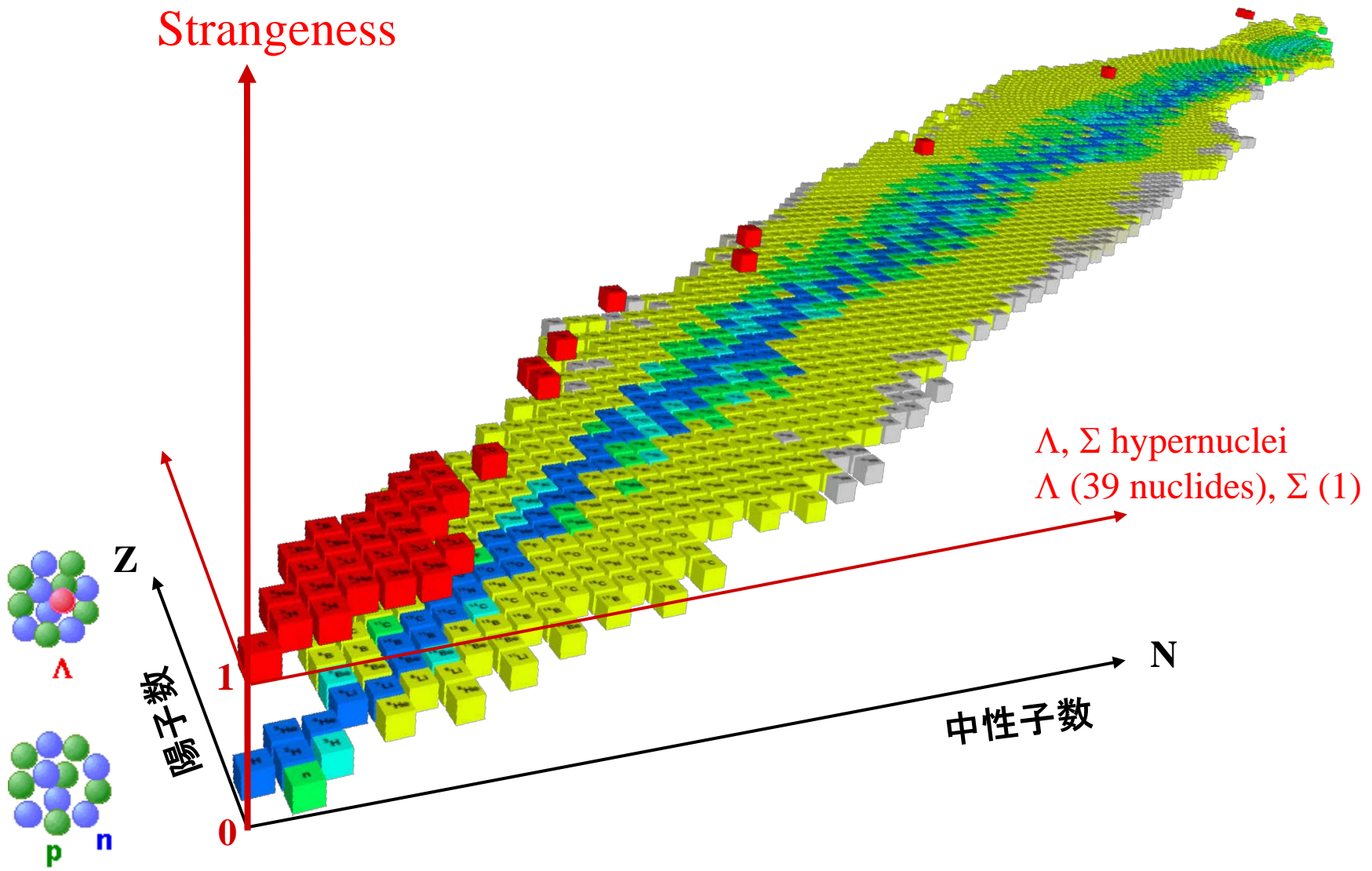
neutron

*no Pauli principle between nucleons and a Λ particle

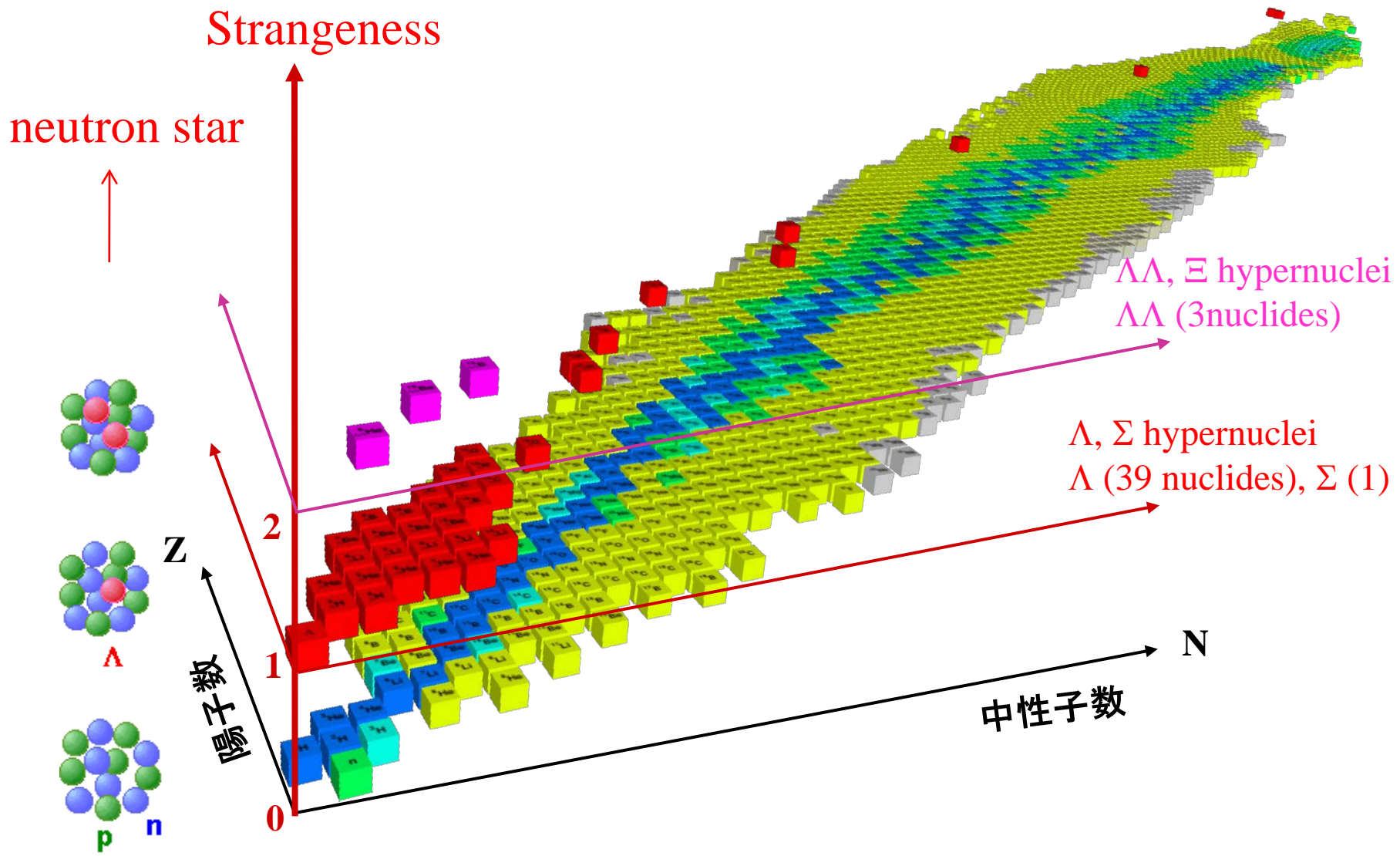




Strangeness



Λ, Σ hypernuclei
 Λ (39 nuclides), Σ (1)

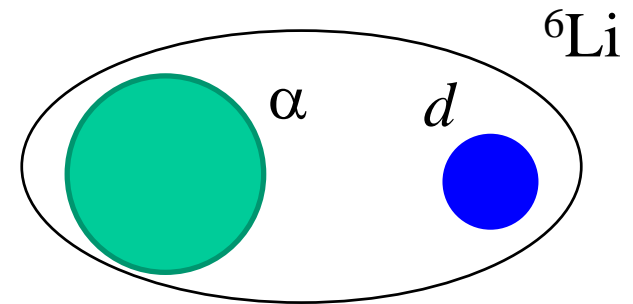
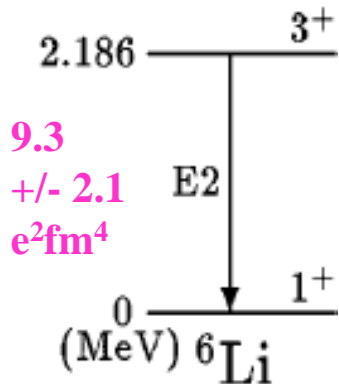


Introduction

Impurity effects: one of the main interests of hypernuclear physics
how does a Λ particle affect several properties of atomic nuclei?

- size, shape, density distribution, single-particle energy, shell structure, fission barrier.....

the most prominent example:
the reduction of $B(E2)$ in ${}^7_{\Lambda}\text{Li}$

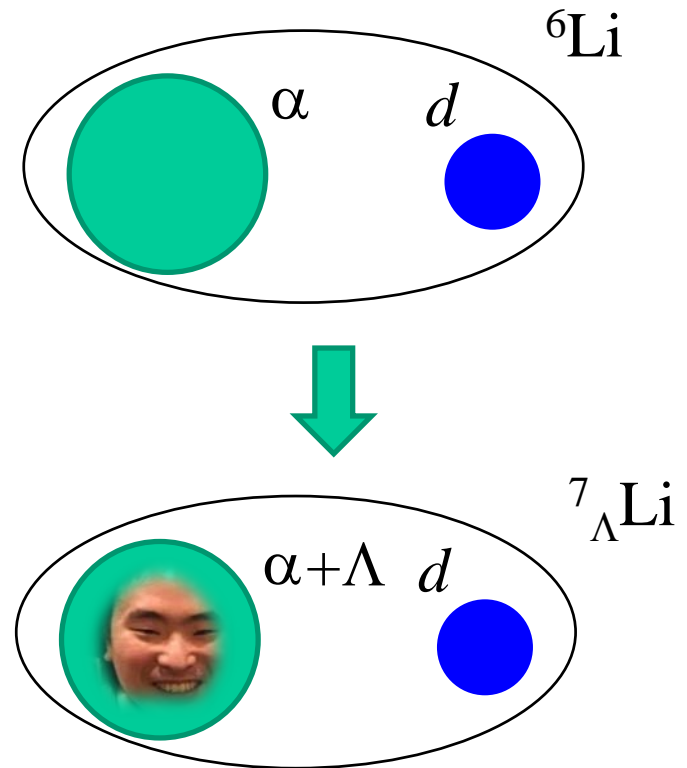
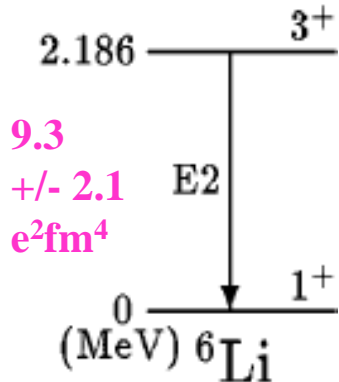


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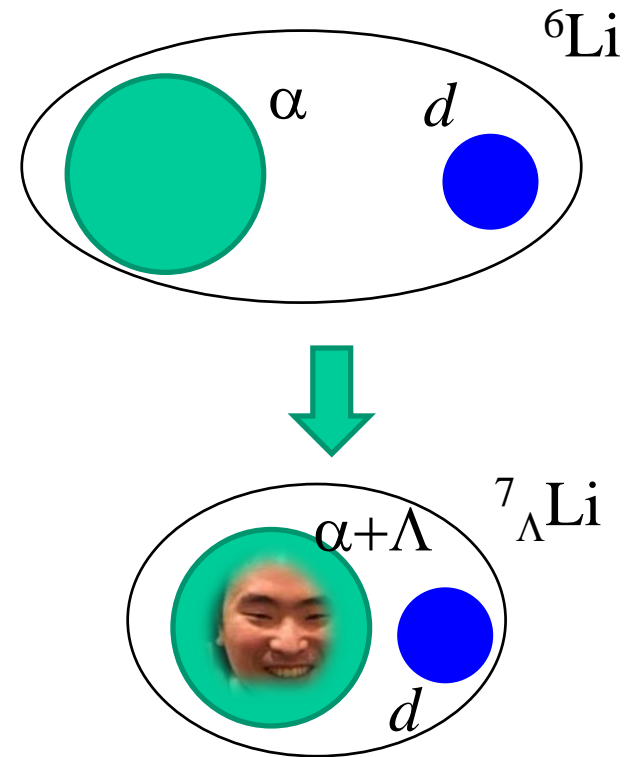
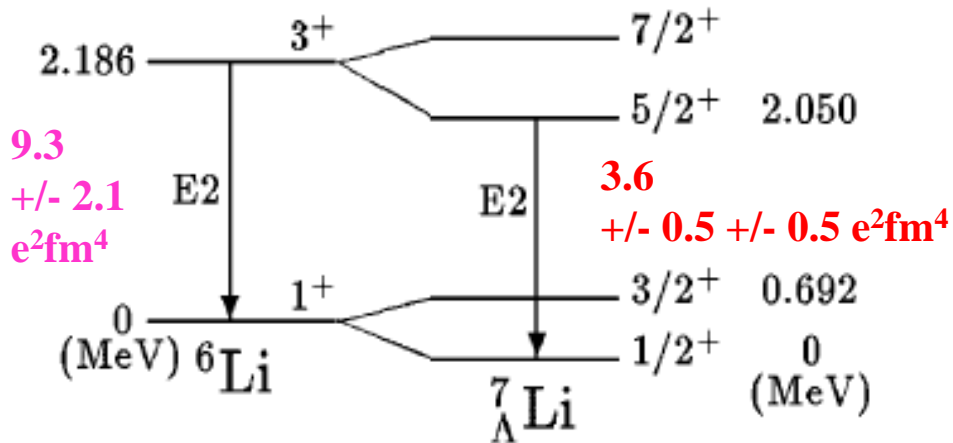


Introduction

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the most prominent example:
 the reduction of $B(E2)$ in ${}^7_{\Lambda}\text{Li}$



K. Tanida et al., PRL86 ('01) 1982

about 19% reduction of size
 (shrinkage effect)

Introduction

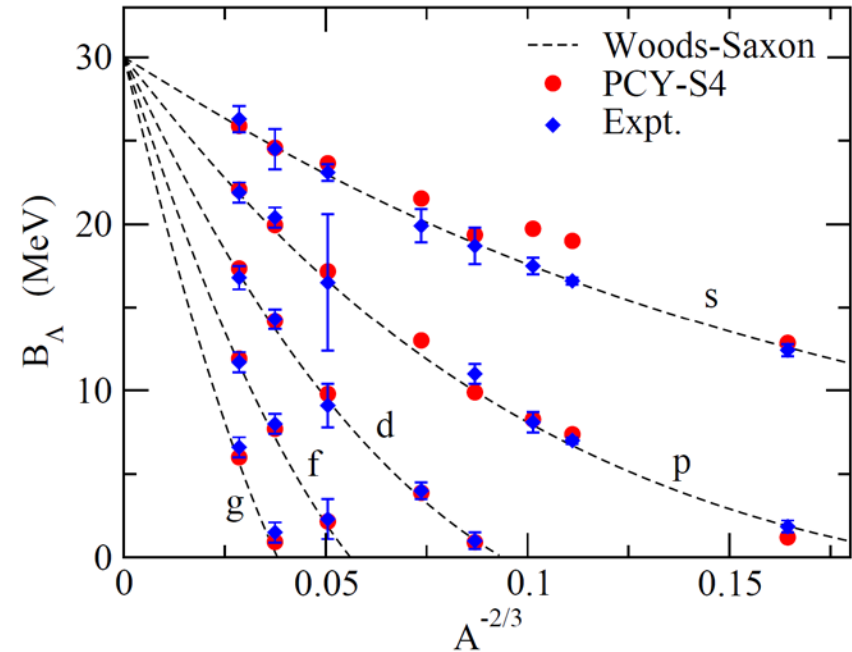
Impurity effects: one of the main interests of hypernuclear physics

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Theoretical approaches:

- ✓ cluster model
- ✓ shell model
- ✓ AMD
- ➔ ✓ self-consistent mean-field models

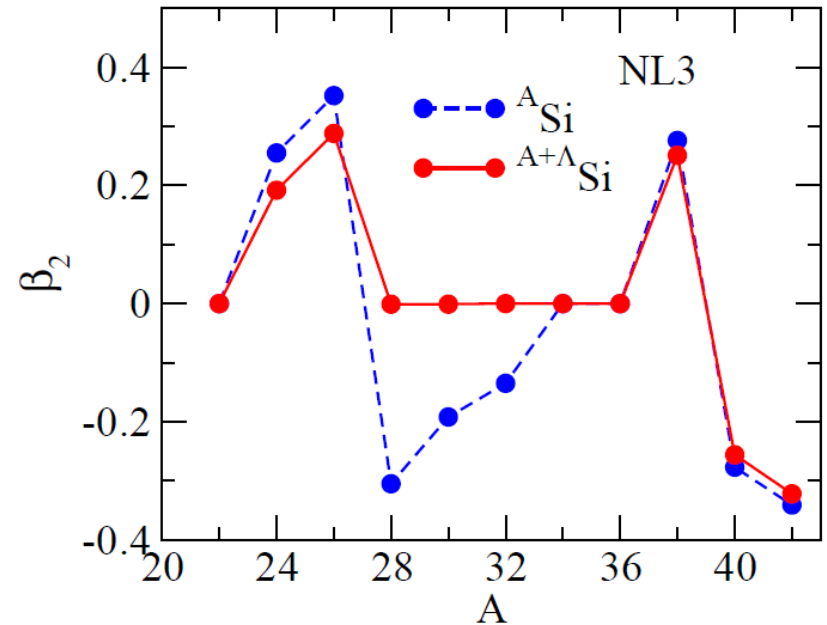
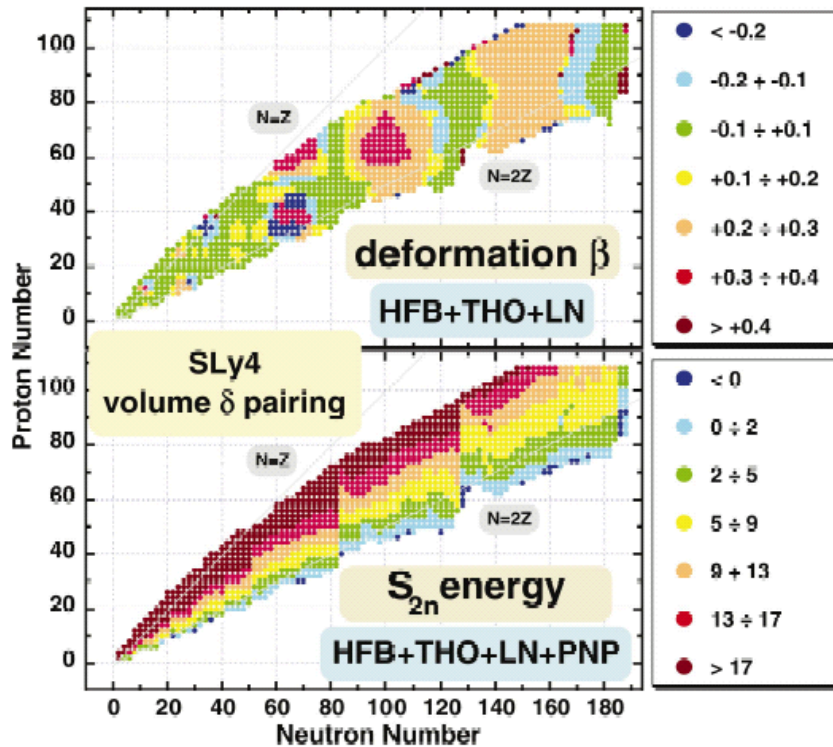
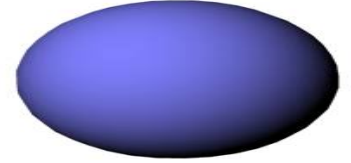


K.H. and J.M. Yao,
Int. Rev. Nucl. Phys. 10 ('16) 263

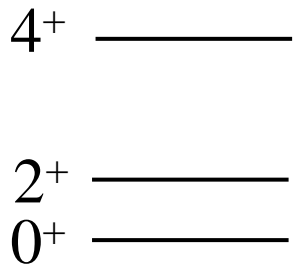
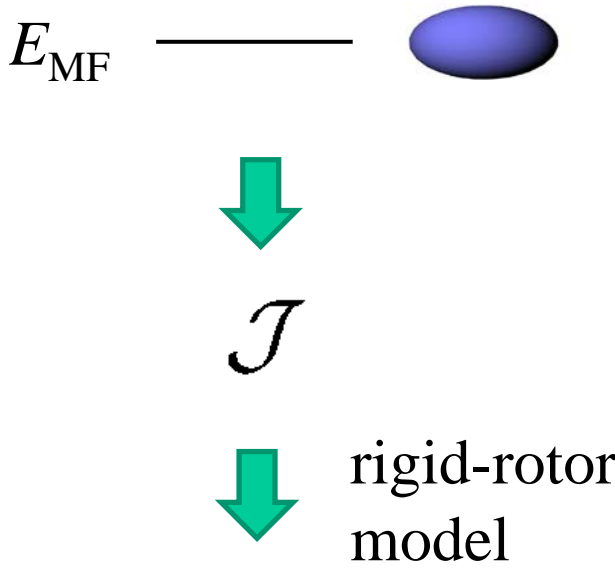
Mean-field approximation and beyond

Self-consistent mean-field (Hartree-Fock) method:

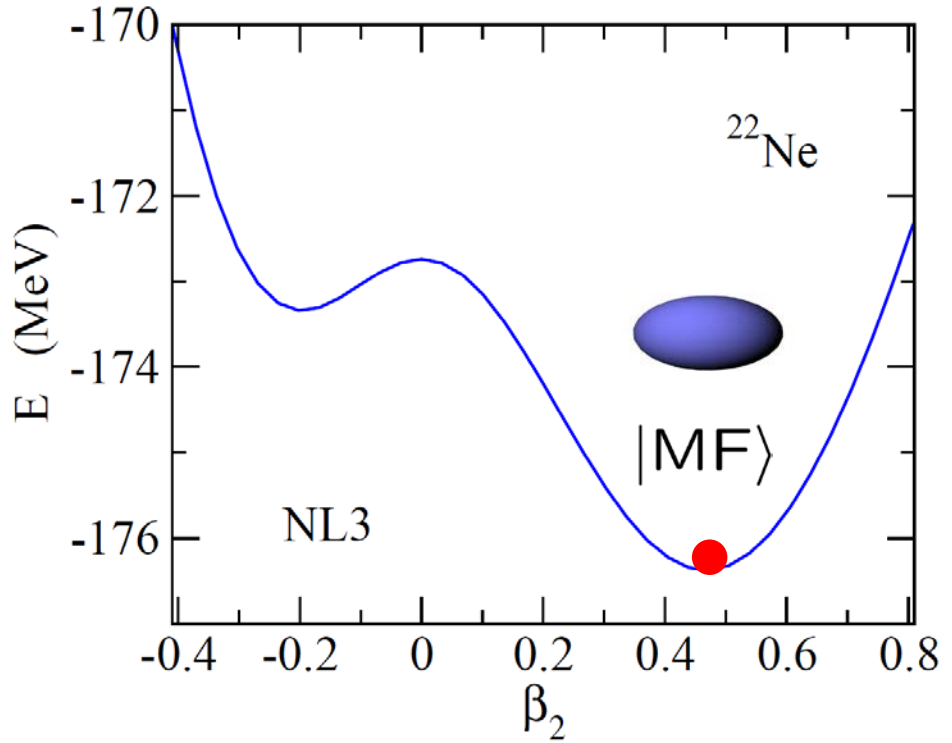
- independent particles in a mean-field potential
- global theory for the whole nuclear chart
- body-fixed frame → intuitive picture for nuclear deformation
- optimized shape can be automatically determined



spectrum based on the mean-field approximation?

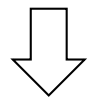
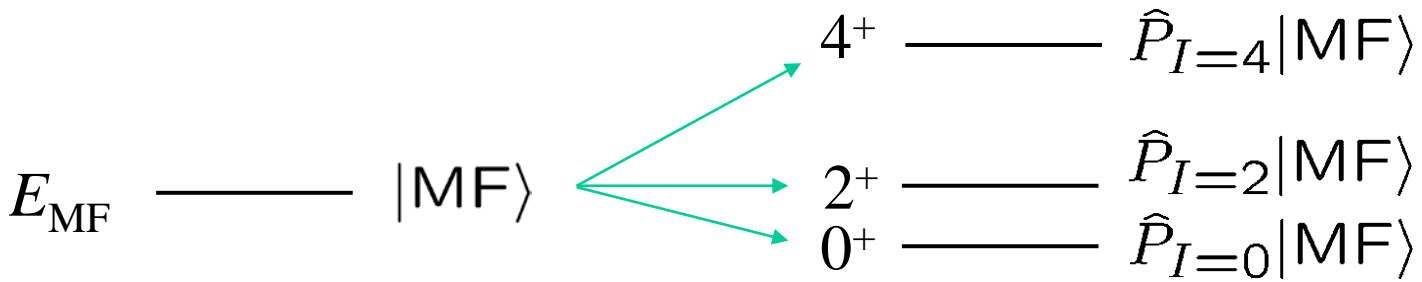


$$E_I = \frac{I(I + 1)\hbar^2}{2\mathcal{J}}$$

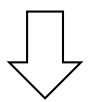


spectrum based on the mean-field approximation?

angular mom.
projection



\mathcal{J}



rigid-rotor
model

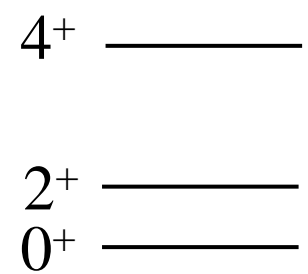
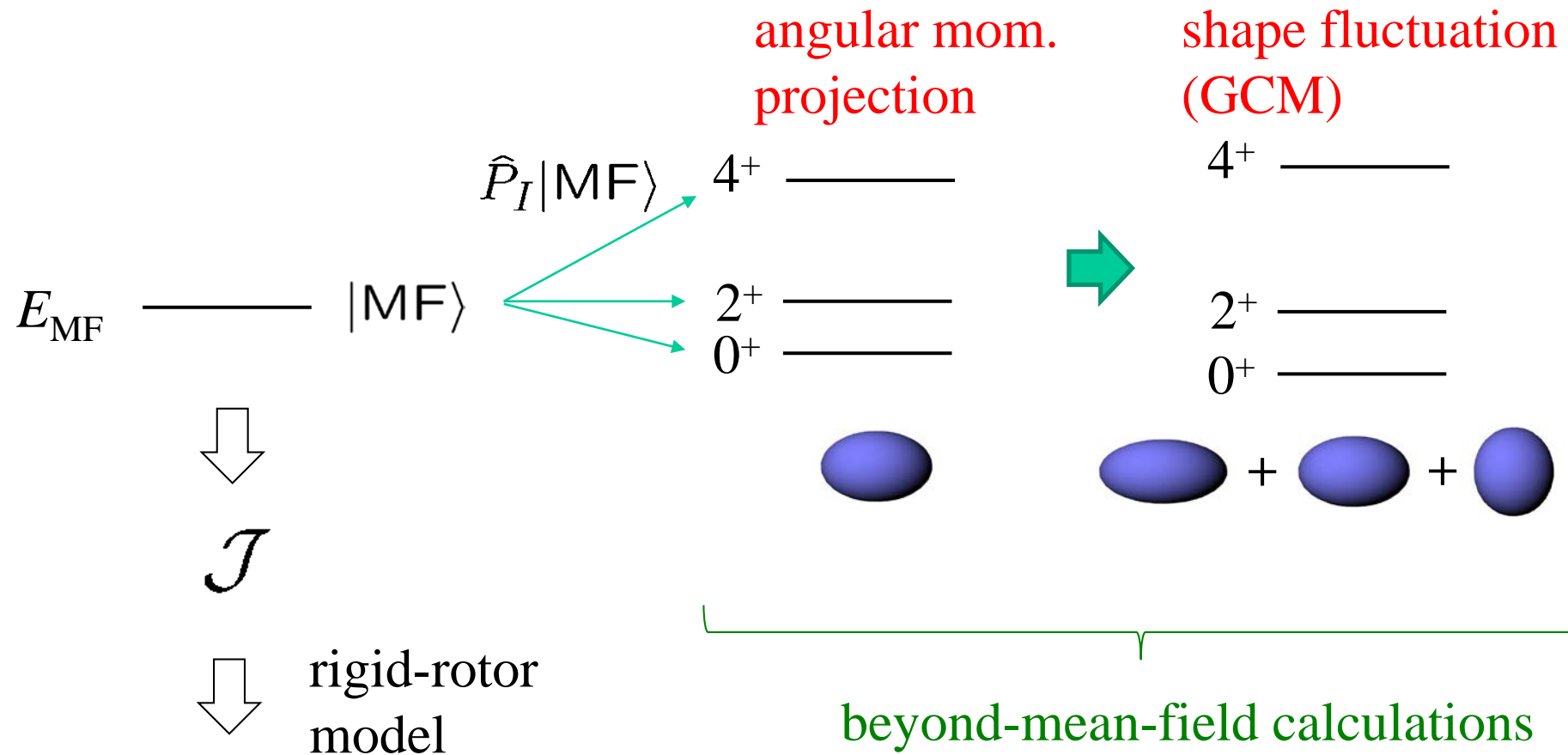
4^+ —————

2^+ —————

0^+ —————

$$E_I = \frac{I(I + 1)\hbar^2}{2\mathcal{J}}$$

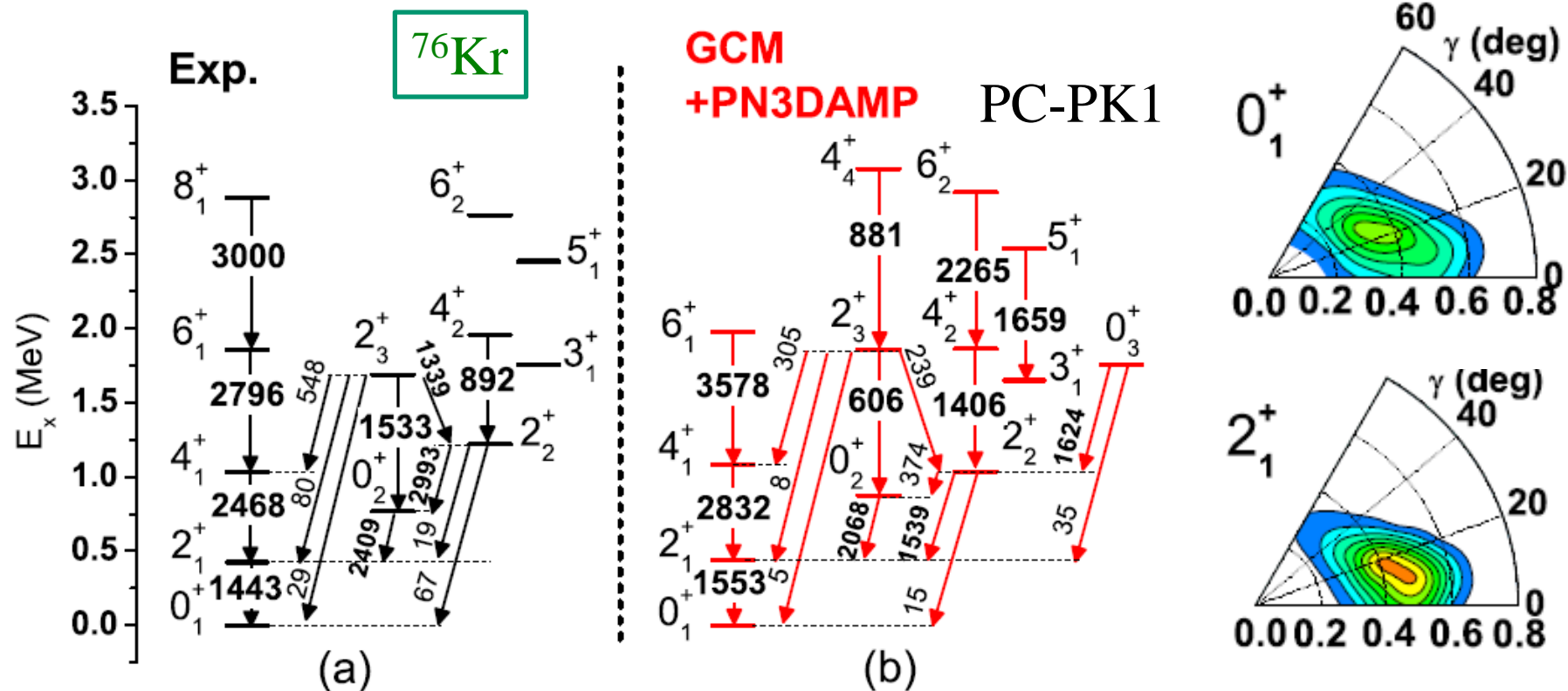
spectrum based on the mean-field approximation?



$$E_I = \frac{I(I + 1)\hbar^2}{2\mathcal{J}}$$

beyond mean-field calculations

- ✓ angular momentum + particle number projections
- ✓ quantum fluctuation (GCM)



J.M. Yao, K.H., Z.P. Li, J. Meng, and P. Ring, PRC89 ('14) 054306

cf. collective coordinates: Quadrupole moments (local operators)

Beyond Mean-Field calculations for hypernuclei

◆ Projection+GCM for the whole (A_c+1) system

H. Mei, K.H. and J.M. Yao, PRC93 ('16) 011301(R)

$$|\Psi_{IM}\rangle = \int d\beta f(\beta) \hat{P}_{MK}^I \hat{P}^N \hat{P}^Z \left[|\Psi_{A_c}(\beta)\rangle |\Psi_{\Lambda}(\beta)\rangle \right]$$

cf. Hill-Wheeler eq. for each I

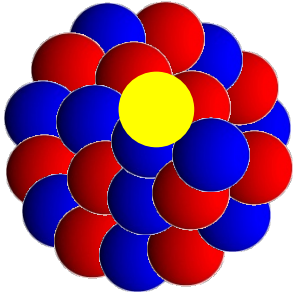
◆ Microscopic particle-rotor model for single- Λ hypernuclei

H. Mei, K.H., J.M. Yao, and T. Motoba,

- ✓ PRC90 ('14) 064302
- ✓ PRC91 ('15) 064305
- ✓ PRC93 ('16) 044307
- ✓ PRC96 ('17) 014308
- ✓ arXiv: 1804.06558.

$$|\Psi_{IM}\rangle = \sum_{j,l,I_c} \left[\begin{array}{c} \Lambda \\ \circ \\ \text{---} \\ \circ \\ I_c \end{array} \right]_{j,l} \quad (\text{IM})$$

Microscopic particle-rotor model for hypernuclei



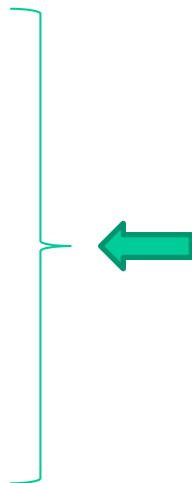
hypernucleus: a clear separation of deg. of freedom

→ Λ +core model

Λ +core model with
core excitations

$$|g.s.\rangle \sim \psi_{s_{1/2}}(\Lambda) \otimes \Psi_{\text{core}}(0^+) \\ + \psi_{d_{5/2}}(\Lambda) \otimes \Psi_{\text{core}}(2^+) + \dots$$

4+ _____
2+ _____
0+ _____
core nucleus



beyond MF
(proj.+GCM)
calculations

- ✓ fully microscopic
- ✓ shape fluctuation
cf. conventional
part.-rot model
- ✓ no Pauli principle
- ✓ rot. and vib. on the equal
footing
- ✓ transitional core

◆ Microscopic particle-rotor model for single- Λ hypernuclei

H. Mei, K.H., J.M. Yao, and T. Motoba, PRC90('14)064302, PRC91('15) 064305
 PRC93('16)044307, PRC96('17) 014308

- i) beyond mean-field calculations for e-e core: $|\Phi_{0+}\rangle, |\Phi_{2+}\rangle, |\Phi_{4+}\rangle, \dots$
- ii) coupling of Λ to the core states

$$|\Phi_{IM}\rangle = \sum_{j,l,I_c} \left[\begin{array}{c} \Lambda \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ I_c \end{array} \right] (IM)$$

Λ +core model with
core excitations

$$\left\{ \begin{array}{l} \Psi_{JM}(\mathbf{r}_\Lambda, \{\mathbf{r}_i\}) = \sum_{n,j,l,I} R_{jlnI}(\mathbf{r}_\Lambda) [\mathcal{Y}_{j\ell}(\hat{\mathbf{r}}_\Lambda) \otimes \Phi_{nI}(\{\mathbf{r}_i\})]^{(JM)} \\ \\ H = H_c + T_\Lambda + \sum_{i=1}^{A_c} v_{N\Lambda}(\mathbf{r}_\Lambda, \mathbf{r}_i) \end{array} \right.$$



coupled equations for R_{jlnI}

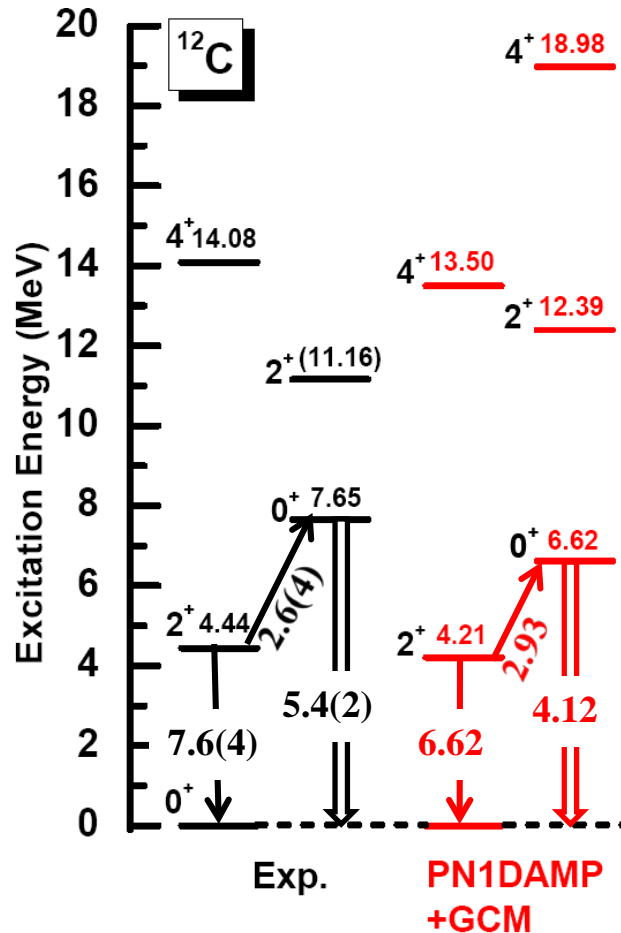
$v_{N\Lambda}$: point coupling relativistic N Λ interaction

Microscopic Particle-Rotor Model for Λ hypernuclei

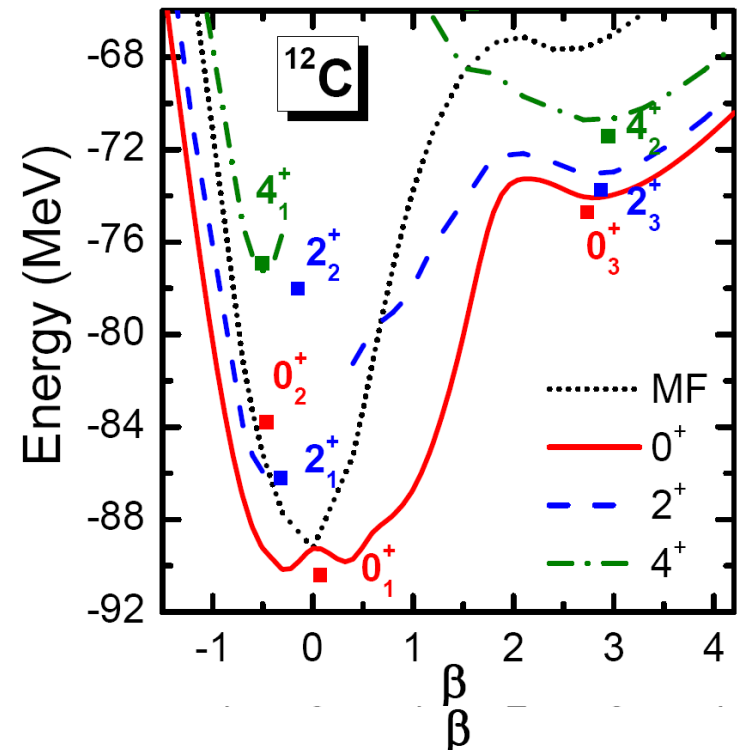
Example: $^{13}_{\Lambda}\text{C}$

i) beyond mean-field calculations for e-e core (^{12}C): GCM + projections

$$|\Phi_{I_c M_c}\rangle = \int d\beta f(\beta) |\Psi_{I_c M_c}(\beta)\rangle = \int d\beta f(\beta) \hat{P}_{M_c K_c}^{I_c} \hat{P}^N \hat{P}^Z |\Psi_{\text{MF}}(\beta)\rangle$$



- ✓ axial symmetry
- ✓ relativistic PC-F1



Microscopic Particle-Rotor Model for Λ hypernuclei

Example: $^{13}_{\Lambda}\text{C}$

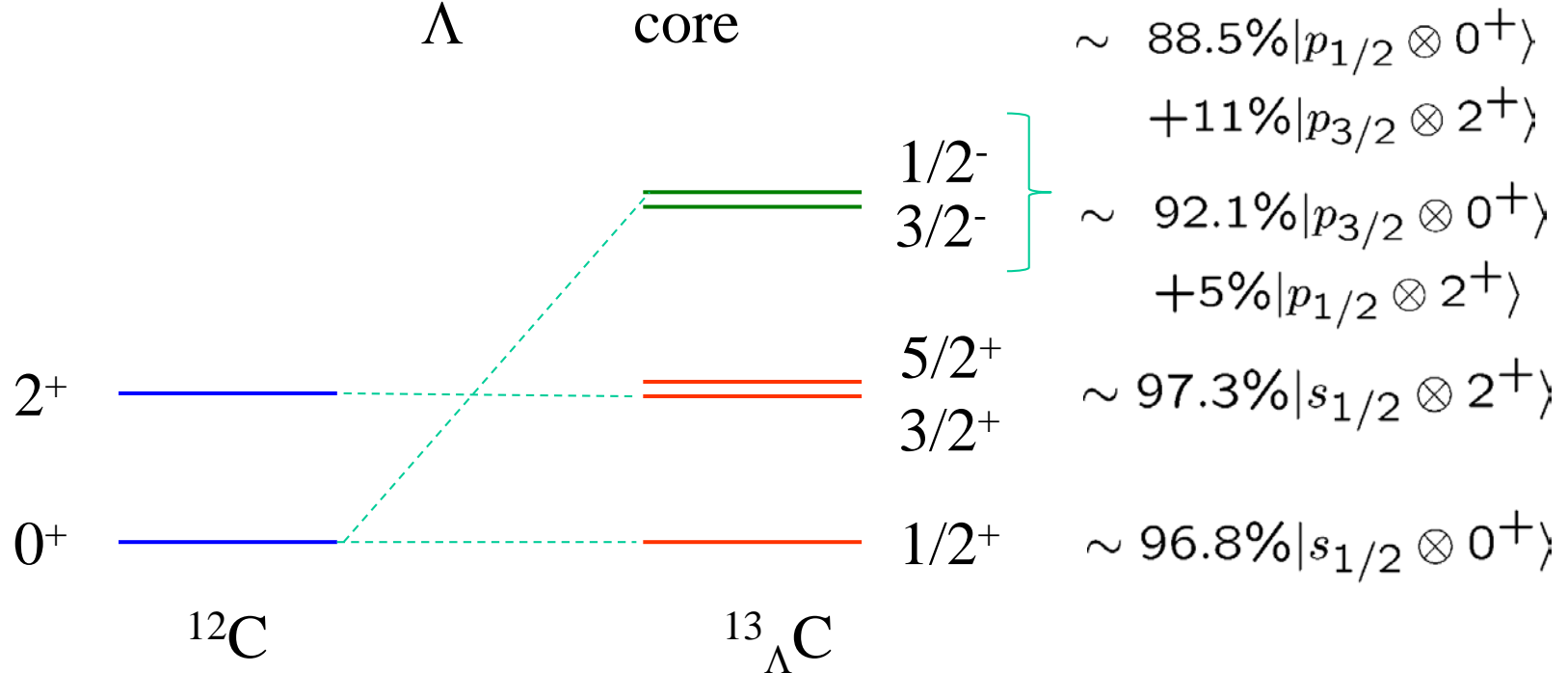
(i) beyond mean-field calculations for e-e core (^{12}C)

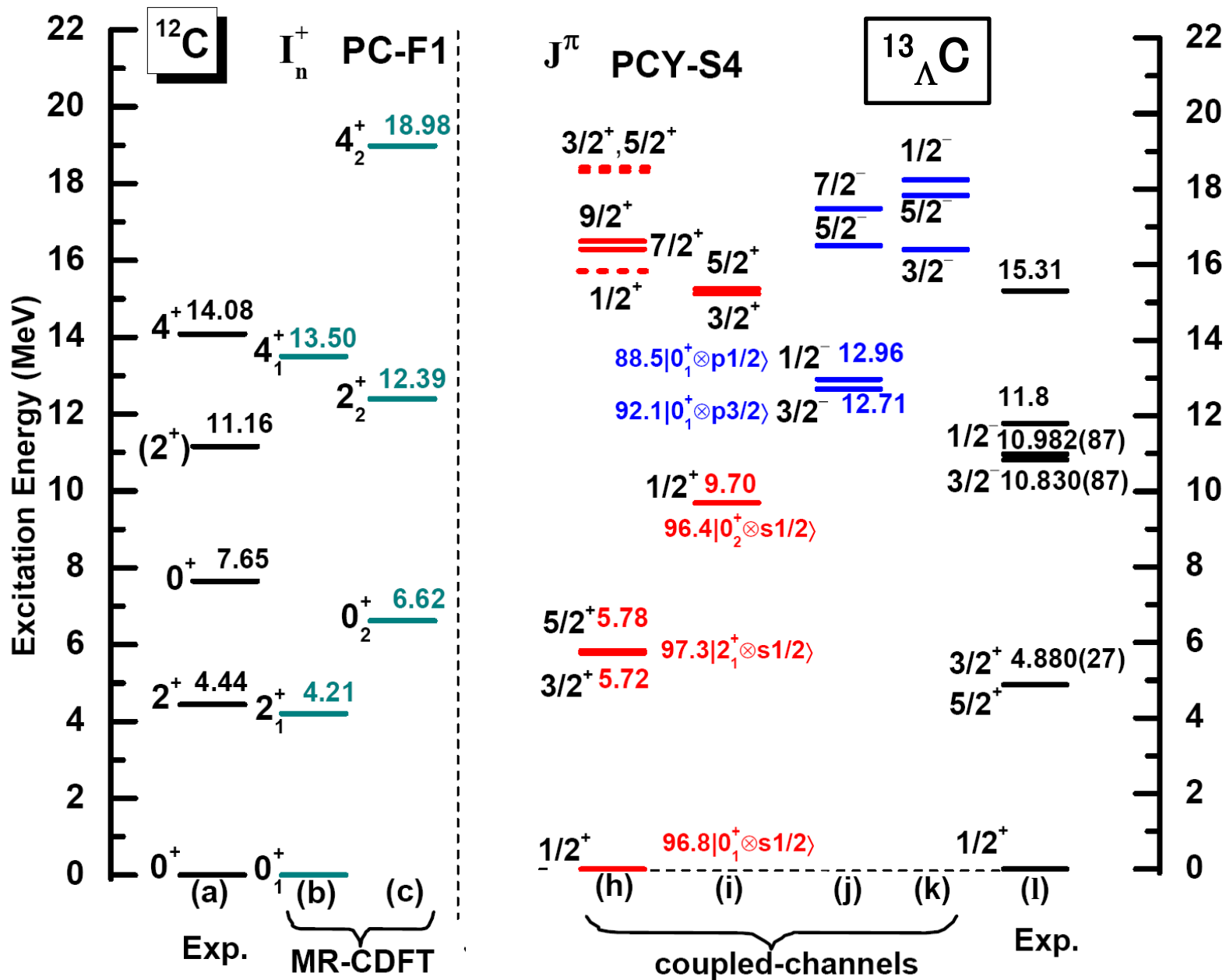
(ii) coupling of Λ to the core states

$$|\Phi_{IM}\rangle = \sum_{j,l,I_c} [\psi_{jl}(r_{\Lambda}) \otimes |\Phi_{I_c}\rangle]^{(IM)}$$

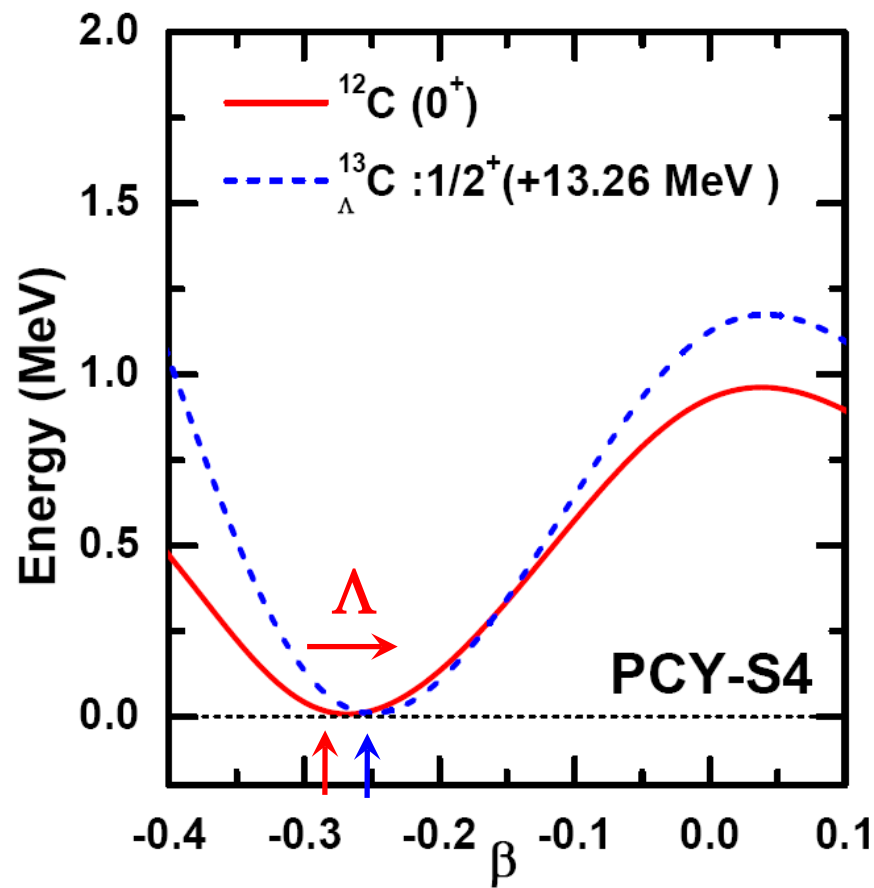
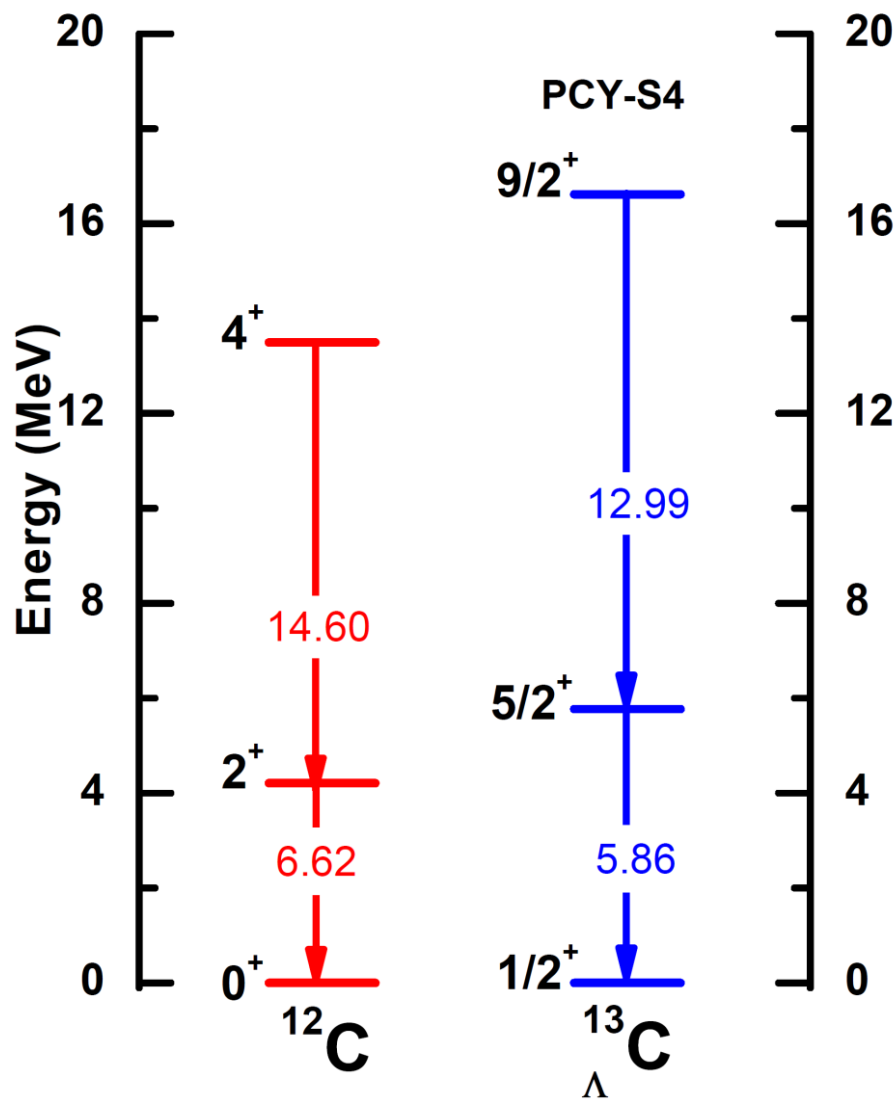
Λ

core





B(E2) transition rates ($e^2\text{fm}^4$)

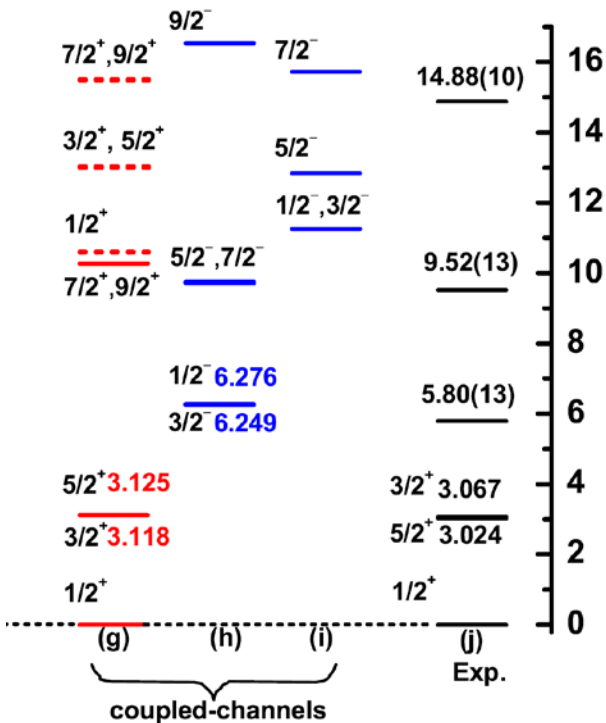


	^{12}C	$^{13}_{\Lambda}\text{C}$
β	-0.27	-0.25
r_p (fm)	2.44	2.39

➤ B(E2) : ~ 11% reduction

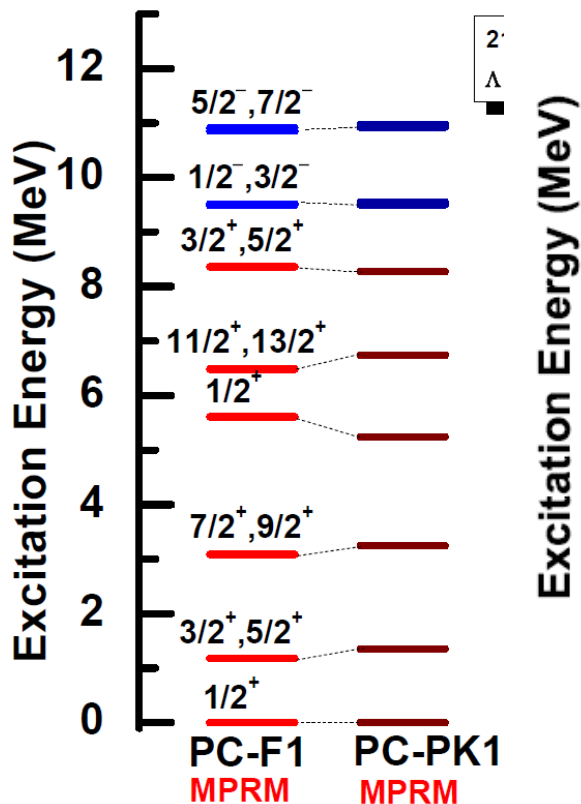
other applications:

${}^9_{\Lambda}\text{Be}$

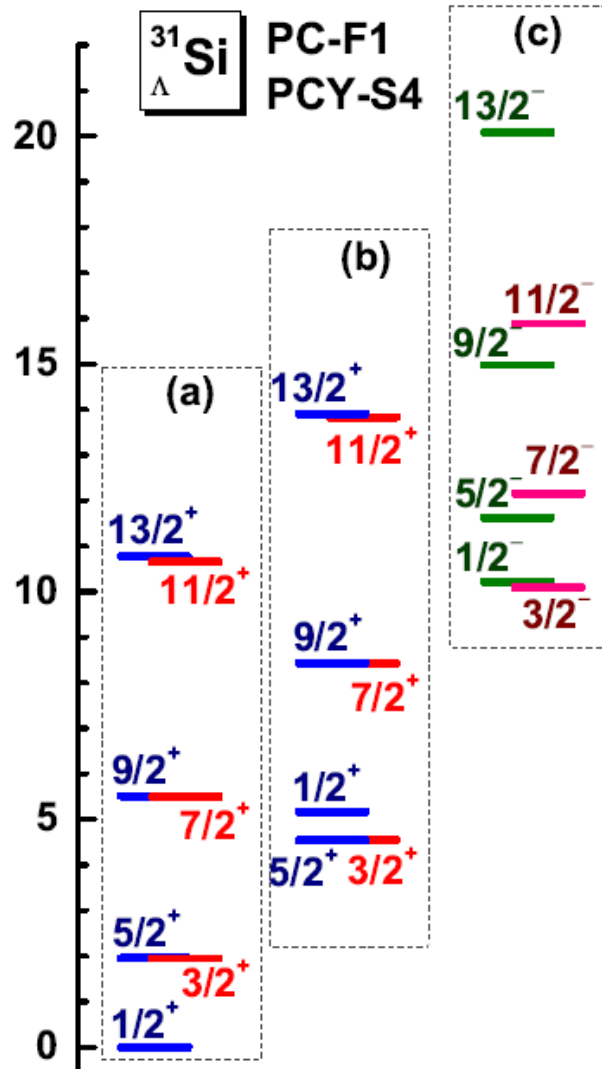


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${}^{21}_{\Lambda}\text{Ne}$

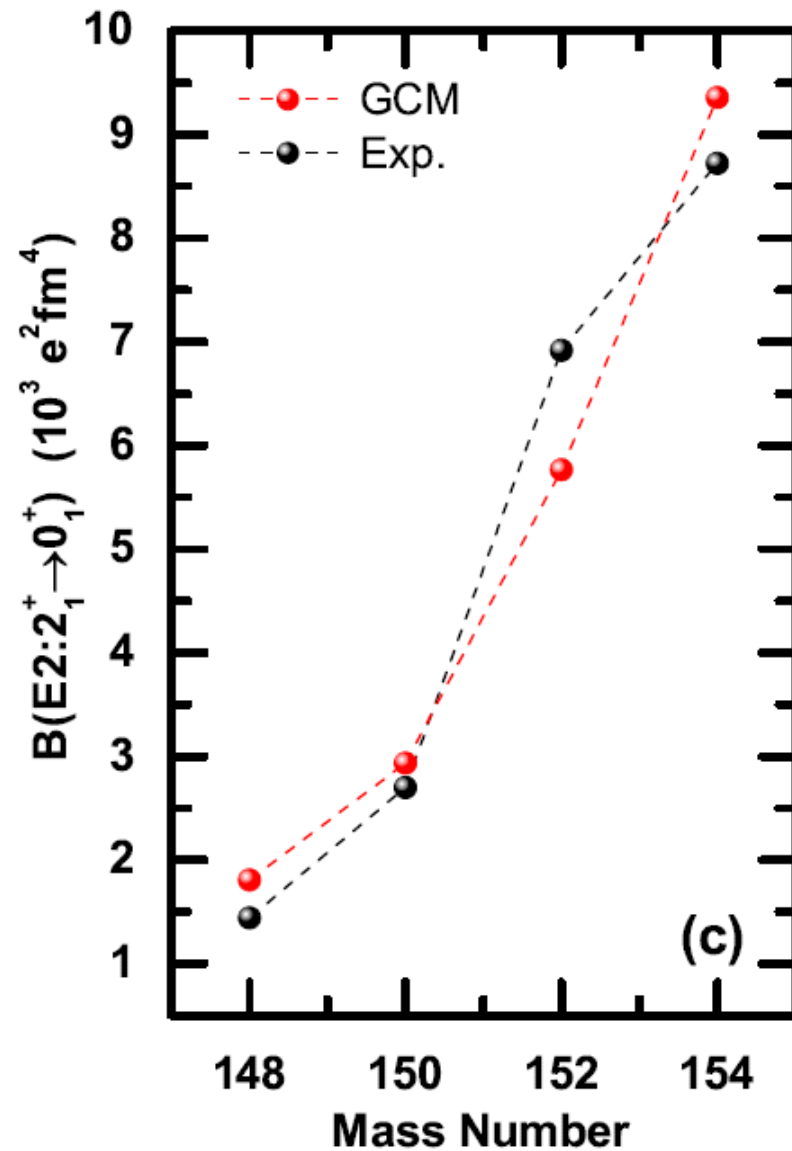
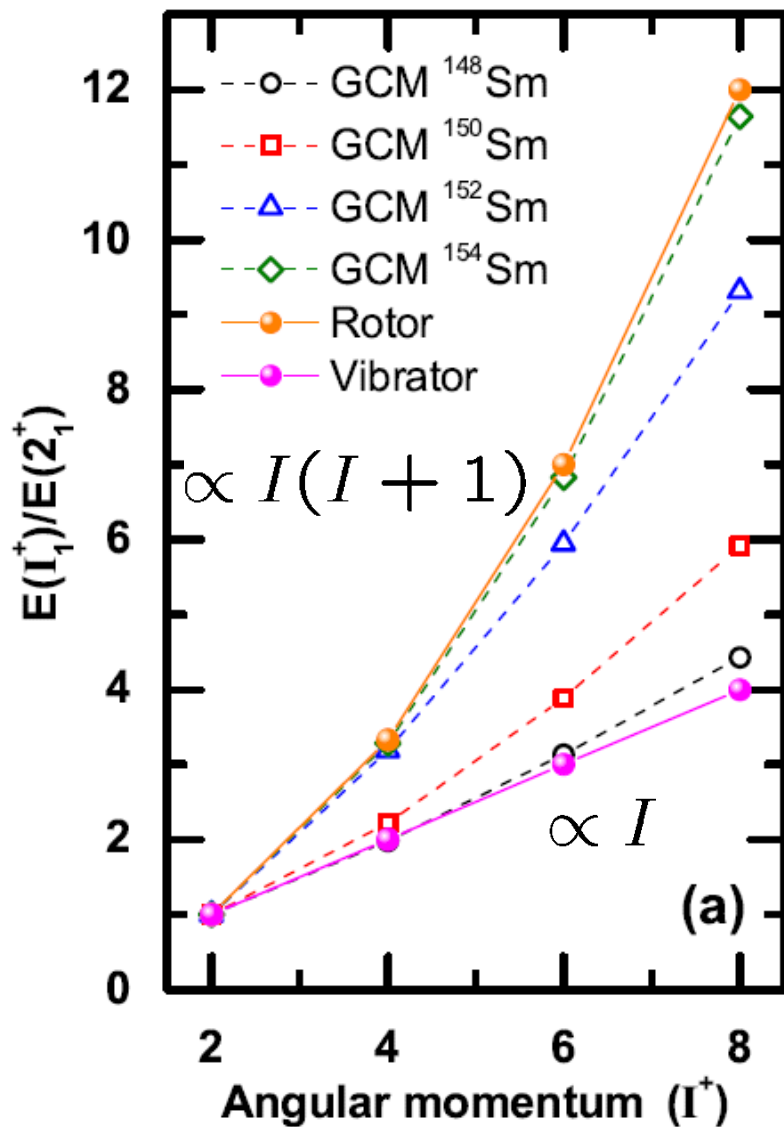


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PRC91 ('15) 064305



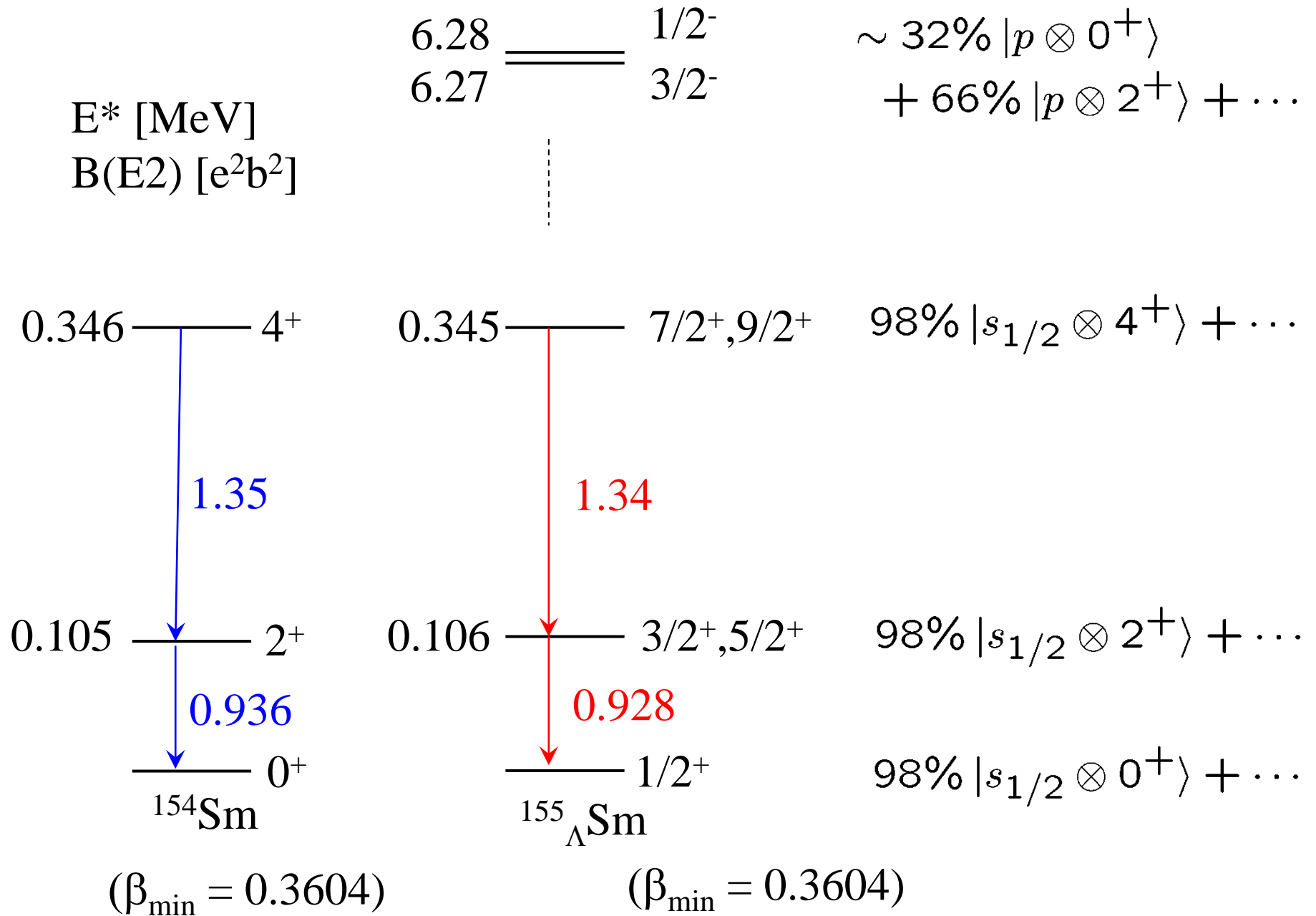
H. Mei, K.H., J.M. Yao,
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arXiv: 1804.06558.

Application to Sm isotopes

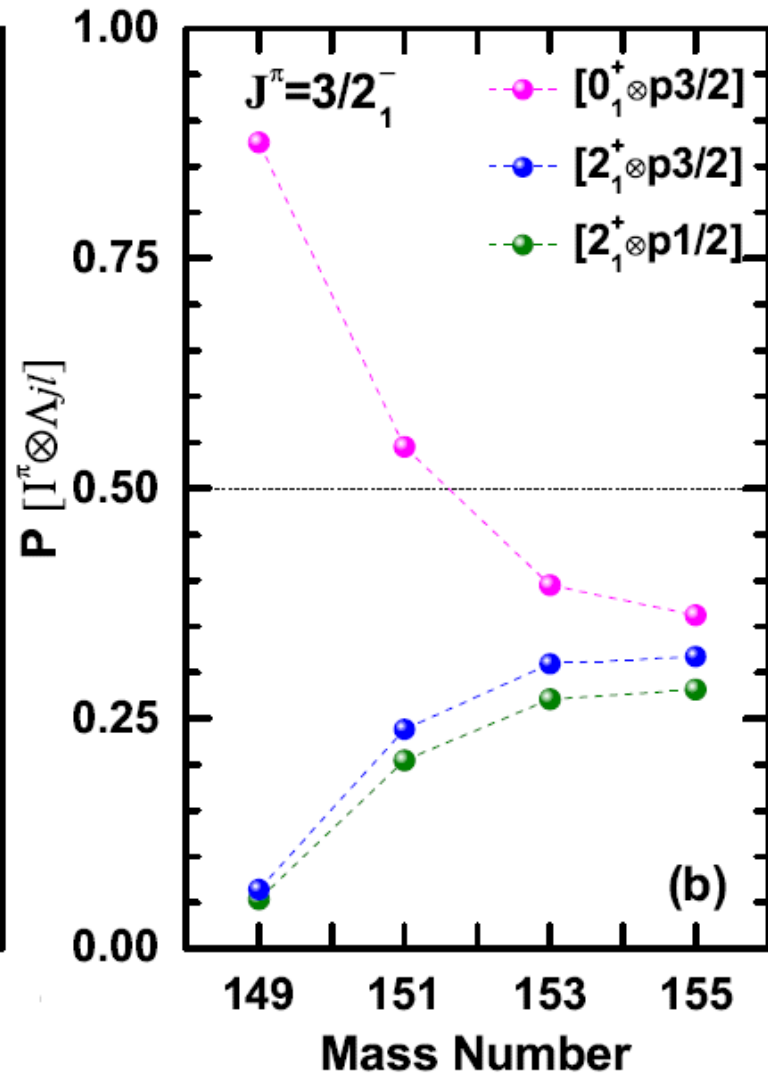
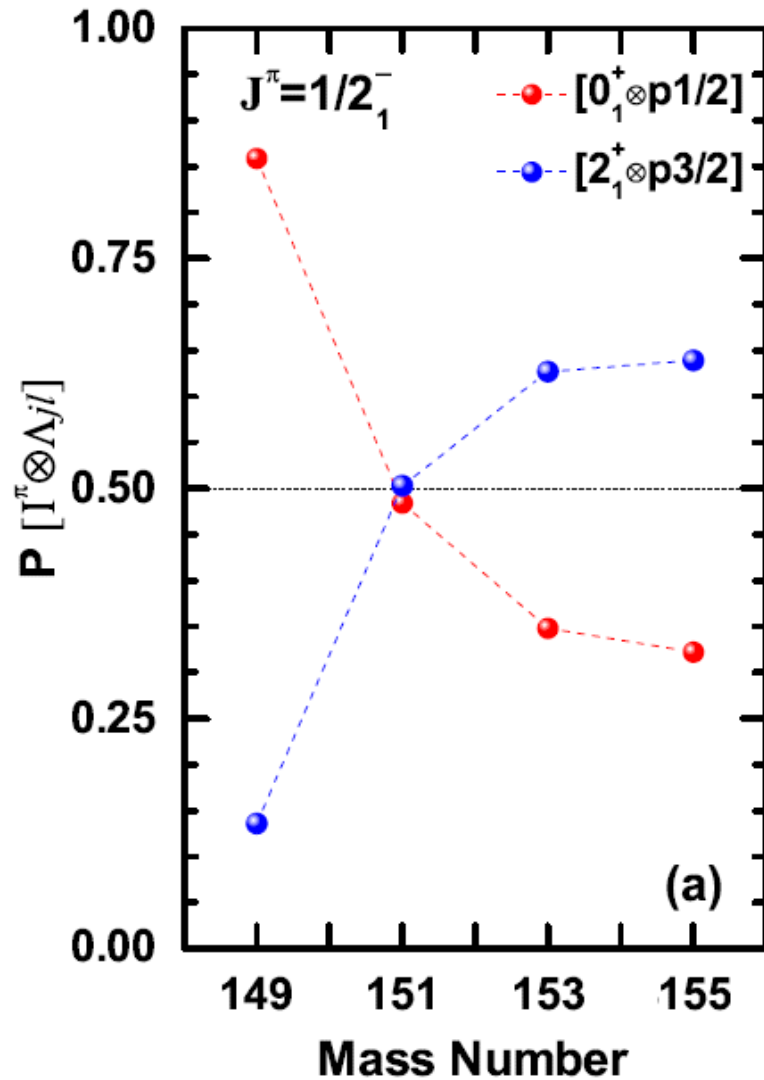


Results for $^{155}_{\Lambda}\text{Sm}$

H. Mei, K.H., J.M. Yao, T. Motoba, PRC91('15) 064305



weak coupling \rightarrow strong coupling



H. Mei, K.H., J.M. Yao, and T. Motoba,
 PRC96 ('17) 014308

Summary

Applications of Beyond-Mean-Field method to hypernuclei

➤ Low-lying spectra of Λ hypernuclei

Microscopic particle-rotor/vibrator model

- ✓ Λ + GCM states for core: particle-core model with core excitations
- ✓ the first calculations for low-lying spectra for hypernuclei based on mean-field type calculations
- ✓ from C to Sm: both rotor and vibrator on an equal footing
- ✓ transitional nuclei

➤ Future perspectives

- ✓ extension to include triaxiality (cf. $^{25}_{\Lambda}\text{Mg}$)